



Partial wave analysis of the $\pi^+\pi^-$ system
produced in double gap
p-p collisions at $\sqrt{s} = 7$ TeV

Taesoo Kim*, Ju Hwan Kang

Yonsei University

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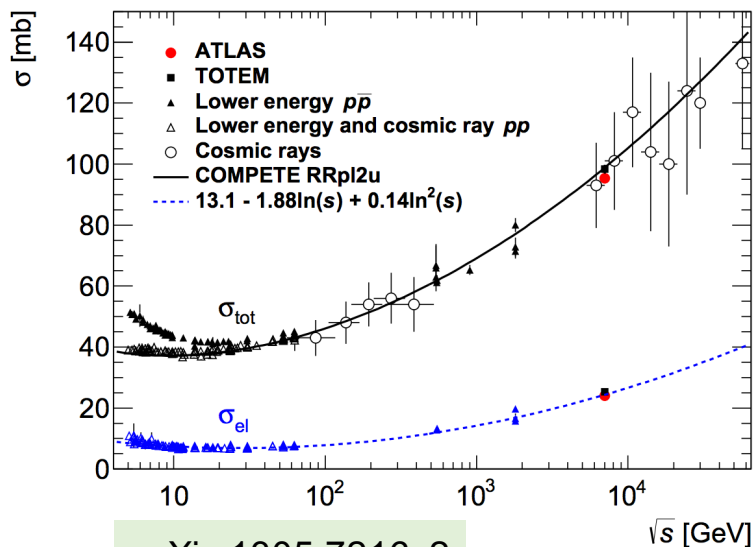
HIM Meeting, IBS

- Motivation of central diffraction
- Data analysis
- Partial wave analysis of $\pi^+ \pi^-$ system
- Conclusion

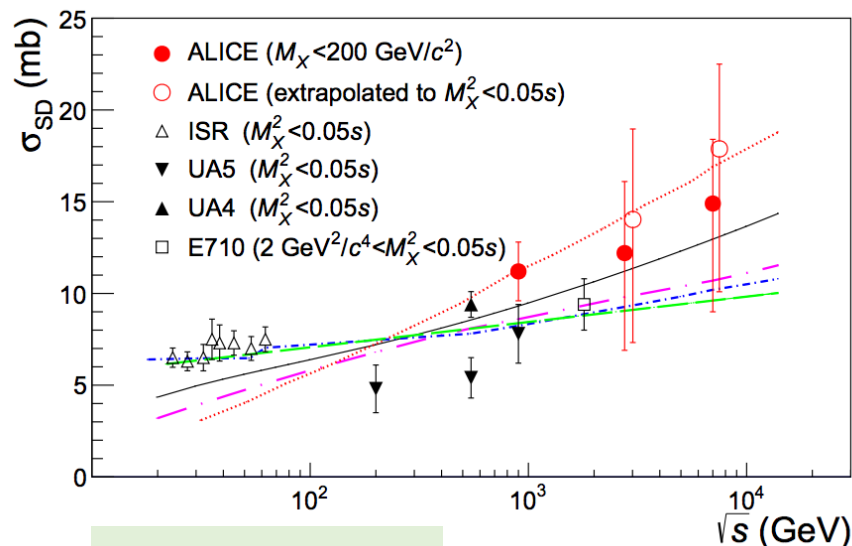
Motivation: inelastic cross section

Total cross section in p-p collisions

- $\sigma_{\text{tot}} = \sigma_{\text{el}} + \sigma_{\text{INEL}}$, and σ_{INEL} increases faster than σ_{el} at high energies due to contributions from **diffractive processes**. Therefore, the diffraction can't be ignored at high energies.



arXiv:1305.7216v2



arXiv:1208.4968v1

- $\sigma_{\text{INEL}} = \sigma_{\text{non-diff. (ND)}} + \sigma_{\text{single-diff. (SD)}} + \sigma_{\text{double-diff. (DD)}} + \sigma_{\text{central-diff. (CD)}} + \dots$

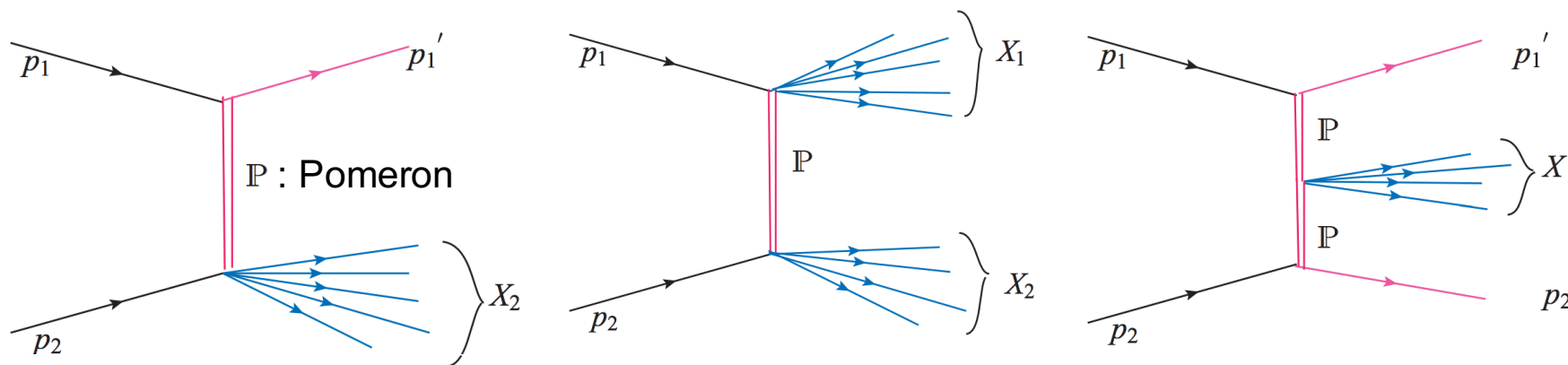
\sqrt{s} (TeV)	$\sigma_{\text{SD}}/\sigma_{\text{INEL}}$	$\sigma_{\text{DD}}/\sigma_{\text{INEL}}$
0.9	0.21 ± 0.03	0.11 ± 0.03
2.76	$0.20^{+0.07}_{-0.08}$	0.12 ± 0.05
7	$0.20^{+0.04}_{-0.07}$	$0.12^{+0.05}_{-0.04}$

SD+DD contribute
30% of INEL

arXiv:1208.4968v1
(ALICE)

Motivation: diffractive processes

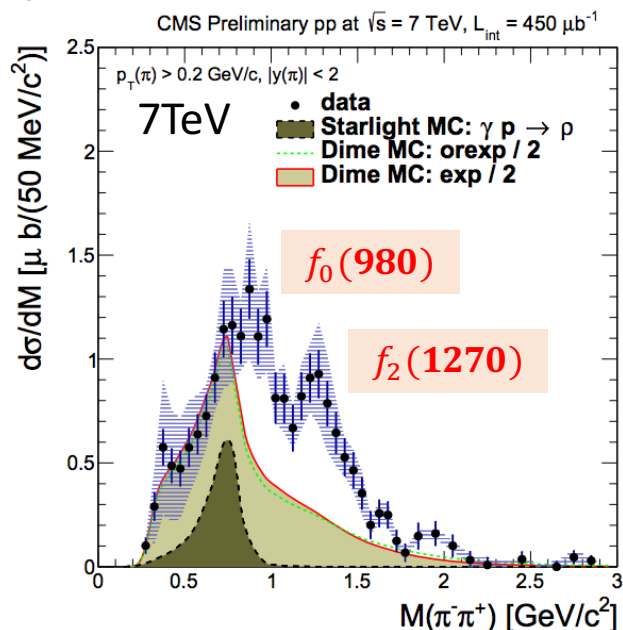
- In Regge theory, all diffractive processes can be described by **Pomeron** at high energies.
 - **Pomeron**: colour singlet object with the quantum number of the vacuum
 - While SD and DD are explained by single-Pomeron exchange, **CD is dominated by double-Pomeron exchange (DPE)**.
- The **diffraction** is defined when the momentum transfer of incoming proton is much less than the centre-of-mass energy.
 - Single Diffraction (SD): one proton is intact and one proton dissociates, $p_1 + p_2 \rightarrow p_1' + X_2$
 - Double Diffraction (DD): two protons dissociate, $p_1 + p_2 \rightarrow X_1 + X_2$
 - **Central Diffraction (CD)**: two protons are intact, $p_1 + p_2 \rightarrow p_1' + X + p_2'$



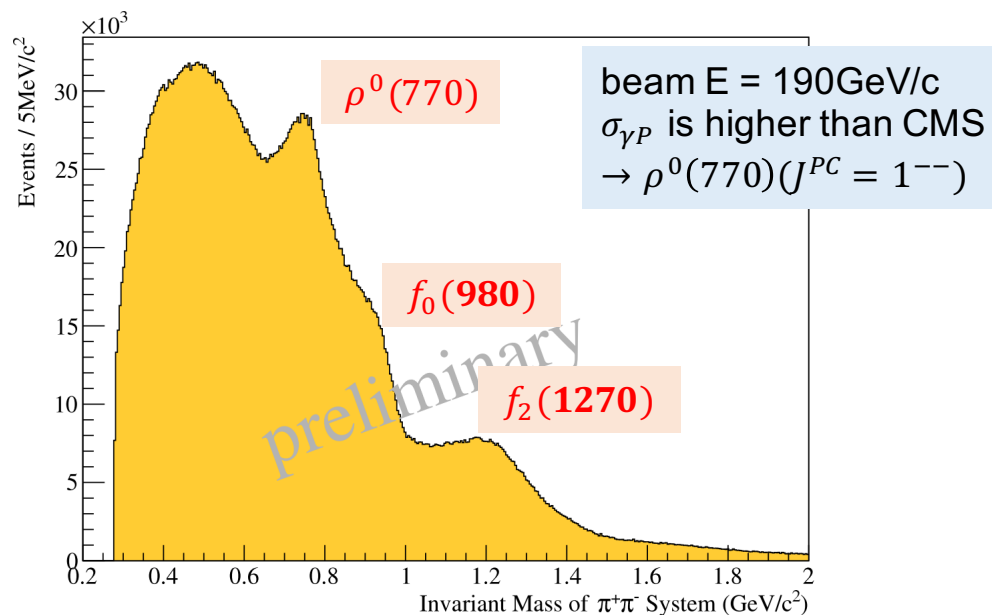
Feynmann diagrams of single (left), double (middle), and central (right) diffraction with Pomeron exchange, arXiv:1005.3894

Motivation: central diffraction (central production)

- Central diffraction, $p_1 + p_2 \rightarrow p_1' + X + p_2'$
 - produce interesting system X such as **glueballs and hybrid** due to glue-rich nature of Pomeron.
 - restrict the quantum numbers of the produced system X ($I^G J^{PC} = 0^+ \text{ even}^{++}$), so final states can be $\pi^+\pi^-$, K^+K^- , $\pi^+\pi^-\pi^+\pi^-$, etc. The $\pi^+\pi^-$ had been analyzed in other experiments, $f_0(980)$ ($J^{PC} = 0^{++}$) and $f_2(1270)$ ($J^{PC} = 2^{++}$) are observed in the $\pi^+\pi^-$ final states.



CMS result, arXiv:1610.08775v2

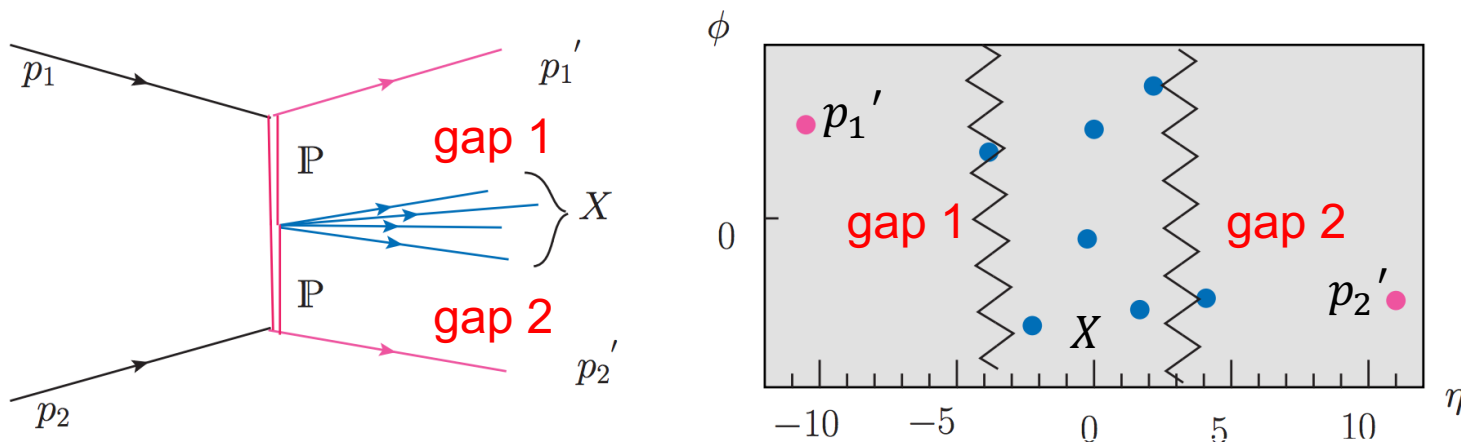


COMPASS result, arXiv:1310.3190v1

- The goal is to investigate $\pi^+\pi^-$ final states in CD and provide properties of produced particles.

Data analysis: double gap topology

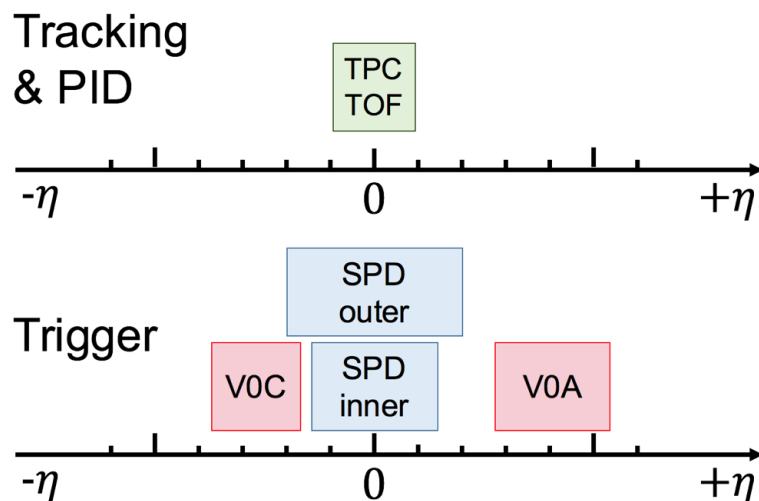
- Even though **A** Large Ion **C**ollider **E**xperiment (**ALICE**) is dedicated experiment for heavy-ion collisions, **ALICE is suitable for investigating central diffraction in p-p collisions.**
- Double gap topology
 - $p_1 + p_2 \rightarrow p_1' + X + p_2'$ can be identified if all protons are measured.
 - ALICE can't detect outgoing protons (p_1', p_2') due to absent of very forward detectors.
 - Alternatively, we can use **double gap (DG) topology** to identify CD.
 - While intact protons have large pseudorapidity (η), the produced system X has very small η because of small momentum transfers.
 - Thus, we have **two gaps between intact protons and the produced system X .**



Central diffraction with DPE and rapidity distribution of produced particles, arXiv:1005.3894

