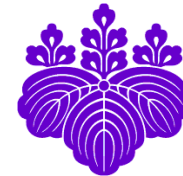


Beam Energy Scan studies at RHIC

Flow studies in small system

Shinichi Esumi
Inst. of Physics, Univ. of Tsukuba
Center for Integrated Research in
Fundamental Science and Engineering (CiRfSE)



for “**Heavy-Ion Meeting (HIM : force)**” just after KPS2016 fall meeting
in **Chonnam National University, Gwangju, Korea**

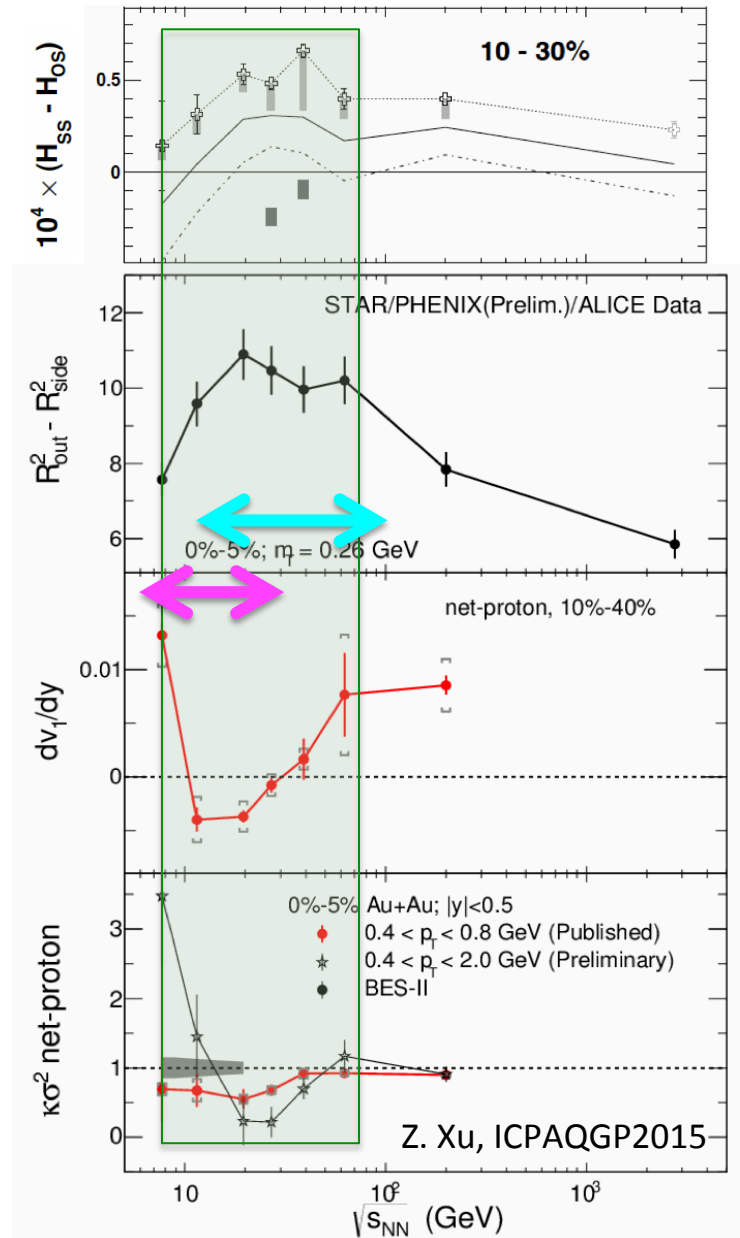
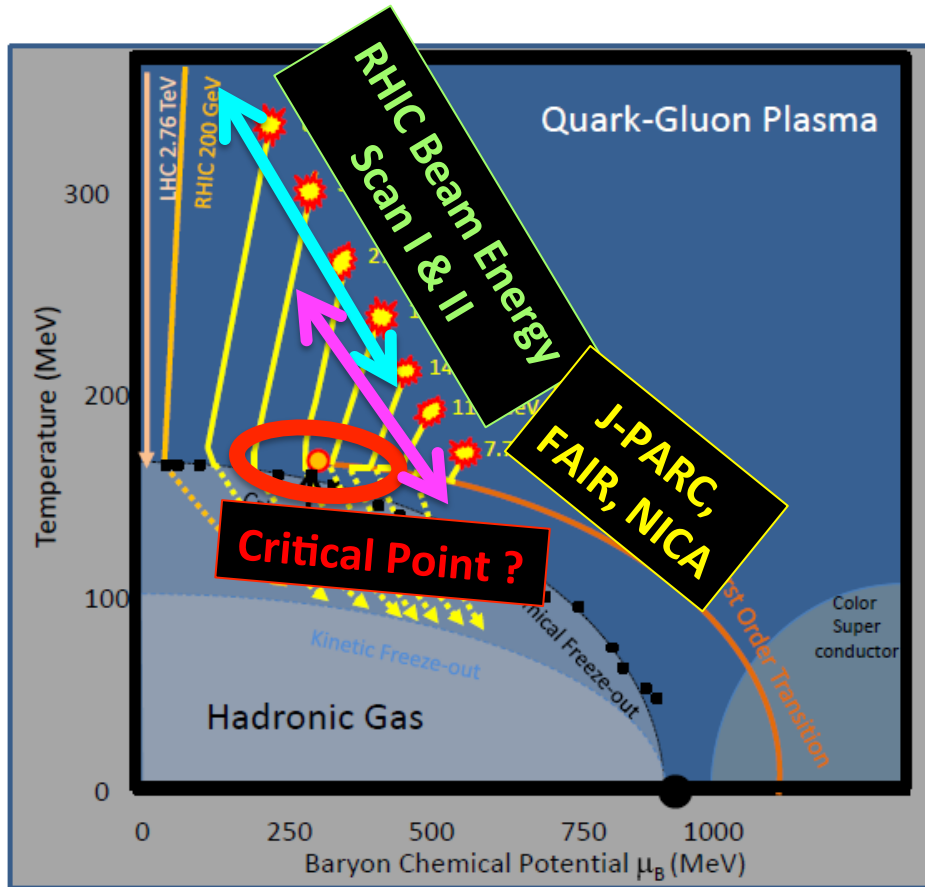
Heavy-Ion Café meeting : in Tokyo-Tsukuba-KEK area (East side of Japan)