Data analysis: ALICE detectors

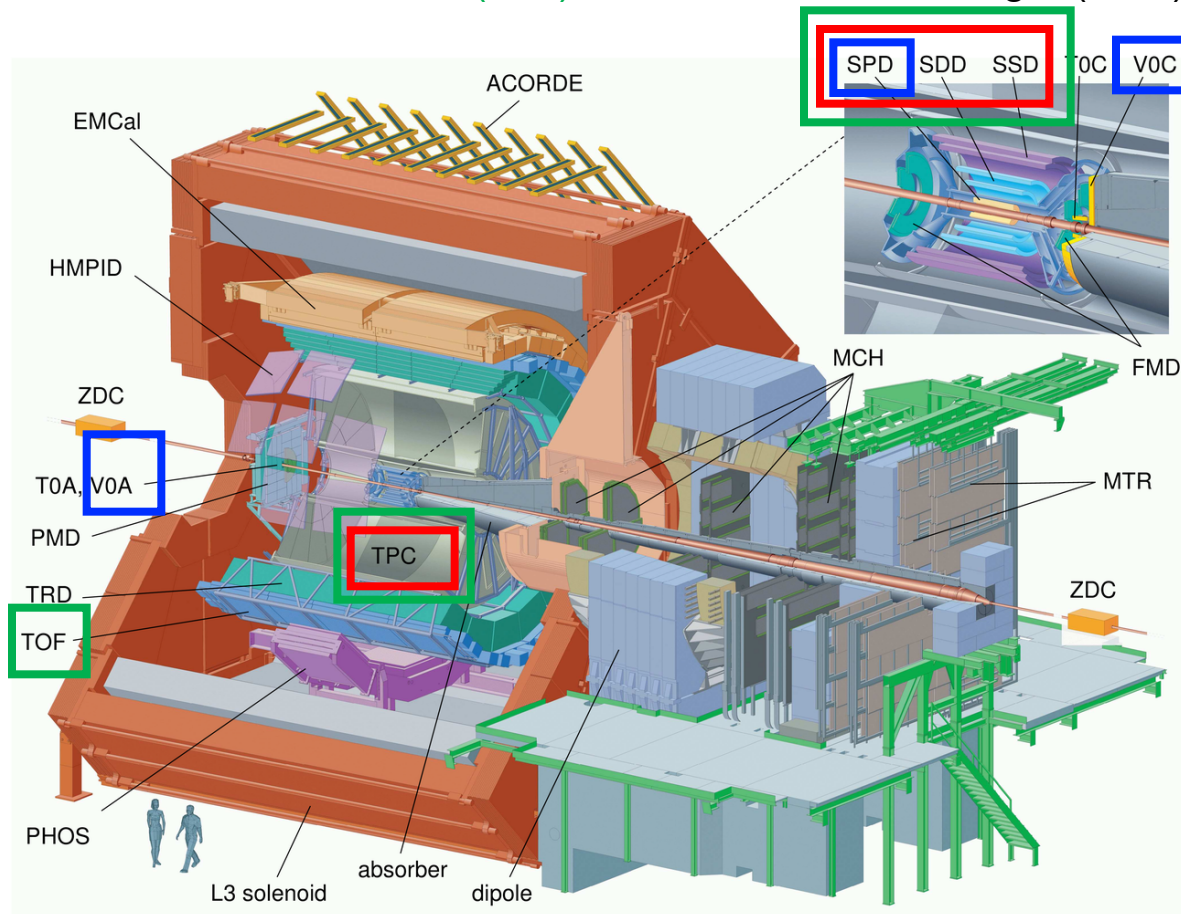
- Double gap topology in ALICE as a trigger
 - This trigger was not implemented as online in Run1. Therefore, we use offline information to reconstruct the DG trigger.
 - Requirement: **some signals in central regions without any activities in forward gaps.**
 - ALICE has **V0, FMD** at forward regions to detect gaps and **SPD** to measure centrally produced signal as trigger detectors.
 - **DG in ALICE: !V0C & !V0A & SPD**, where & (!) is logical AND (NOT)
 - No signals on V0A,C side and at least one fired chip in SPD
 - **Sub-sample: !FMDC & !V0C & !FMDA & !V0A & SPD** (enhanced gap definition)



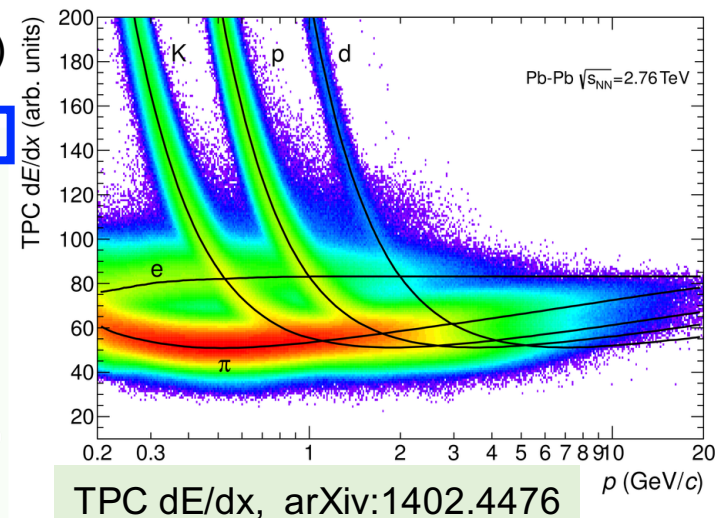
TPC: $-0.9 < \eta < 0.9$
SPD outer layer: $-2 < \eta < 2$
SPD inner layer: $-1.4 < \eta < 1.4$
V0A: $2.8 < \eta < 5.1$
V0C: $-3.7 < \eta < -1.7$
FMDA: $1.7 < \eta < 5.1$
FMDC: $-3.4 < \eta < -1.7$

Data analysis: ALICE detectors

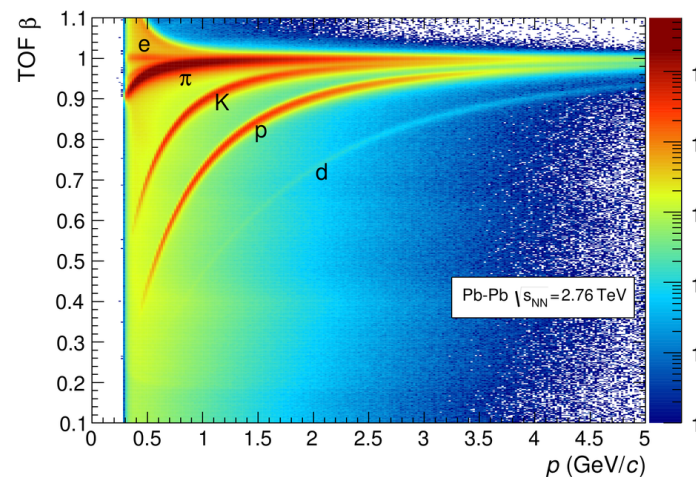
- **Trigger:** V0, Forward Multiplicity Detector (FMD), Silicon Pixel Detector (SPD)
- **Tracking:** Inner Tracking System (ITS) + Time Projection Chamber (TPC)
- **Particle Identification (PID):** ITS, TPC, Time Of Flight (TOF)



ALICE schematic view, arXiv:1402.4476



TPC dE/dx, arXiv:1402.4476



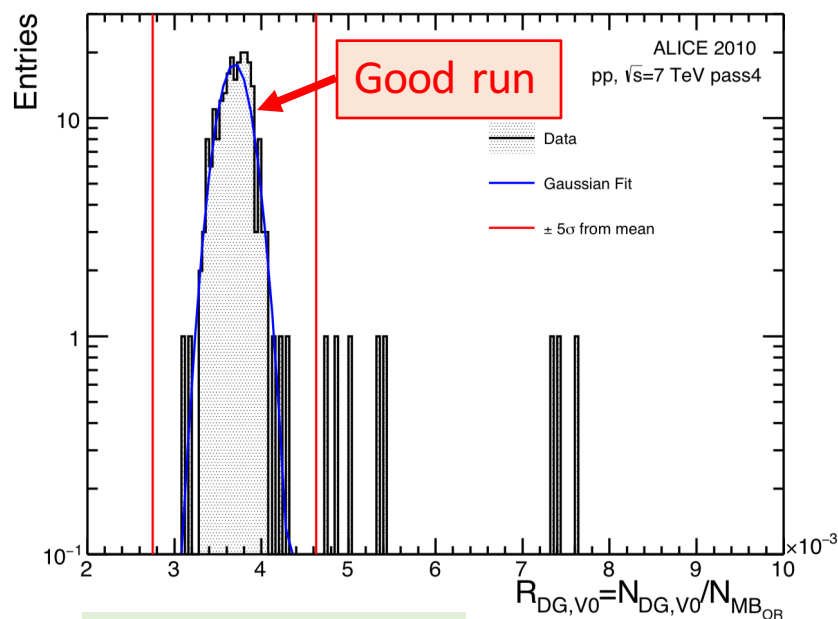
TOF particle velocity, arXiv:1402.4476

Data analysis: dataset

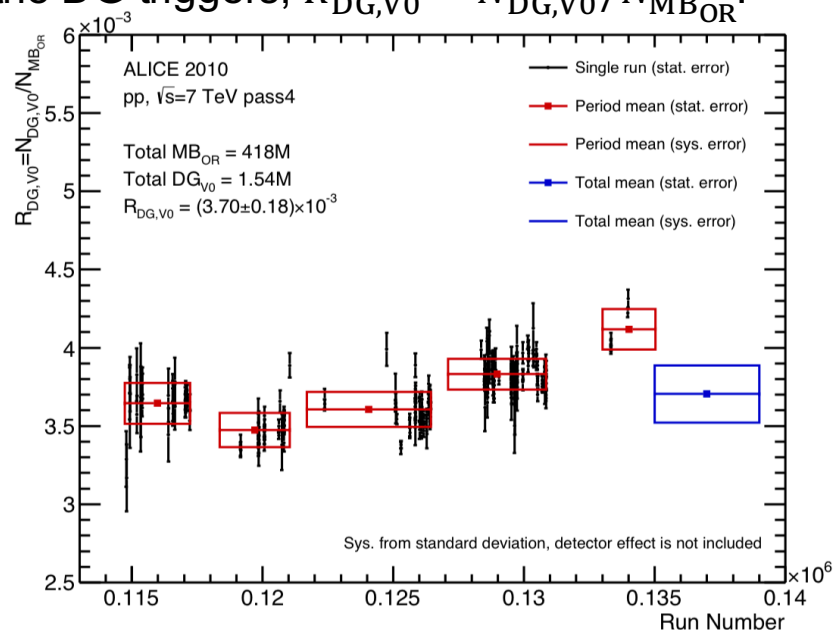
Dataset

- LHC10b, c, d, e, f pass4 (all available data in p-p collisions at $\sqrt{s} = 7$ TeV)
- Minimum bias trigger in ALICE
 - MB_{OR} : V0C || V0A || SPD, where || is logical OR (Total # ~ 418M)
 - Note that DG is defined only in MB_{OR}
- Double gap using V0+SPD: !V0C & !V0A & SPD (Total # ~ 1.5M)

Run quality analysis to evaluate the ratio of the DG triggers, $R_{DG,V0} = N_{DG,V0}/N_{MB_{OR}}$.



Distribution of $R_{DG,V0}$



$R_{DG,V0}$ as a function of run numbers and it is stable

Data analysis: event and track selection

- Event selection procedures to reject pile-up and beam-gas events.

Procedures	# of events (%)
MB_{OR} offline	418M (100%)
Vertex cut, $ z_{vtx} < 10$ cm	345M (83%)
Pile-up rejection using secondary SPD vertex	336M (80%)
SPD $N_{clusters}$ vs. $N_{tracklets}$	336M (80%)
Double-gap	0.98M (0.2%)



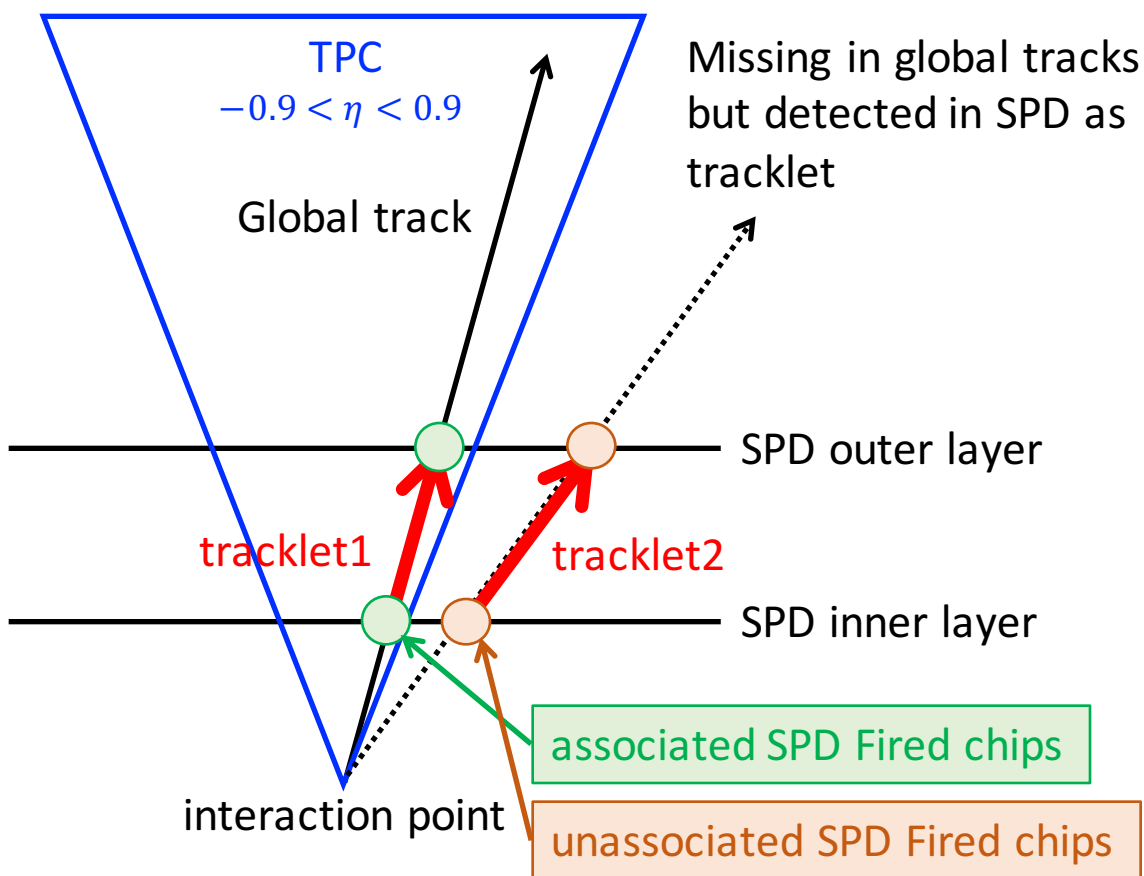
- Trackcuts: Standard trackcuts + More trackcuts to select only N-track events

Standard trackcuts	Value
# of clusters in TPC (LHC10d,e,f)	> 70
# of crossed rows in TPC (LHC10b,c)	> 70
Ratio crossed rows over findable clusters in TPC (LHC10b,c)	> 0.8
Chi2 per cluster in TPC	< 4
Accept kink daughter	false
Require TPC, ITS refit	true
Cluster requirement in ITS	kSPD,kAny
DCA to vertex X,Y p_T dependency	$0.0182+0.0350/p_T^{1.01}$
Chi2 of TPC constrained global	< 36
DCA to vertex Z	< 2 cm
DCA to vertex 2D	false
Require sigma to vertex	false

More trackcuts	Value
# of shared cluster in TPC	< 3
Distance between z_{trk} and z_{vtx}	< 6 cm
Eta of track	-0.9 to 0.9
No unassociated tracklet for selected track	
No unassociated SPD fired chip for selected track	
PID: Bayesian probabilities are used P_p or $P_K > 95\%$ are rejected $P_\pi < 60\%$ are rejected	

Data analysis: event and track selection

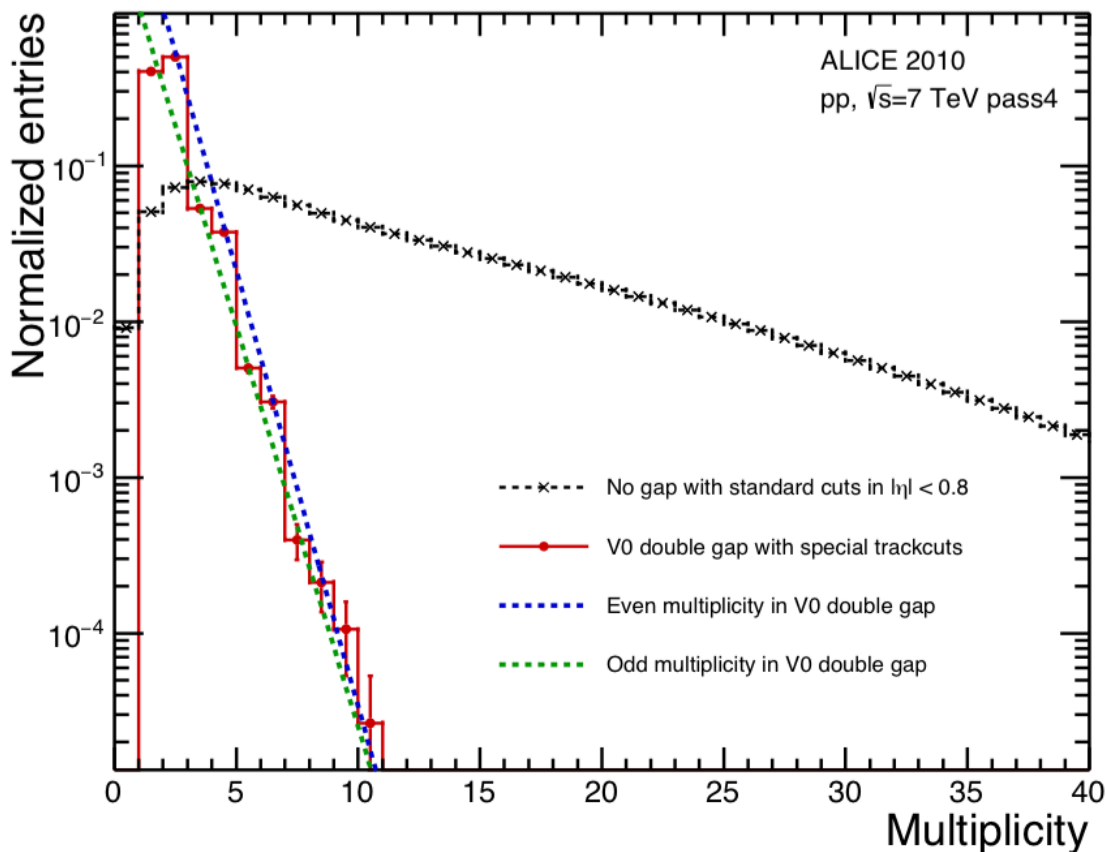
- Global track in ALICE: $-0.9 < \eta < 0.9$
- Another definition of track in ALICE: **tracklet**
 - A line between one point in SPD inner layer and another point in SPD outer layer
 - Eta of tracklet : $-2 < \eta < 2$



1. $N_{\text{tracklets}} > N_{\text{tracks}}$: **rejected**
This means we required **no activities outside of TPC** regions to enhance gap definitions. Before, no signals in
 $2.8 < \eta < 5.1$
 $-3.7 < \eta < -1.7$
Now, we can have **more gaps in**
 $-2.0 < \eta < -0.9$
 $+0.9 < \eta < +2.0$
additionally.

2. **unassociated SPD fired chips : rejected**
reduce noisy SPD chips ensuring signals are from tracks

Data analysis: raw multiplicity distribution

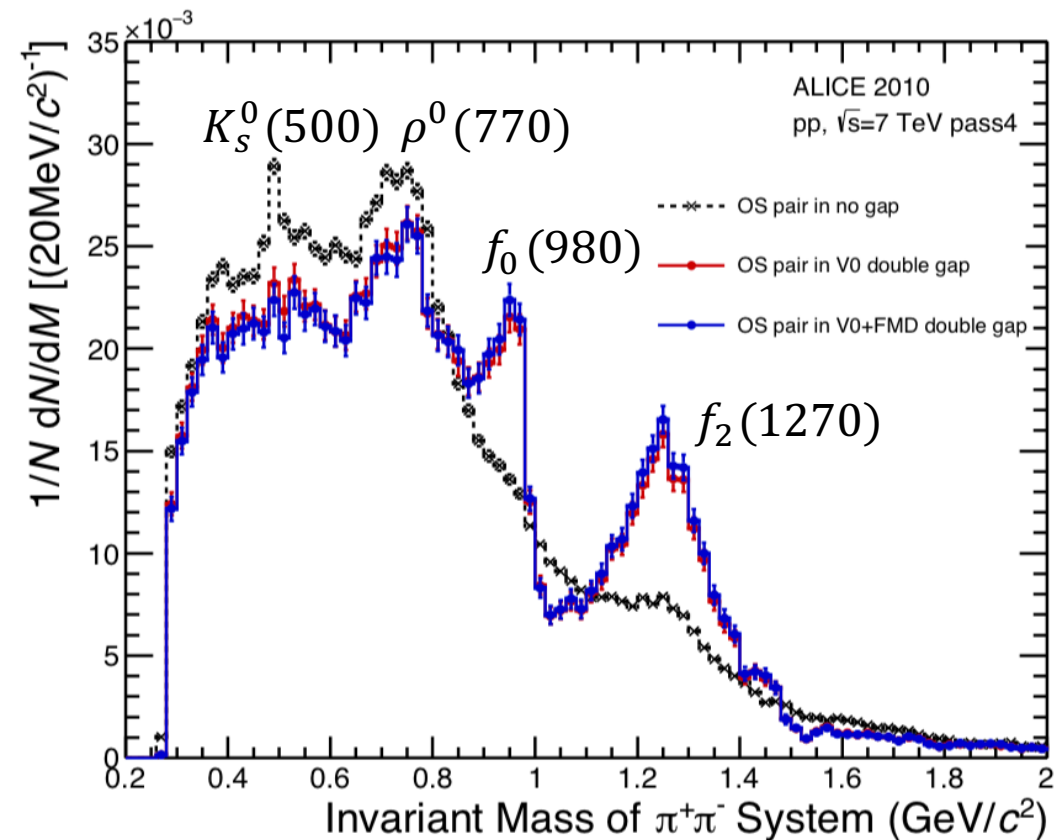


X-axis : Multiplicity
Y-axis : Normalized entries

Black = No gap
Red = V0 double gap
Blue = Even number in V0 DG
Green = Odd number in V0 DG

- No gap (NG) event can be used as comparison because this refers non-diffractive events.
 - NG: !DG & !Single gap A-side & !Single gap C-side
- DG shows clear difference with NG events and has very small multiplicities for all events.
- More of even-multiplicity events than odd-multiplicity events (DPE produce only even multiplicities) → DG triggers pick up DPE process as well as background.

Data analysis: raw invariant mass distribution of $\pi^+\pi^-$



X-axis : Invariant mass of $\pi^+\pi^-$
Y-axis : Normalized entries

Black = No gap

Red = V0 double gap (~40K)

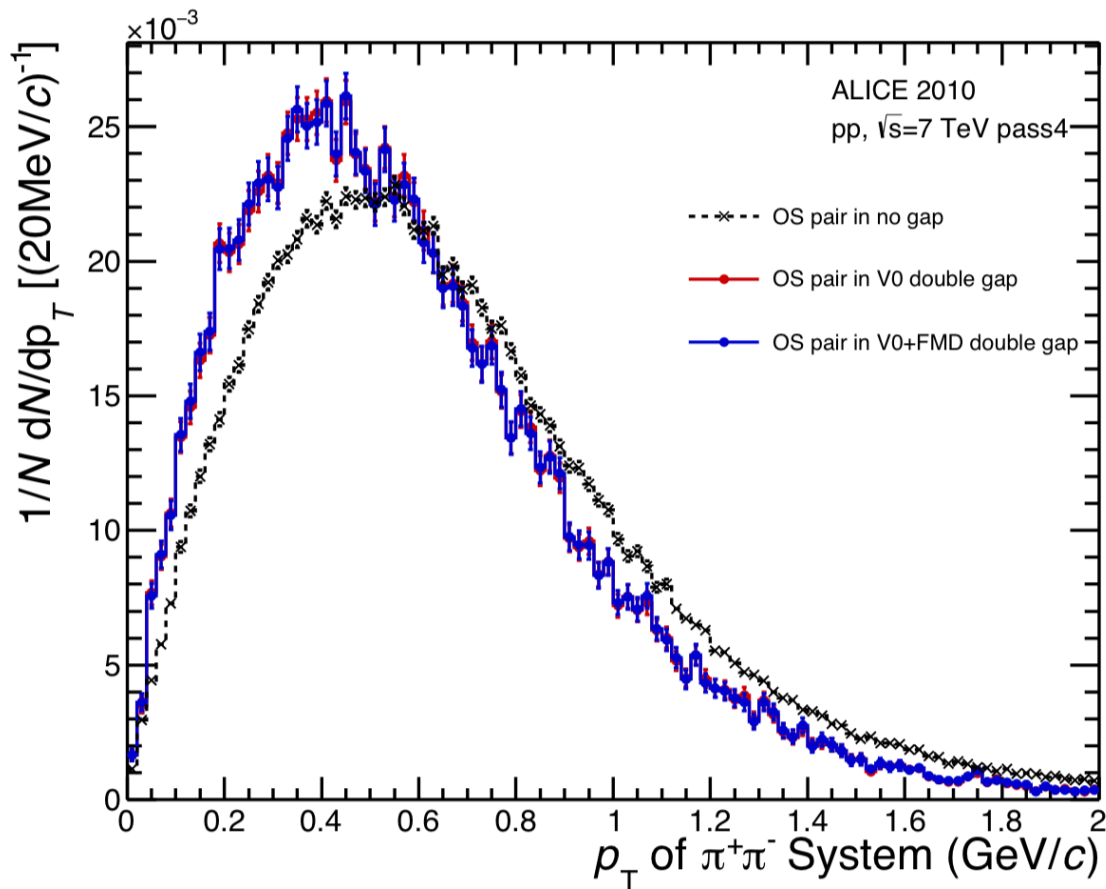
Blue = V0+FMD double gap (~35K)

$\rho^0(770)$ appeared in DG which is not allowed in DPE process

1. photon-Pomeron interaction
2. Feed-down from 3- or 4- body decay
3. Pure background

- Like-sign contamination is very low $\sim 3\%$ of total two-pion events.
- Again, NG is used as comparison and it has $K_S^0(500)$ and $\rho^0(770)(J^{PC} = 1^{--})$.
- There are clear signals of $f_0(980)$ and $f_2(1270)$ in both V0 and V0+FMD gaps and no difference between these two gaps. \rightarrow V0 gap can be used for further analysis due to large statistics.
- DG contains DPE process with $\pi^+\pi^-$ final states as well as background.

Data analysis: p_T distribution of $\pi^+\pi^-$



X-axis : p_T of $\pi^+\pi^-$
Y-axis : Normalized entries

Black = No gap

Red = V0 double gap (~40K)

Blue = V0+FMD double gap (~35K)

- As DPE is related to small momentum transfer in transverse plane, p_T of produced system should be very small.
- Mean p_T of DG is smaller than NG and there is no difference between V0 and V0+FMD gaps.
 - DG contains DPE process with $\pi^+\pi^-$ final states as well as background.

Data analysis: estimation of background

- Even though DG selects the DPE process, there is a chance that **other processes are triggered with DG as background**.

- $N_{DG,2\pi} = N_{CD,2\pi} * \epsilon_{CD,2\pi} + N_{NCD,2\pi} * \epsilon_{NCD,2\pi}$, where NCD means non central diffraction.
 - $NCD = ND+SD+DD+\dots$

- To estimate amounts and shape of background, we used Pythia6 because **Pythia6 doesn't have CD process at all**.

- Same track and event selections as data are applied to Pythia6.

- The goal is to get a purity of data samples and distinguish signal and background in the data.

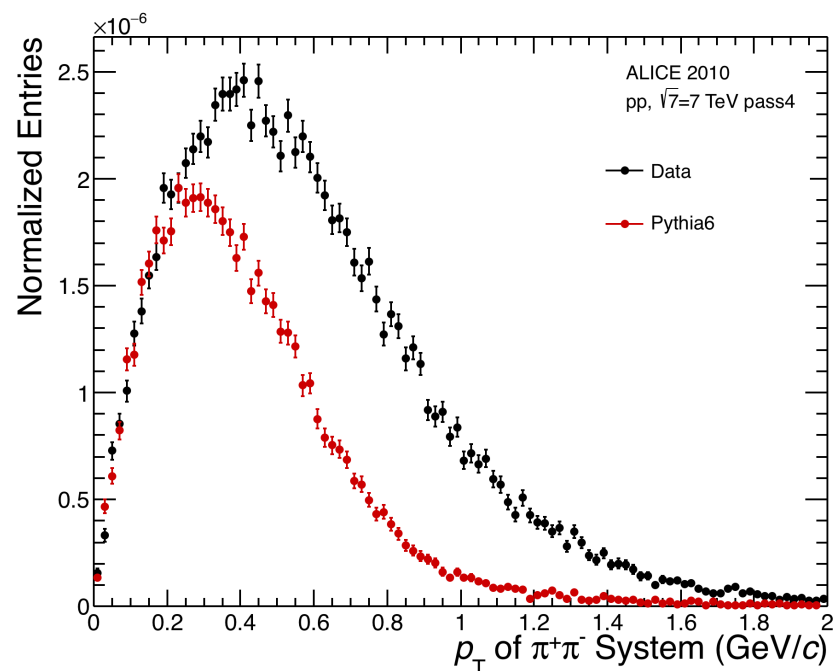
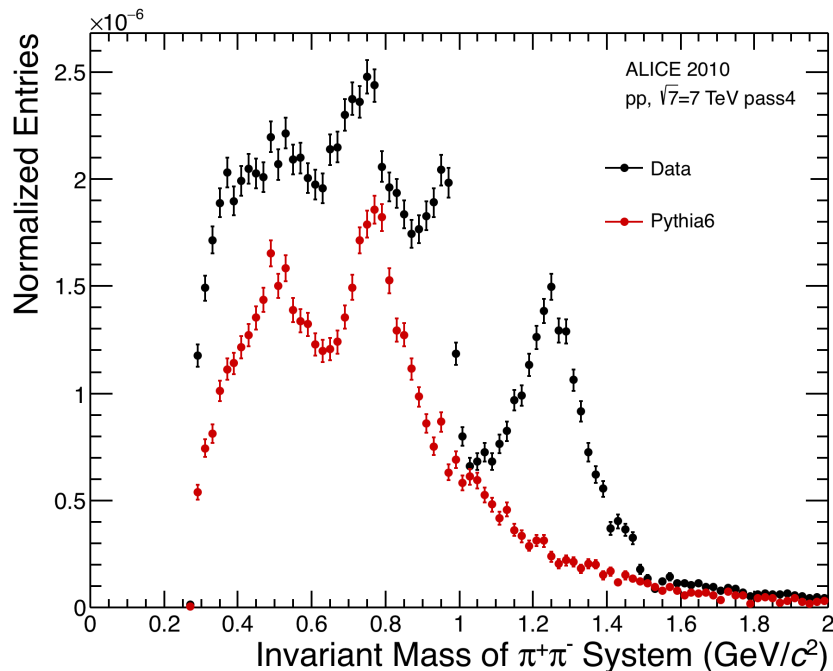
- Purity of data sample

- $$P = \frac{N_{CD,2\pi} * \epsilon_{CD,2\pi}}{N_{DG,2\pi}} = \frac{N_{DG,2\pi} - N_{NCD,2\pi} * \epsilon_{NCD,2\pi}}{N_{DG,2\pi}} = \frac{\text{Data} - \text{Pythia6}}{\text{Data}}$$

- Analysis of backgrounds from other sources is ongoing using Pythia8, PHOJET and STARLIGHT

1. Feed down from high mass central diffraction (Pythia8, PHOJET)
2. $\rho^0(770)$ from photon-Pomeron interaction (STARLIGHT)