Heavy-Ion Pub meeting in Hiroshima-Osaka-Nara-Nagoya area (West side of Japan)

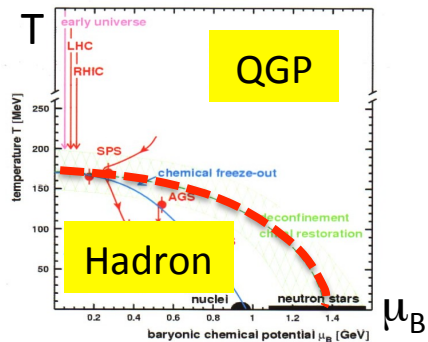
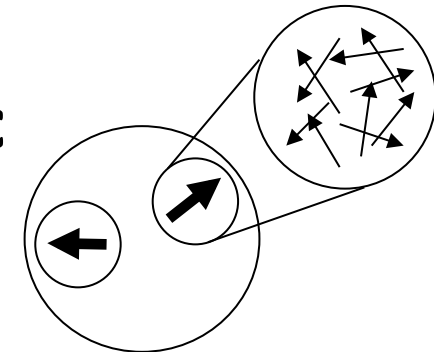
RHIC beam energy scan (BES) program from phase I to phase II

~ 2016

2019 ~

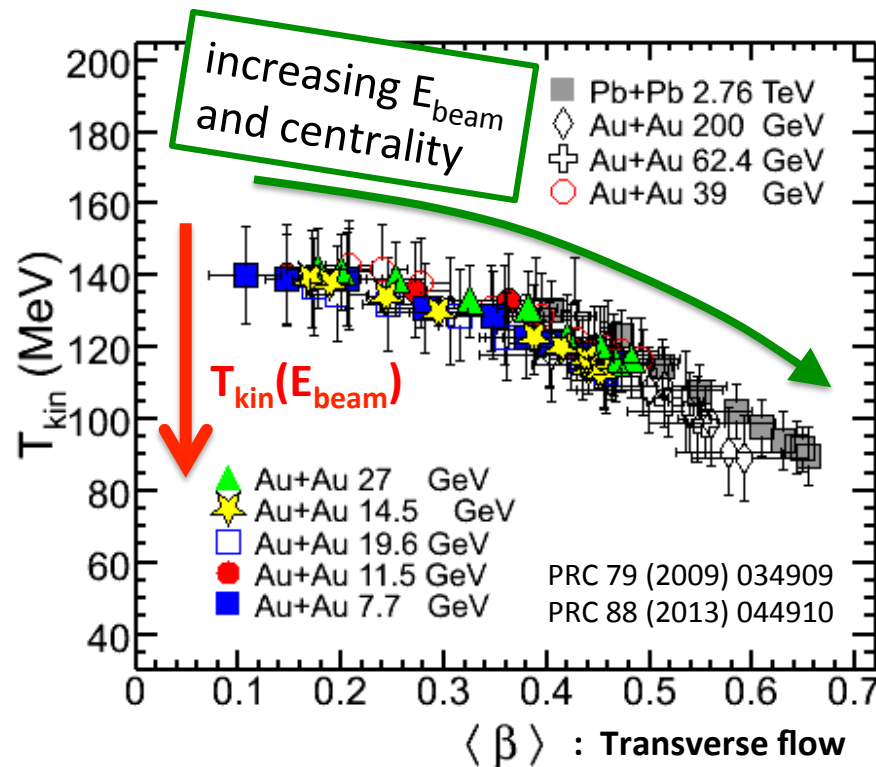
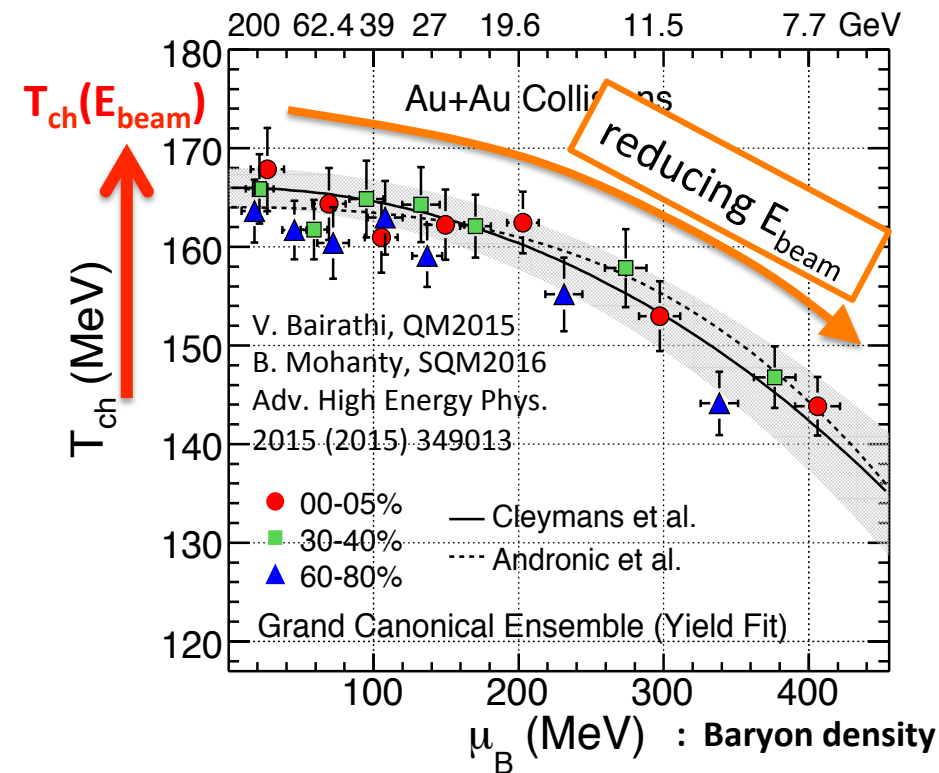