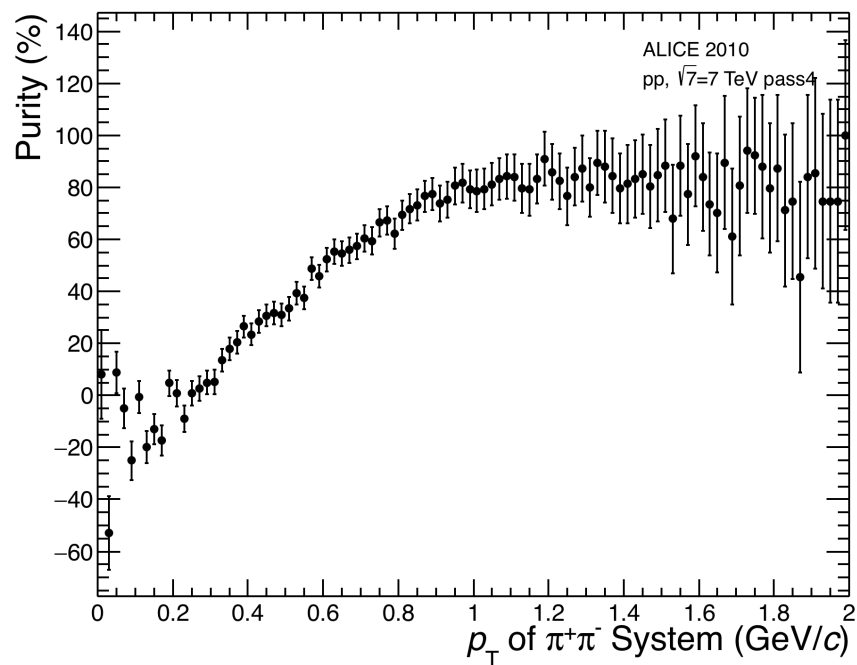
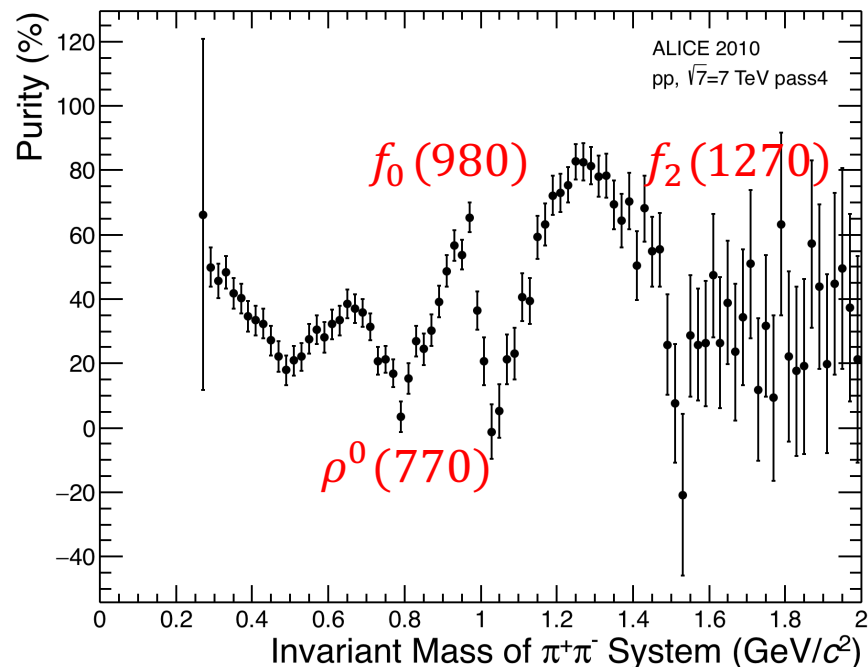
Data analysis: estimation of background



Invariant mass and p_T of $\pi^+\pi^-$ with data (black) and MC (Red). All histograms are normalized with each N_{MBOR}

- According to Pythia6, there are large continuum non-resonant background below 1 GeV, and $\rho^0(770)$ from NCD is observed with the DG trigger.
 - Most of $\rho^0(770)$ in the data can be from NCD, not photon-Pomeron interaction.
 - This can explain why we observe $\rho^0(770)(J^{PC} = 1^{--})$ in DPE.
- We may use the cut on p_T in the data to distinguish signal and background, however, it is impossible to have a such cut.
 - It's hard to decompose signal and background in the data

Data analysis: estimation of background



Purity as a function of an invariant mass (left) and p_T (right) of $\pi^+\pi^-$ system

- Purity of the data sample is about 60~80% at $f_0(980)$ and $f_2(1270)$, and almost 0% at $\rho^0(770)$.
 - Mean value of purity is around 50%.
 - If it is possible to get purities including backgrounds from other sources, cross section of $\pi^+\pi^-$ system can be obtained and compared with CMS.
- The higher the p_T is, the larger the purity is.
 - There is large amount of contamination of data sample in low p_T regions.
 - Note that this is model dependent.

Partial wave analysis: basic formalism

- In principle, invariant mass spectrum of $\pi^+\pi^-$ system is **mixed with many meson states**.
 - **Partial wave analysis (PWA) allows to decompose particles** into different quantum number states.
- Basic formalism †
 - PWA is tool to find out **‘number of events of a given mass bin’ having specific quantum number**
 - Partial amplitudes: J_M^ϵ , where J is spin, ϵ is reflectivity, and M is magnetic quantum number e.g. $S_0^-, D_0^-, D_1^-, D_1^+, \dots$ (complex number)
 - **Number of particles in one mass bin = $|J_M^\epsilon|^2$**
 - Likelihood function for finding ‘ n ’ events of a given bin with a finite acceptance $\eta(\Omega)$:
 - $$L = \left[\frac{\bar{n}^n}{n!} e^{-\bar{n}} \right] \prod_i^n \left[\frac{I(\Omega_i)}{\int I(\Omega)\eta(\Omega)d\Omega} \right]$$
 - By applying extended log-likelihood method, equation is simplified to minimizing function F .
 - $F = -\sum_i \ln I(\Omega_i) + \sum_{LM} t_{LM} \epsilon_{LM}$, where i is event number and (L,M) are quantum numbers.
 - **Angular distribution from the data:** $I(\Omega_i) = \sum_{LM} t_{LM} \text{Re} Y_L^M(\Omega_i)$
, where Y_L^M is a spherical harmonic function and Ω_i is solid angle of π^+ in GJ frame.
 - **Efficiency term from MC:** $\epsilon_{LM} = \frac{4\pi}{N_{gen}} \sum_j \text{Re} Y_L^M(\Omega_j)$, for acceptance correction
 - t_{LM} : **fit parameters**, but can be exchanged to partial wave components, J_M^ϵ .
 - Minimizing F using `Minuit (MIGRAD)` in `ROOT`

† Suh-Urk Chung, “Techniques of Amplitude Analysis for Two-pseudoscalar Systems”, Physical Review D56, 7299, 1997

Partial wave analysis: correlation between fit parameters

- t_{LM} have correlations with partial amplitudes and we can obtain J_M^ϵ doing PWA.

$$\sqrt{4\pi}t_{00} = |S_0^-|^2 + |P_0^-|^2 + |P_1^-|^2 + |P_1^+|^2 + |D_0^-|^2 + |D_1^-|^2 + |D_1^+|^2 + |D_2^-|^2 + |D_2^+|^2$$

$$\sqrt{4\pi}t_{10} = \frac{2}{5}(\sqrt{15}D_1^+P_1^+ + \sqrt{15}D_1^-P_1^- + 5P_0^-S_0^- + 2\sqrt{5}P_0^-D_0^-)$$

$$\sqrt{4\pi}t_{11} = \frac{\sqrt{2}}{5}(\sqrt{15}D_2^+P_1^+ + \sqrt{15}D_2^-P_1^- + \sqrt{15}D_1^-P_0^- + 5P_1^-S_0^-)$$

$$\sqrt{4\pi}t_{20} = \frac{1}{35}(\sqrt{5}(10|D_0^-|^2 + 5|D_1^-|^2 + 5|D_1^+|^2 - 10|D_2^-|^2 - 10|D_2^+|^2 + 14|P_0^-|^2 - 7|P_1^+|^2 - 7|P_1^-|^2) + 70D_0^-S_0^-)$$

$$\sqrt{4\pi}t_{21} = \frac{\sqrt{2}}{35}(5\sqrt{15}D_2^+D_1^+ + 35S_0^-D_1^- + 5D_1^-(\sqrt{15}D_2^- + 7D_0^-) + 7\sqrt{15}P_0^-P_1^-)$$

$$\sqrt{4\pi}t_{22} = \frac{1}{35\sqrt{2}}(70D_2^-S_0^- + \sqrt{15}(5|D_1^-|^2 - 5|D_1^+|^2 + 7|P_1^-|^2 - 7|P_1^+|^2) - 20D_0^-D_2^-)$$

$$\sqrt{4\pi}t_{30} = \frac{6}{\sqrt{35}}(\sqrt{3}D_0^-P_0^- - D_1^+P_0^+ - D_1^-P_1^-)$$

$$\sqrt{4\pi}t_{31} = \sqrt{\frac{3}{35}}(4D_1^-P_0^- + 6\sqrt{3}D_0^-P_1^- - D_2^+P_1^+ - D_2^-P_1^-)$$

$$\sqrt{4\pi}t_{32} = \sqrt{\frac{6}{7}}(D_1^-P_1^- - D_1^+P_1^+ + P_0^-D_2^-)$$

$$\sqrt{4\pi}t_{33} = \frac{3}{\sqrt{7}}(D_2^-P_1^- - D_2^+P_1^+)$$

$$\sqrt{4\pi}t_{40} = \frac{1}{7}(6|D_0^-|^2 - 4|D_1^-|^2 - 4|D_1^+|^2 + |D_2^-|^2 + |D_2^+|^2)$$

$$\sqrt{4\pi}t_{41} = -\frac{\sqrt{5}}{7}(D_1^+D_2^+ + D_1^-D_2^- - 2\sqrt{3}D_0^-D_1^-)$$

$$\sqrt{4\pi}t_{42} = \frac{\sqrt{10}}{7}(|D_1^-|^2 - |D_1^+|^2 + \sqrt{3}D_0^-D_2^-)$$

$$\sqrt{4\pi}t_{43} = \sqrt{\frac{5}{7}}(D_1^-D_2^- - D_1^+D_2^+)$$

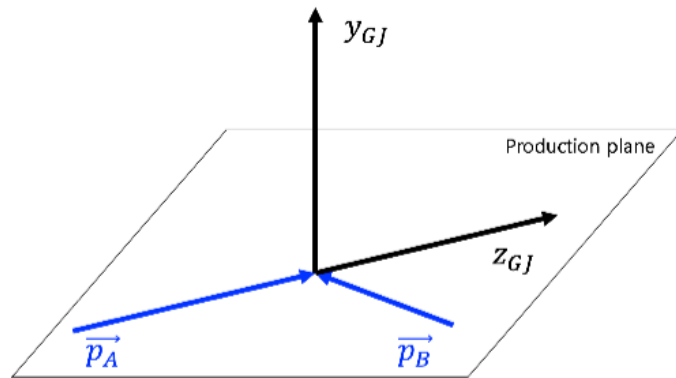
$$\sqrt{4\pi}t_{44} = \sqrt{\frac{5}{14}}(|D_2^-|^2 - |D_2^+|^2)$$

These terms have deep correlation with $M = 2$ waves.

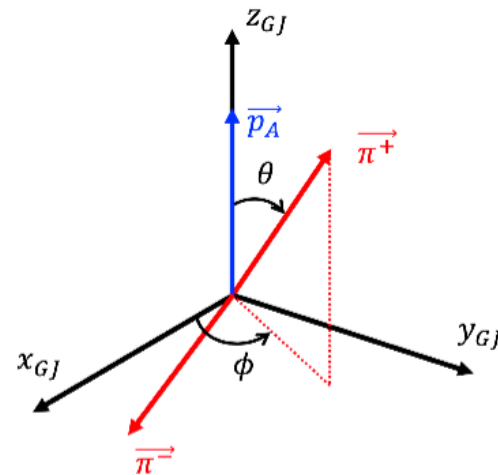
Our analysis results show these are compatible to zero, therefore, we can ignore $M = 2$ waves.

Partial wave analysis: GJ'-frame

- Gottfried-Jackson frame is used as the coordinate system of PWA.
 - Pomeron mechanism
 - z-axis: \vec{p}_z of incoming Pomeron in the $\pi^+\pi^-$ rest frame
 - y-axis: $\vec{p}_z \times \vec{p}_x$ in LAB frame
 - x-axis: $\vec{p}_y \times \vec{p}_z$ in the $\pi^+\pi^-$ rest frame
 - As we can't detect outgoing protons, we don't know momentum of Pomerons.
 - **Proton mechanism**, ignoring Pomeron in this case (GJ'-frame)
 - z-axis: \vec{p}_z of incoming proton in the $\pi^+\pi^-$ rest frame

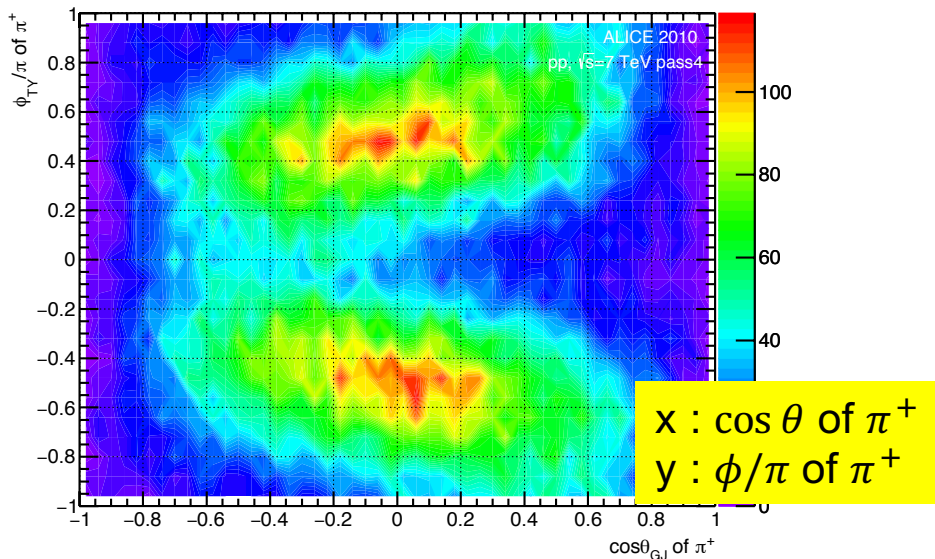
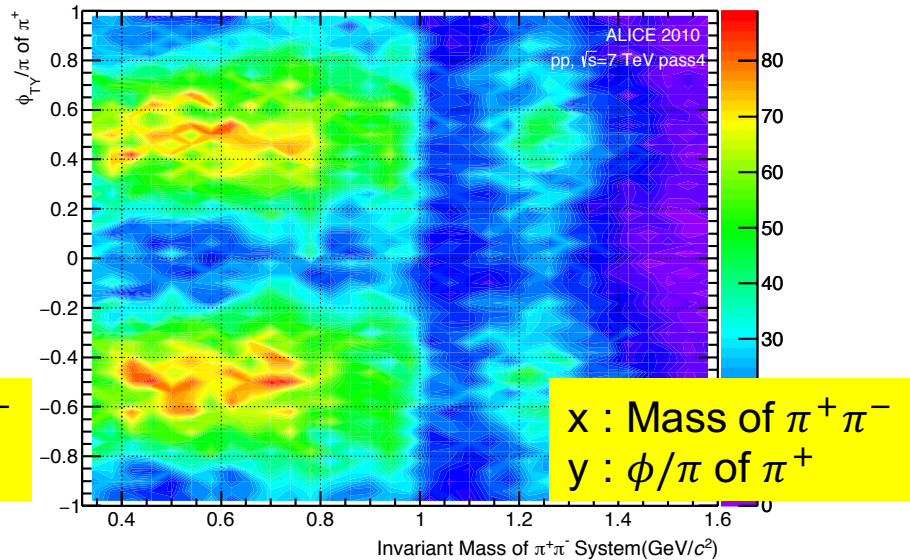
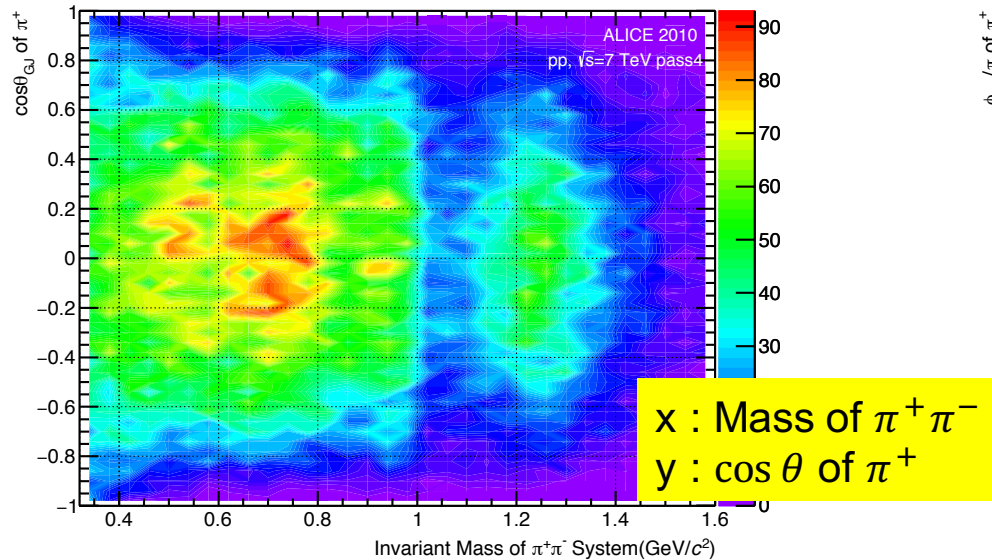