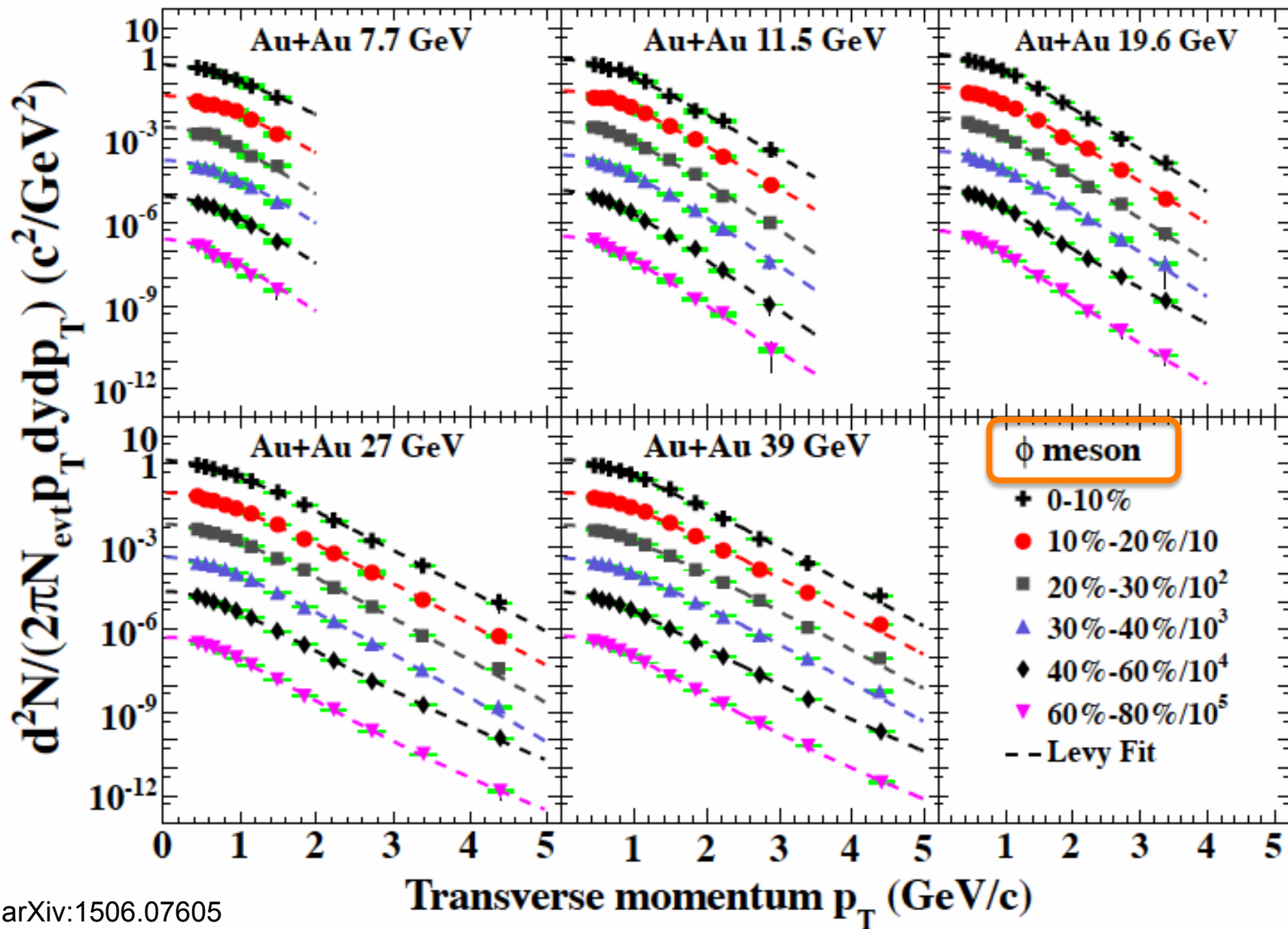
Chemical and Thermal kinetic freeze-out with radial flow



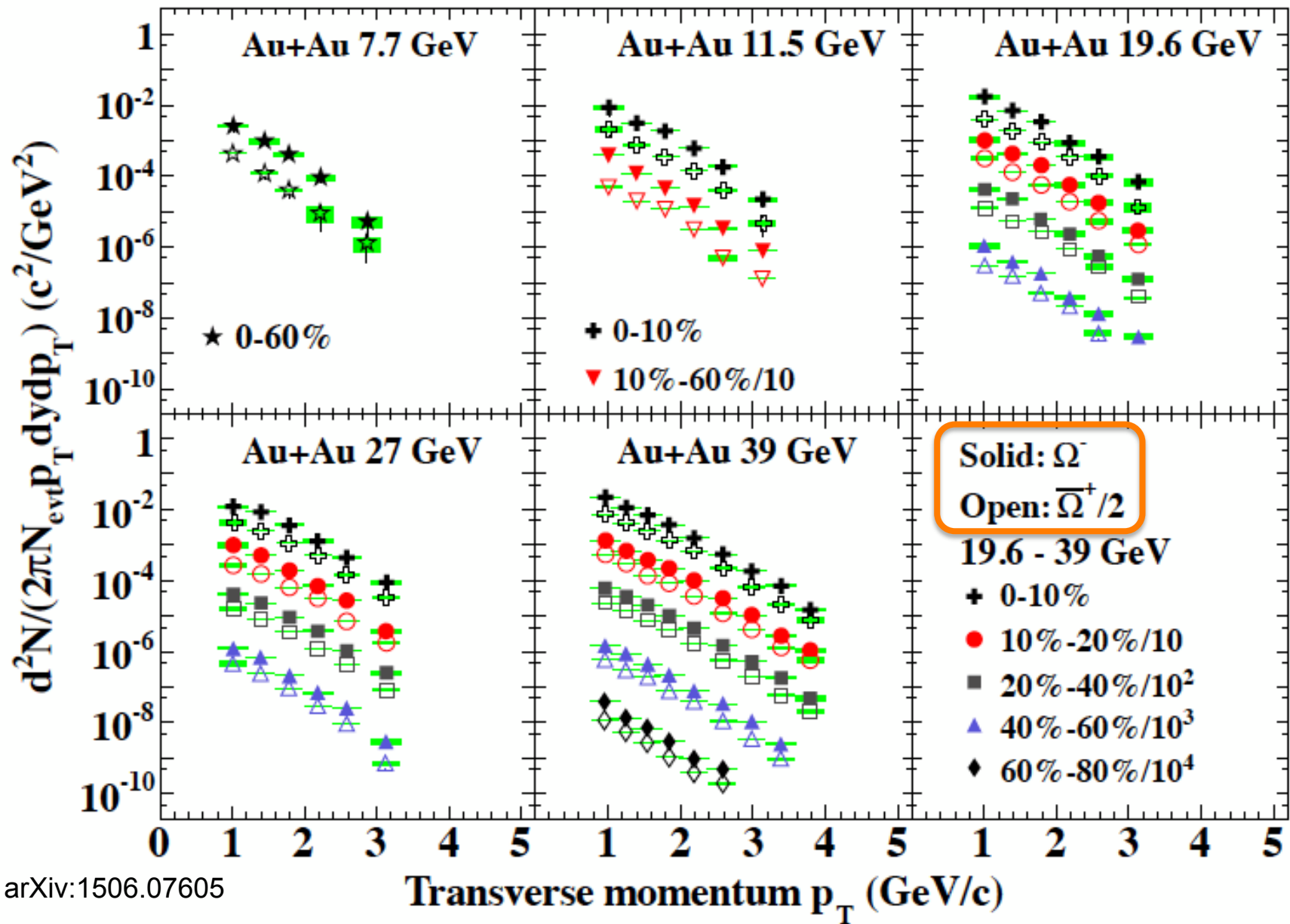
Hadron yields are fitted with chemical thermal model in order to extract (T_{ch}, μ_B) parameters.

Hadron p_T spectra are fitted with Blast-wave model in order to extract (T_{kin}, β_T) parameters.