GJ'-frame with production plane



GJ'-frame with definition of solid angle

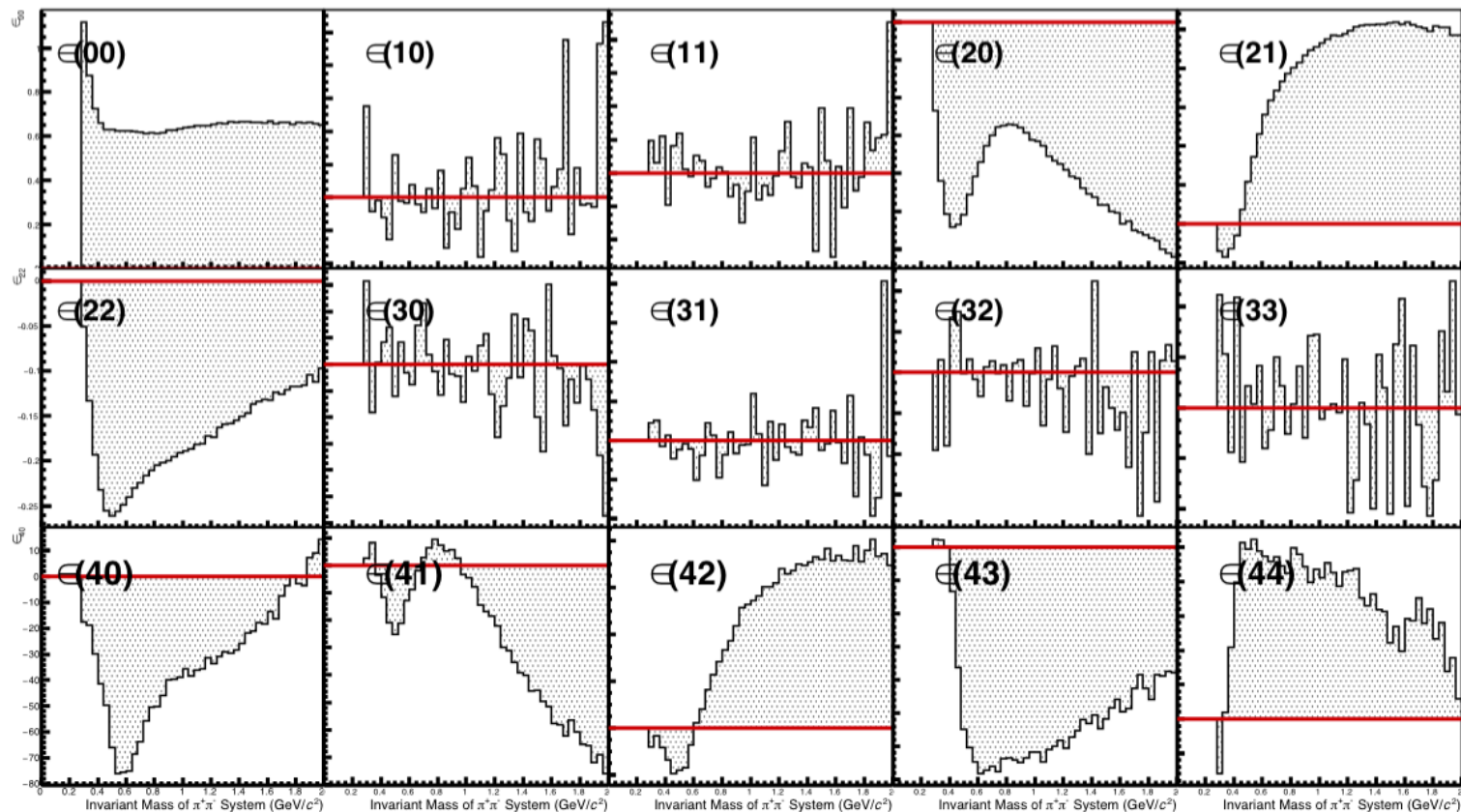
Partial wave analysis: $I(\Omega_i)$ in minimizing function F



Raw angular distributions in the data. These are decomposed to different partial amplitudes according to spherical harmonics with acceptance correction using PWA.

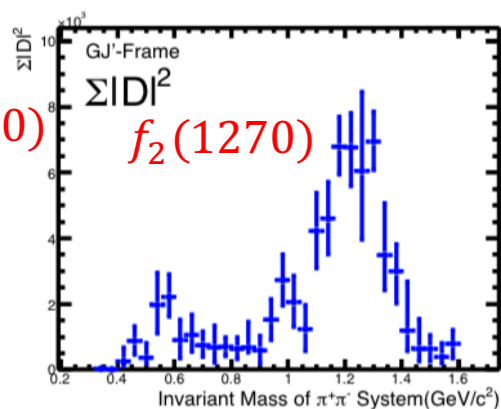
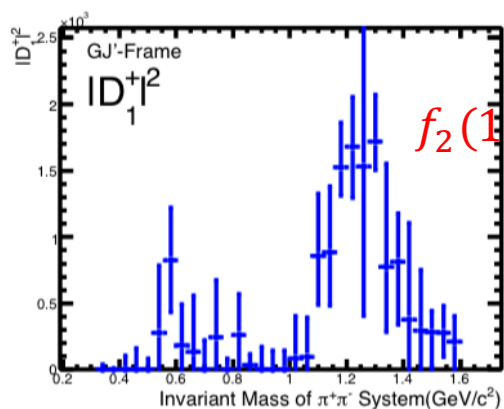
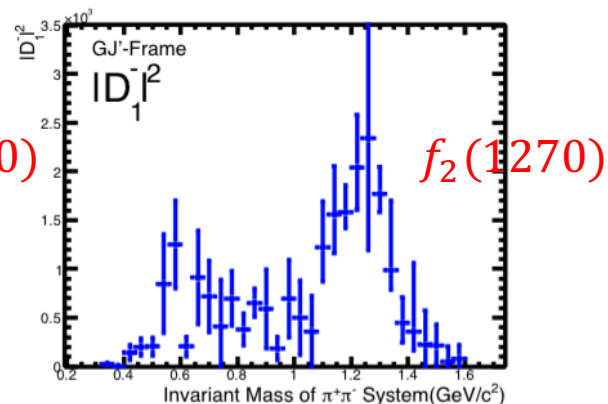
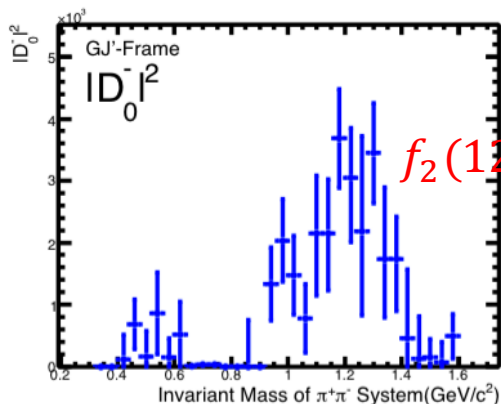
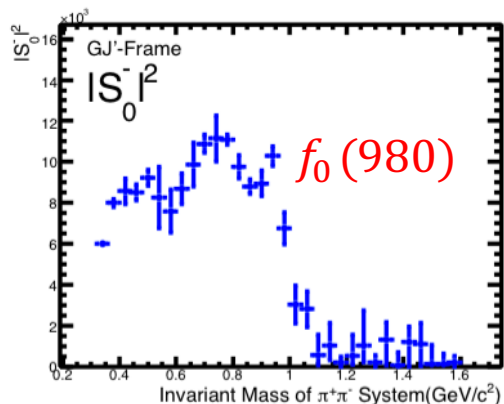
Partial wave analysis: ϵ_{LM} in minimizing function F

- **MC set:** special generator is prepared for partial wave analysis
 - Generator: DRgen from COMPASS, $p + p \rightarrow p + X + p \rightarrow p + \pi^+ \pi^- + p$
 - system X is produced from double-Pomeron exchange and decay to only $\pi^+ \pi^-$
 - Generated system has $|y_{X,Gen.}| < 2$, however, $|y_{X,Gen.}| < 1$ is applied to impose proper condition of CEP
- ϵ_{LM} roughly means acceptance X efficiency for (L,M) quantum numbers



Partial wave analysis: Results

- Used wave-set = $S_0^-, D_0^-, D_1^-, D_1^+$ (spin 0,2)
 - $M = 2$ wave assumed to be zero based on t_{LM} results.
 - P -waves are not included to reduce uncertainties (DPE produce only even spin waves).
 - The reflectivity – and + don't interfere each other.
 - Width of mass bin = $40 \text{ MeV}/c^2$ and $(0.32, 1.6) \text{ GeV}/c^2$ are used due to limited statistics



- The $f_0(980)$ and $f_2(1270)$ are appeared in spin 0 and 2 respectively as expected.
- Large continuum background is in S-wave at low mass regions, and there is almost no background in D-waves.
- $f_2(1270)$ is appeared in all D-waves.

Partial wave analysis: mass dependent fit

- Intensities are fitted with coherent background and one Breit-Wigner function

$$F_{\text{fit}} = \left| \underbrace{(a_0 \cdot e^{ia_1})}_{\text{phase factor}} \cdot \underbrace{bkg(m)}_{\text{background}} + \underbrace{a_2 BW(m)}_{\text{Breit-Wigner}} \right|^2$$

phase factor
between background
and Breit-Wigner

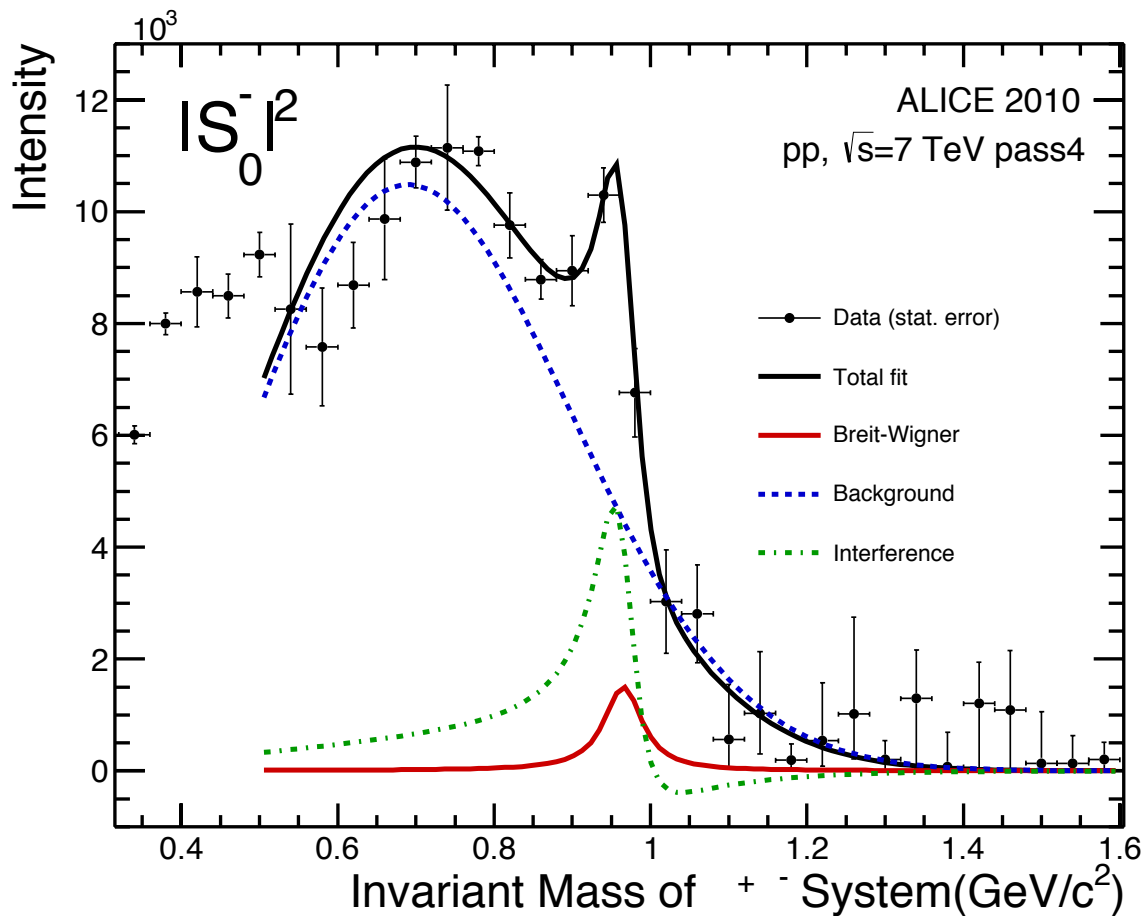
$$bkg(m) = \sqrt{\frac{q}{m^2}} e^{(-b_1 q - b_2 q^2)} \text{ for S-wave}$$
$$bkg(m) = 1 \text{ for D-wave}$$

$$BW(m) = \frac{m\Gamma(m)}{m^2 - m_0^2 - im_0\Gamma(m)}, \Gamma(m) = \Gamma_0 \frac{q B_l^2(q^2 R^2)}{m B_l^2(q_0^2 R^2)}$$

a_0, a_1, a_2, b_1, b_2 : fit parameters
 m_0, Γ_0 : mass and width of resonance (fit parameters)
 q : breakup momentum
 B_l : Barrier factor from [1]
 R : empirical interaction radius (~ 1 fm)

[1] F. Von Hippel and C. Quigg. Centrifugal-barrier effects in resonance partial decay widths, shapes, and production amplitudes. *Phys. Rev.*, D5:624–638, 1972.

Partial wave analysis: mass dependent fit of $|S_0^-|^2$

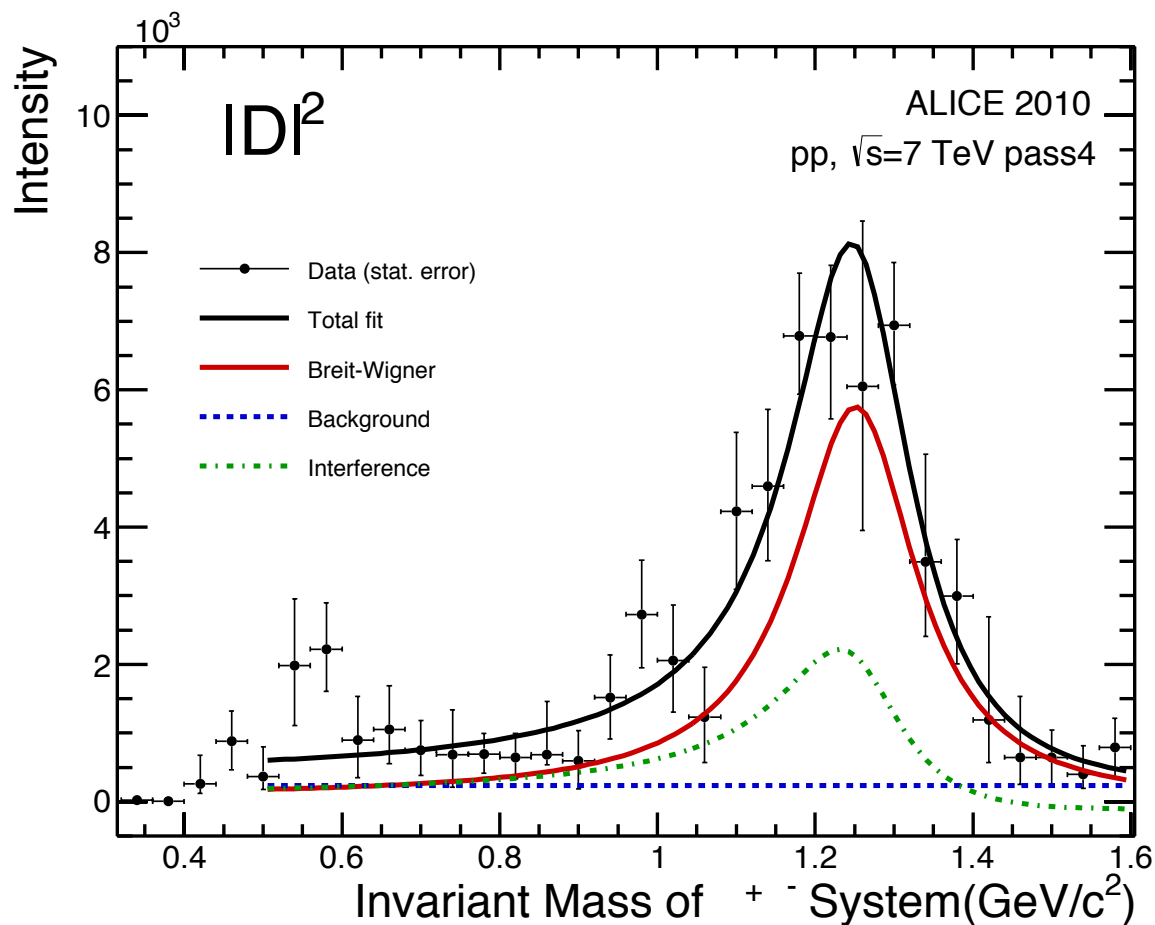


x : Invariant mass of $\pi^+ \pi^-$
 y : $|S_0^-|^2$

The data is well-fitted with large continuum **background** and **$f_0(980)$ signal**. Two functions are interfered each other at $f_0(980)$ regions.

$f_0(980)$	Mass (MeV/c^2)	Width (MeV/c^2)	χ^2/NDF
PDG	980 ± 10	40 to 100	
From fit	$965 \pm 21(\text{stat.})$	$56 \pm 42(\text{stat.})$	1.4

Partial wave analysis: mass dependent fit of $\Sigma|D|^2$



x : Invariant mass of $\pi^+ \pi^-$
 y : $\Sigma|D|^2$

The data is well-fitted with small constant background and $f_2(1270)$ signal. Two functions are interfered each other.

$f_2(1270)$	Mass (MeV/c^2)	Width (MeV/c^2)	χ^2/NDF
PDG	1275.1 ± 1.2	$185.1^{+2.9}_{-2.4}$	
From fit	$1257 \pm 16(\text{stat.})$	$187 \pm 37(\text{stat.})$	0.94

Conclusions

- Data analysis
 - Double-Pomeron exchange dominates central production at high energies and generates only even multiplicities.
 - ALICE could measure central productions by utilizing double gap topology.
 - $\pi^+\pi^-$ final states are studied with special trackcuts and $f_0(980)$ and $f_2(1270)$ are clearly seen.
 - Currently, purity is estimated as 50% and cross section will be obtained using various MC.
- Partial wave analysis has been done to get properties of produced particles.
 - Spin, mass, and width of produced particles are obtained.

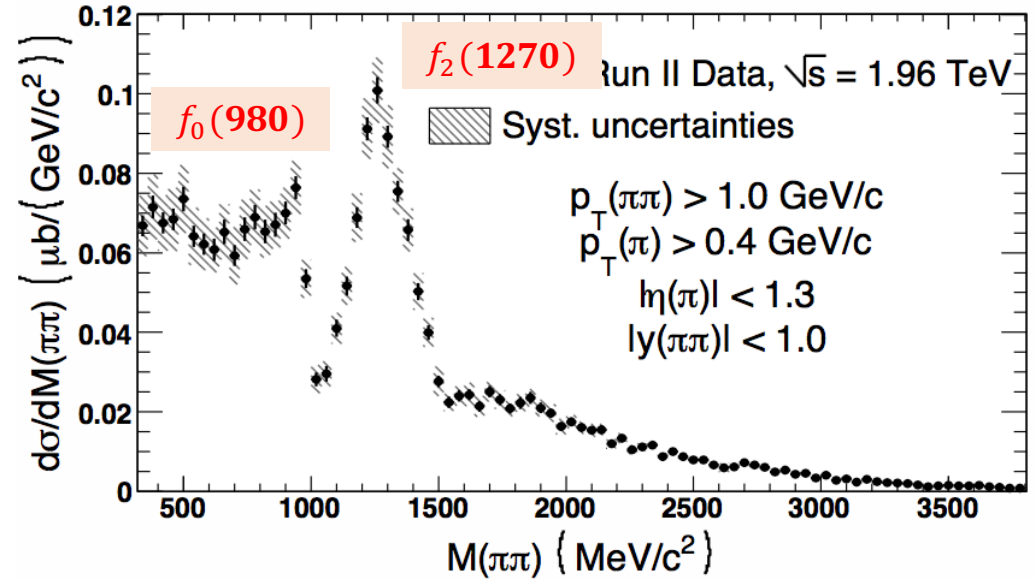
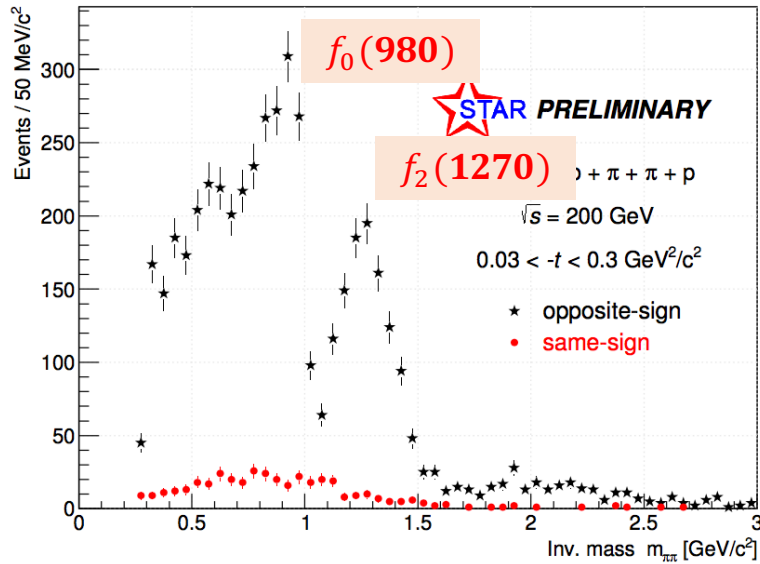
$f_0(980)$	Mass (MeV/c ²)	Width (MeV/c ²)	Spin
PDG	980 ± 10	40 to 100	0
ALICE	$965 \pm 21(stat.)$	$56 \pm 42(stat.)$	0

$f_2(1270)$	Mass (MeV/c ²)	Width (MeV/c ²)	Spin
PDG	1275.1 ± 1.2	$185.1^{+2.9}_{-2.4}$	2
ALICE	$1257 \pm 16(stat.)$	$187 \pm 37(stat.)$	2

- Systematic uncertainties and cross section of $f_0(980)$ and $f_2(1270)$ will be obtained.

$\pi^+\pi^-$ invariant mass distribution from other experiments

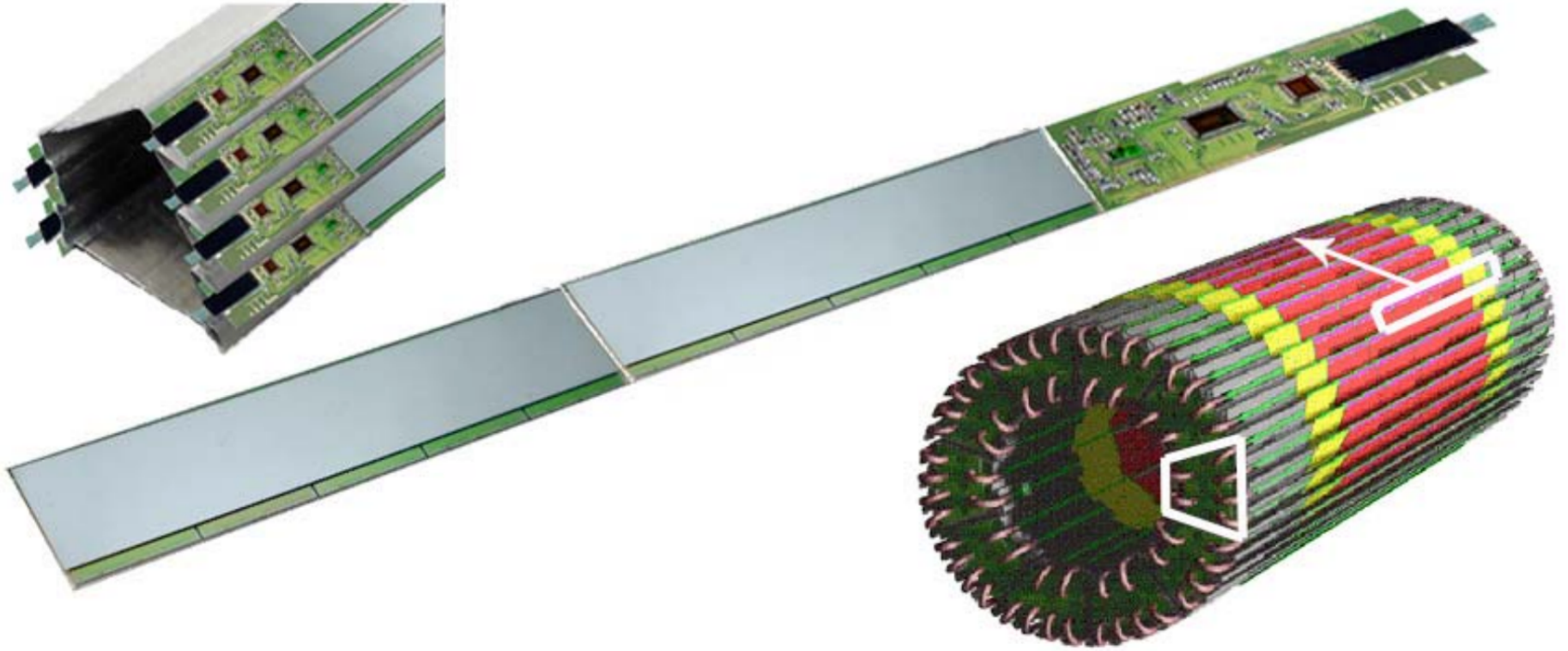
Invariant mass of $\pi\pi$, $p_T^{\text{miss}} < 0.1$ GeV/c, not acceptance-corrected, statistical errors only



STAR results, Acta Phys.Polon. B47 (2016) 53-58

CDF results, arXiv:1502.01391v3

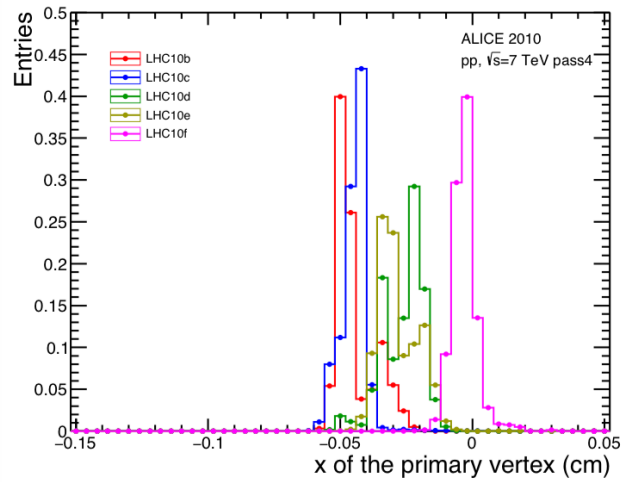
Silicon Pixel Detector (SPD)



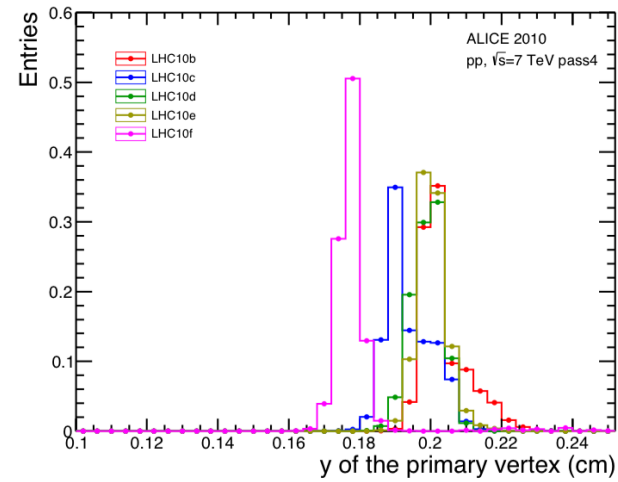
1200 chips
400 at inner and 800 at outer

THE ALICE SILICON PIXEL DETECTOR (SPD), A. KLUGE

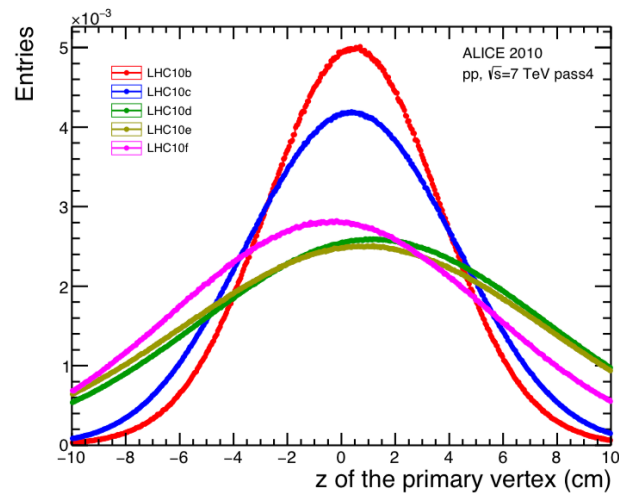
Vertex distributions



(a) x_{vtx} from the data

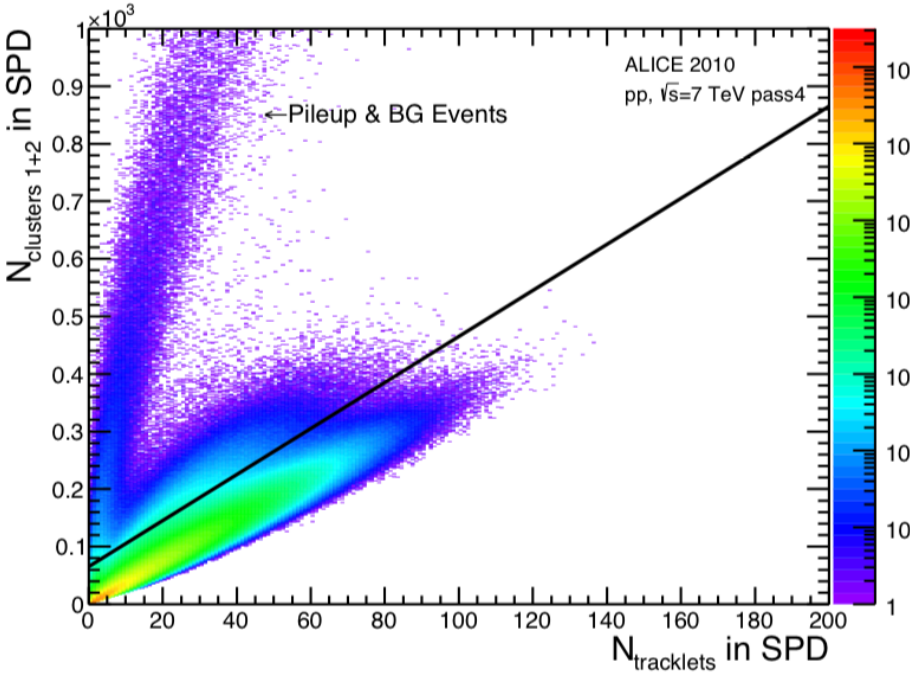


(b) y_{vtx} from the data

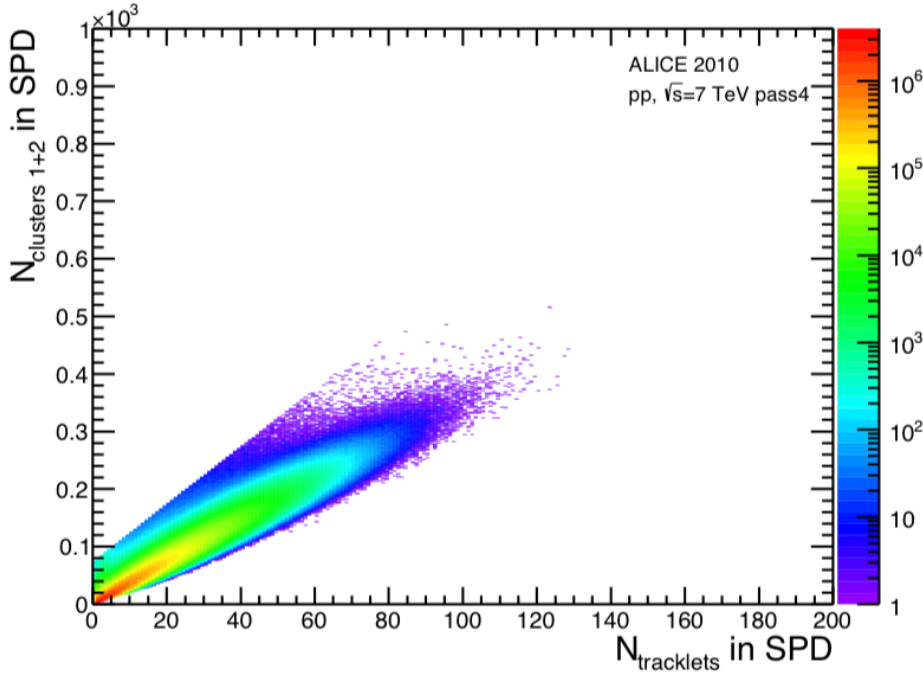


(c) z_{vtx} from the data

SPD clusters versus SPD tracklets cut

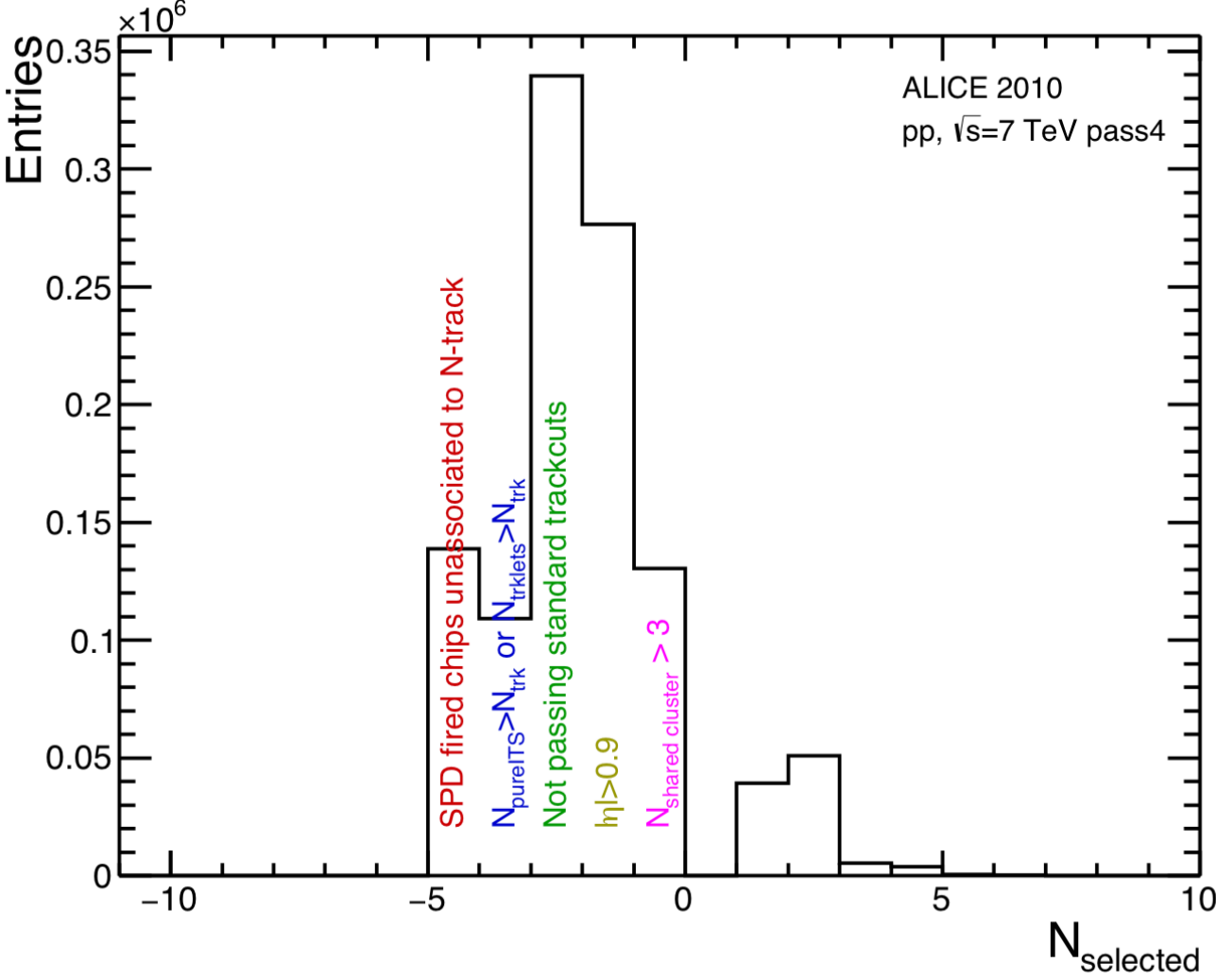


(a) Before cluster cut

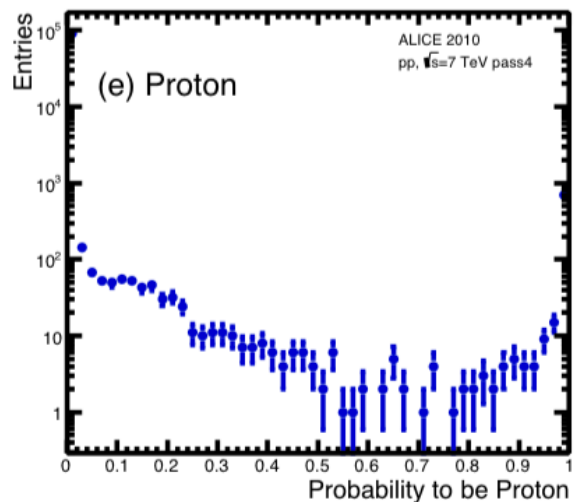
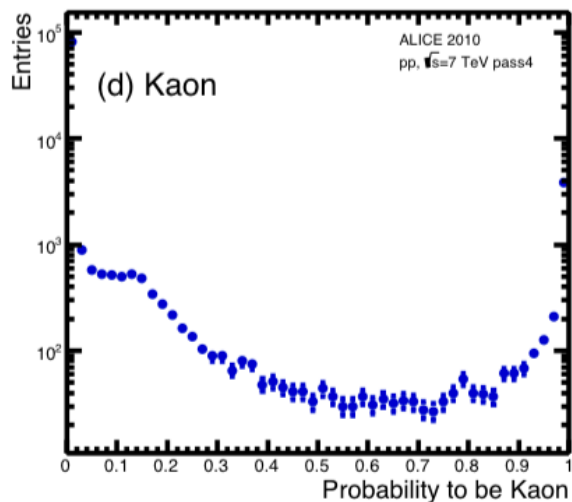
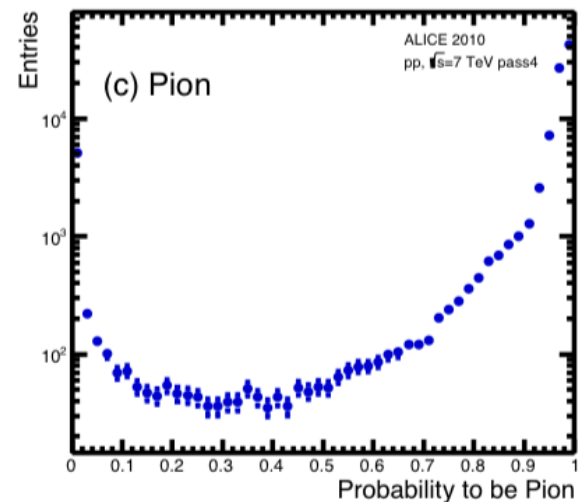
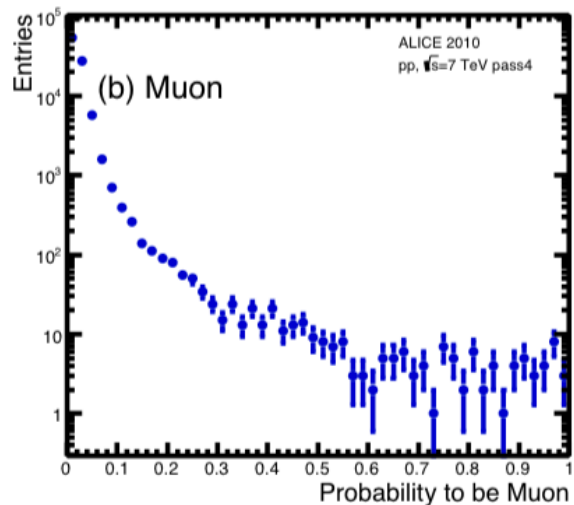
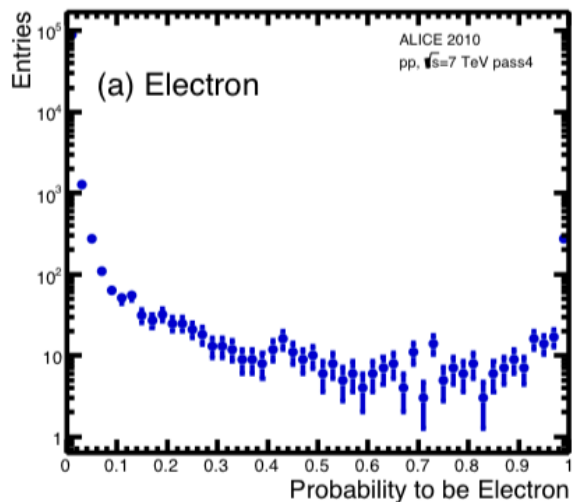


(b) After cluster cut

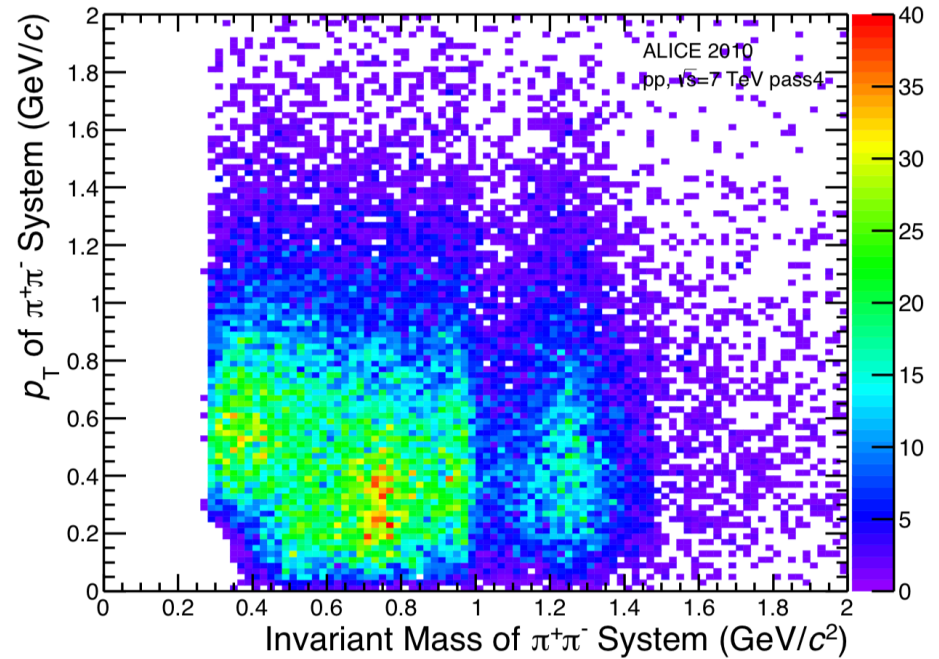
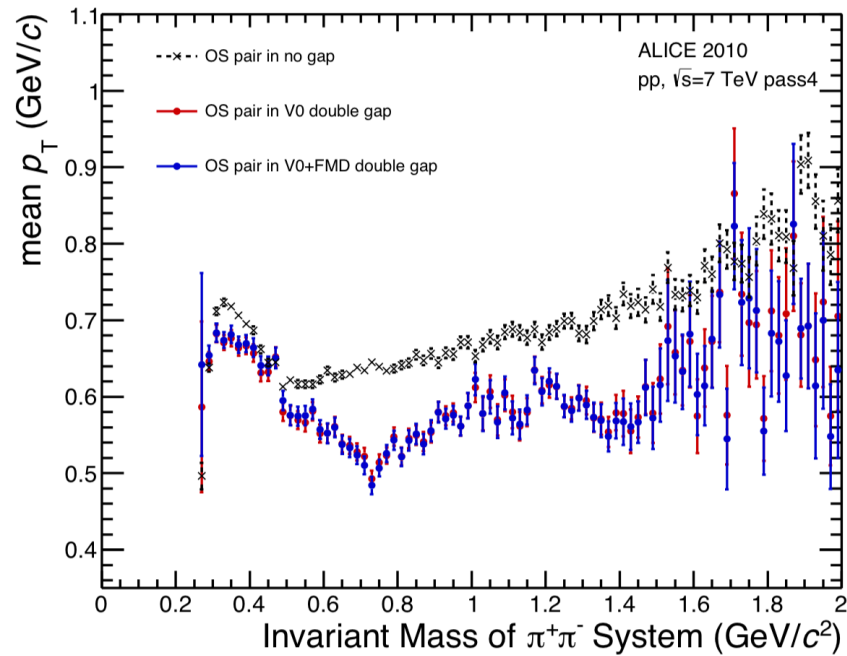
Rejected events from trackcuts



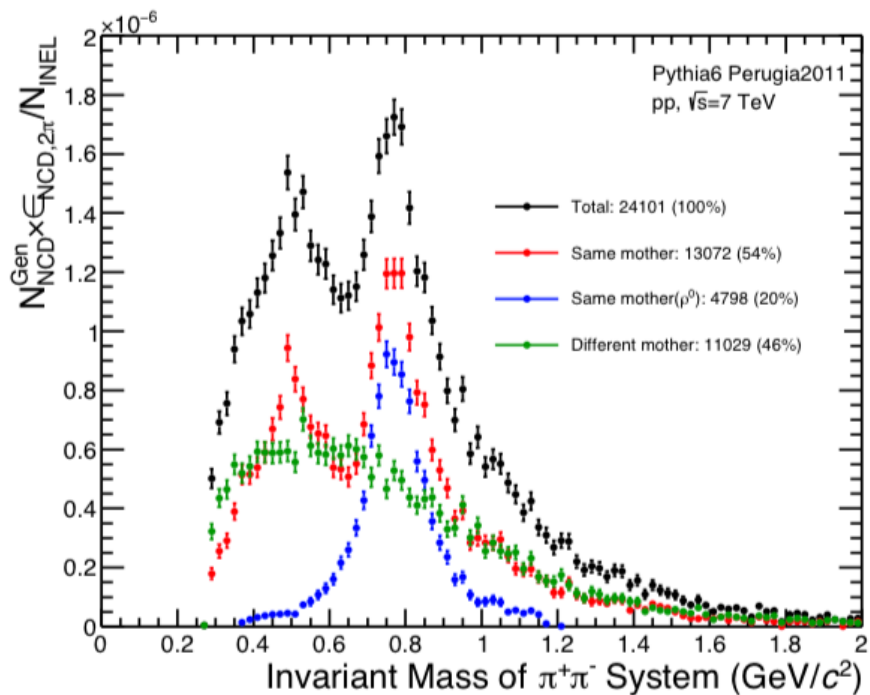
Bayesian probabilities



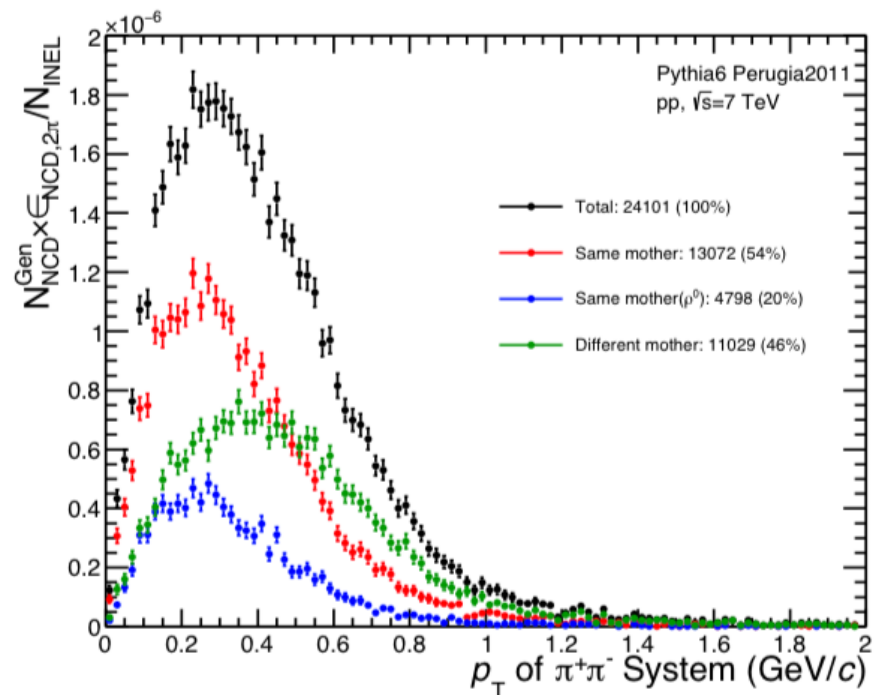
mean p_T versus mass, p_T versus mass



Estimation of background with mother particle



(a) Mass



(b) p_T

Differential cross section of DRgen (MC)

$$d\sigma_{p_1 p_2 \rightarrow p_1 X p_2} = e^{bt_1} (1-x_1)^{1-2\alpha_{\mathbb{P}}(t_1)} e^{bt_2} (1-x_2)^{1-2\alpha_{\mathbb{P}}(t_2)} \sigma_{\mathbb{P}\mathbb{P} \rightarrow X} dx_1 d^2q_1 dx_2 d^2q_2$$

$b : 8\text{GeV}^{-2}$

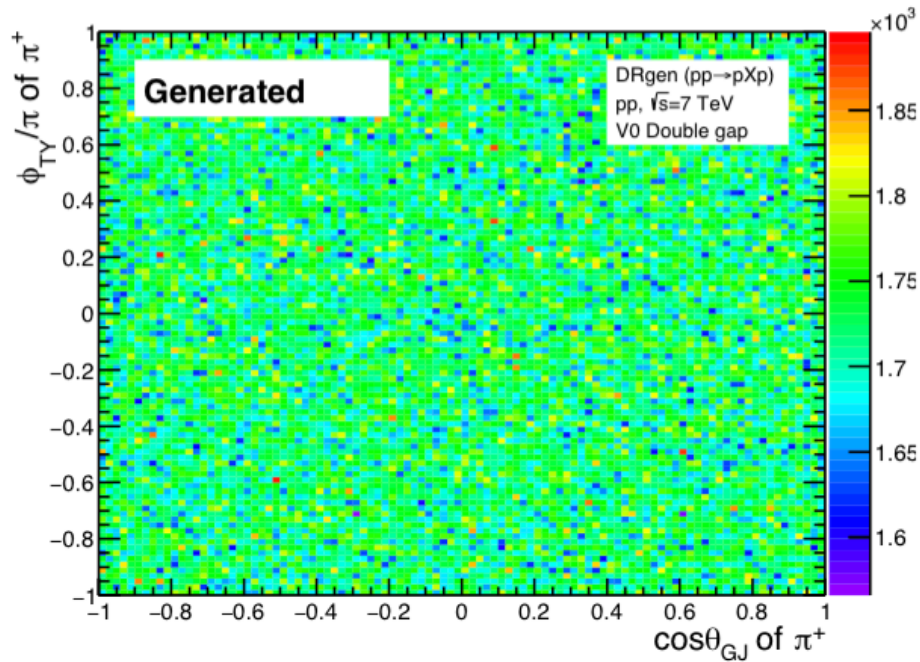
t_1, t_2 : Transfer momenta of Pomerons

x_1, x_2 : Feynmann variables of outgoing protons

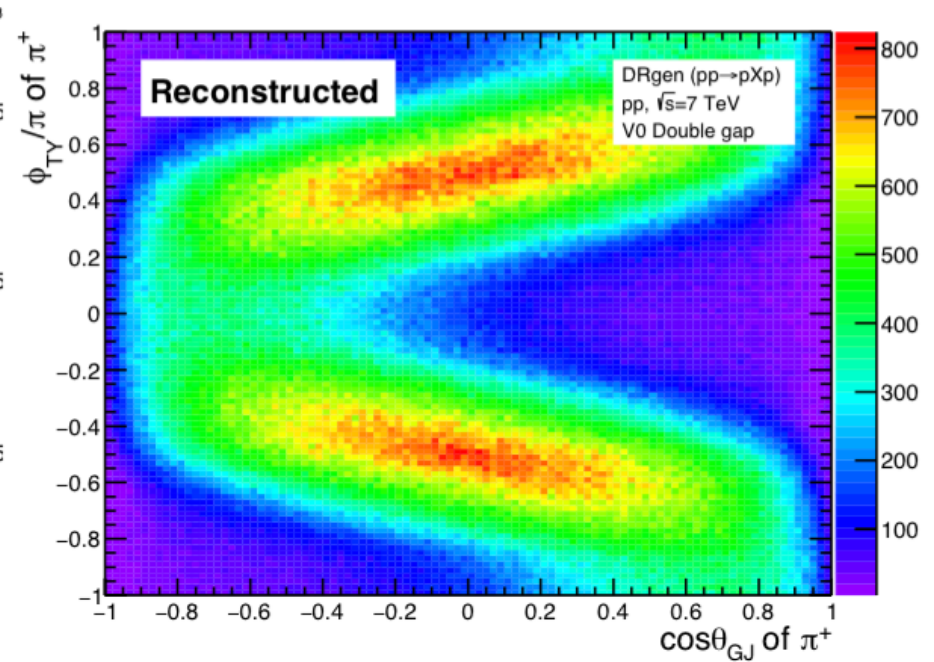
$\alpha_{\mathbb{P}}$: Pomeron trajectory, $\alpha_{\mathbb{P}} = 1.08 + 0.25t$

q_1, q_2 : Transverse momenta of outgoing protons

Angular distribution of MC

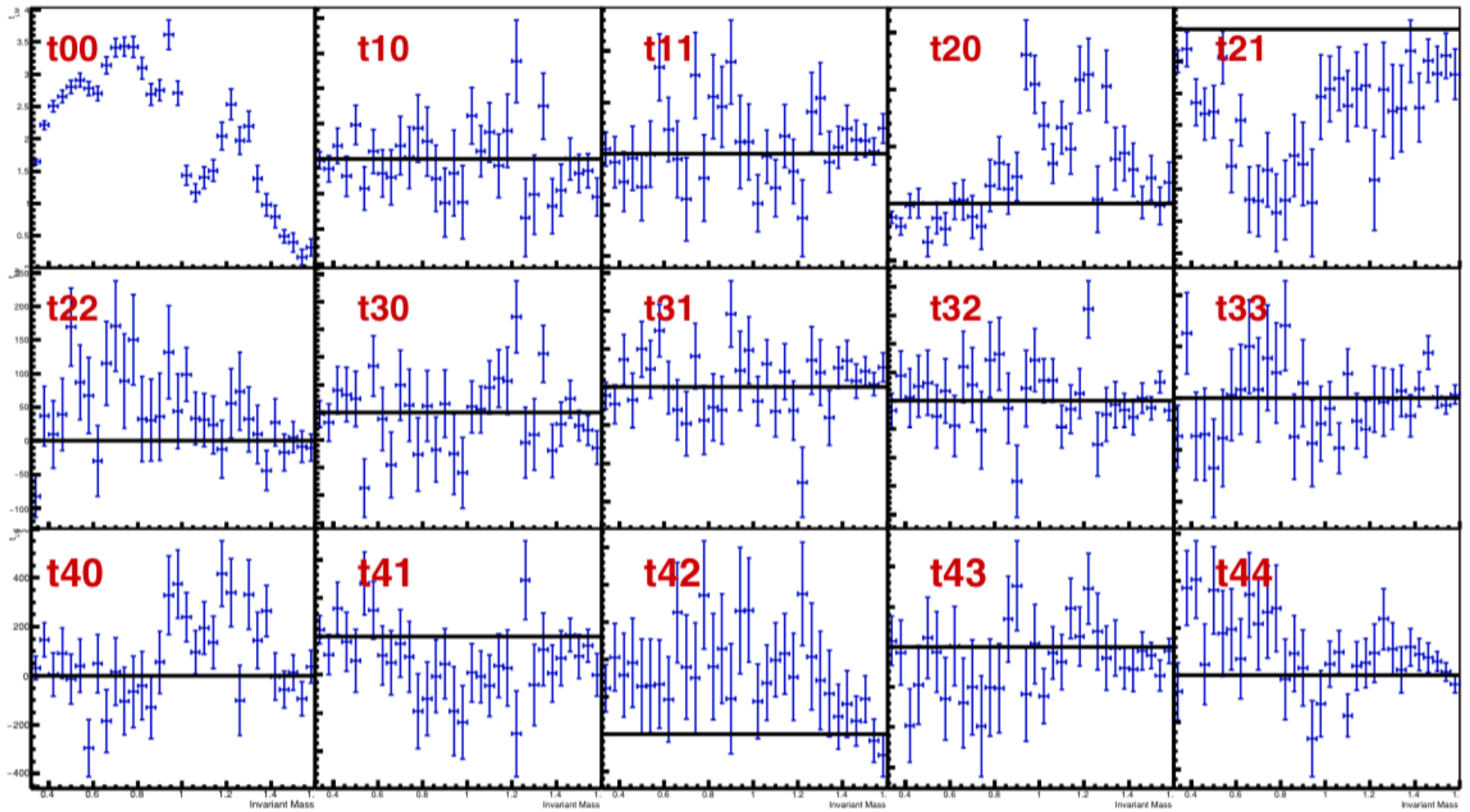


(a) Generated ϕ/π versus $\cos\theta$ of π^+



(b) Reconstructed ϕ/π versus $\cos\theta$ of π^+

PWA based on t_{LM}



Barrier factor

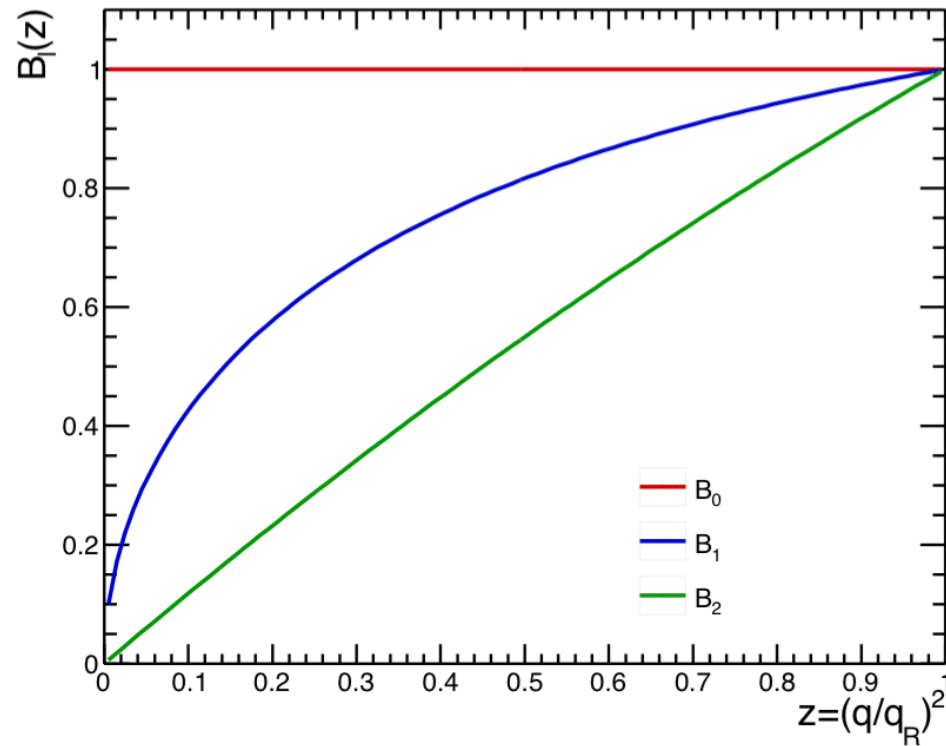
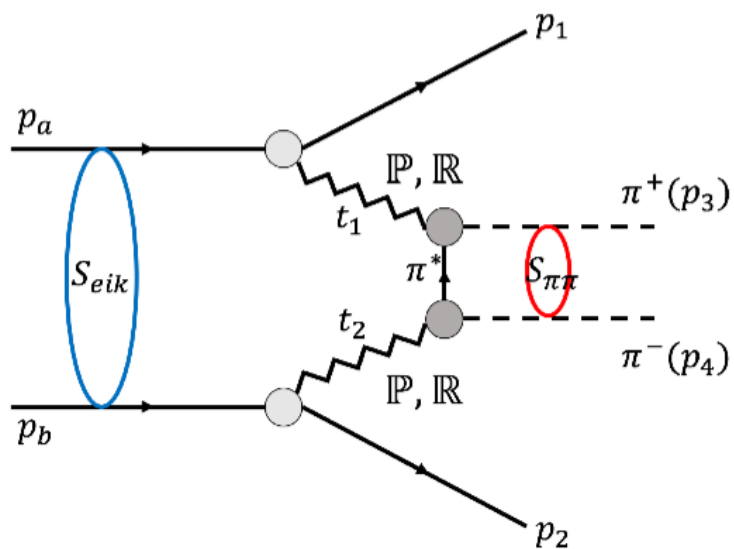
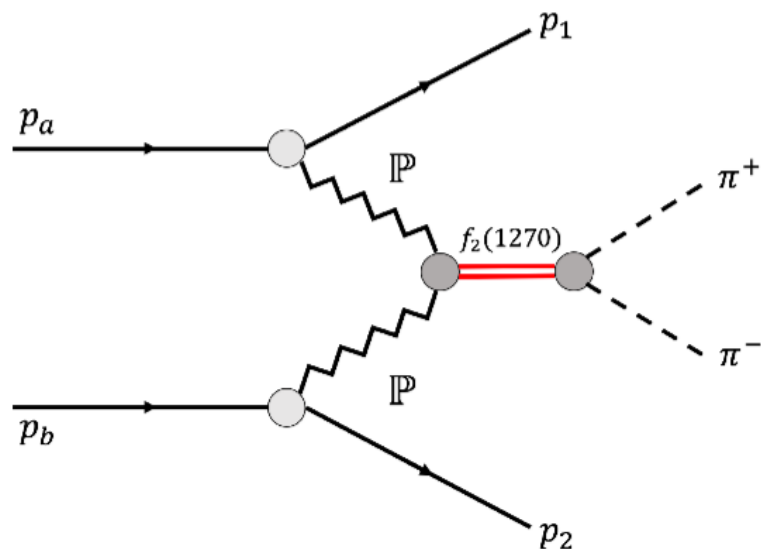


Fig. 3.10: Barrier factor B_l as a function of $z = (q/q_R)^2$ with $l = 0, 1, 2$.

Feynmann diagrams of DPE



(a) Continuum



(b) Resonances

Fig. 1.2: Feynmann diagram of the central diffraction producing dipion system. Both protons are intact only exchanging small momentum transfer $t_1 = (p_a - p_1)^2$, $t_2 = (p_b - p_2)^2$ with Pomeron (\mathbb{P}) at high energies. On the left is continuum production of dipion pairs and on the right is resonance production i.e $f_2(1270)$.