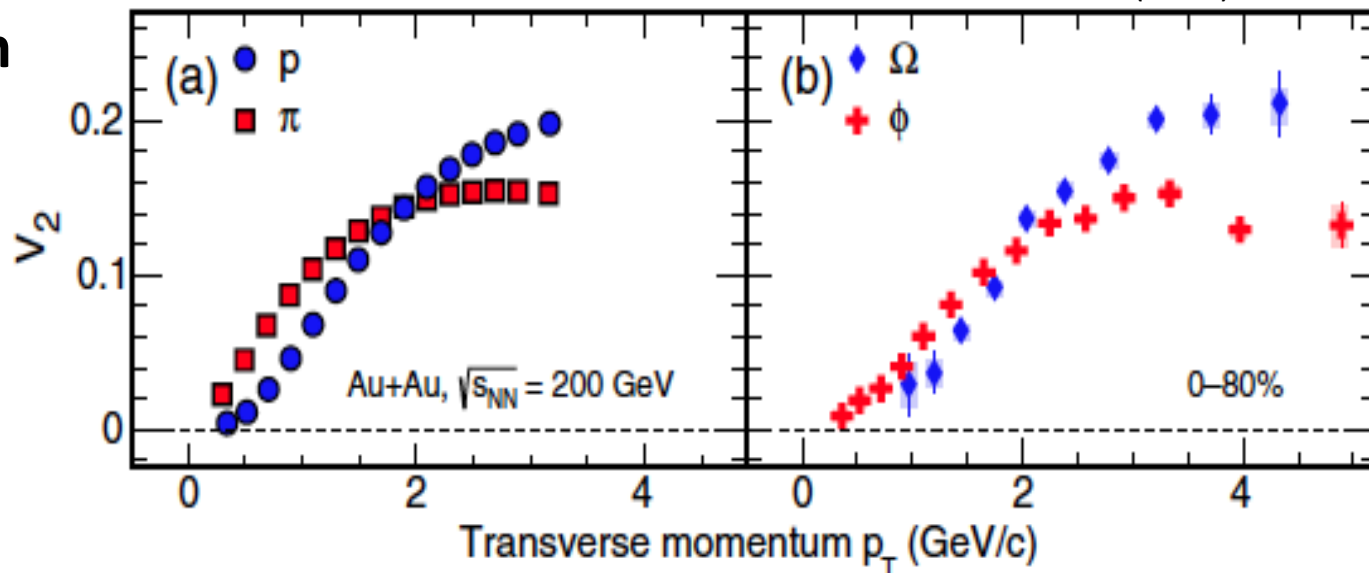
arXiv:1506.07605



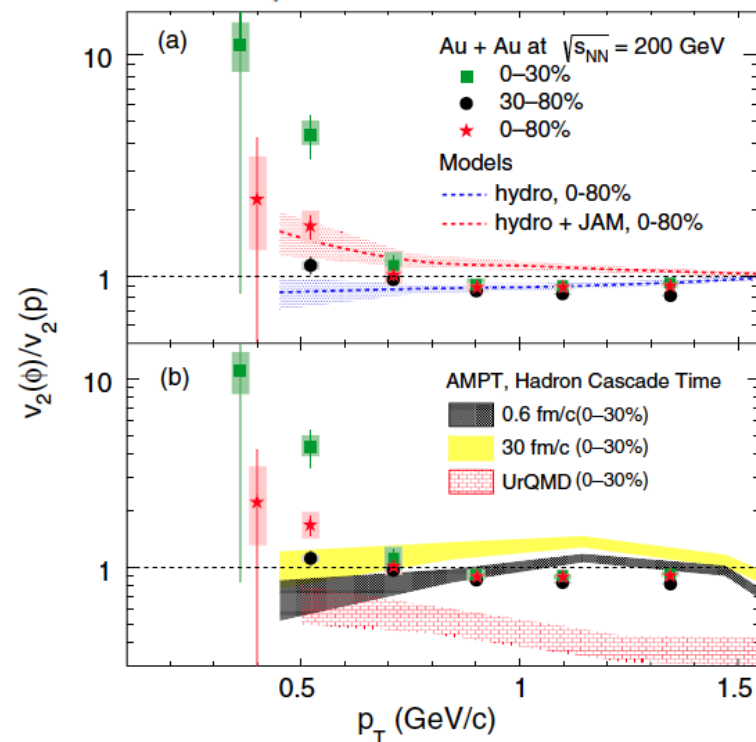
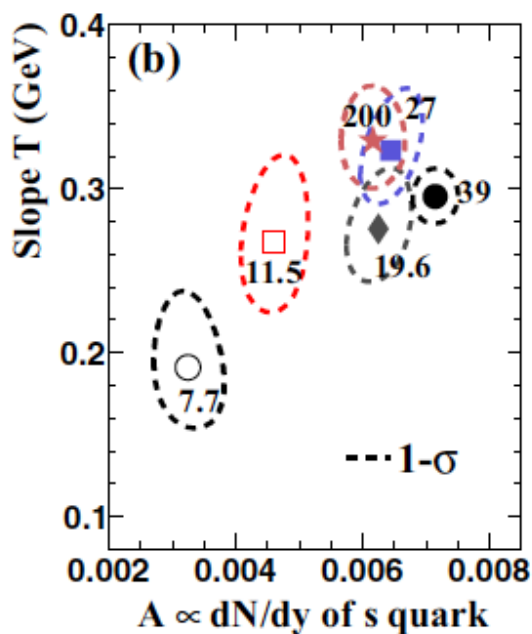
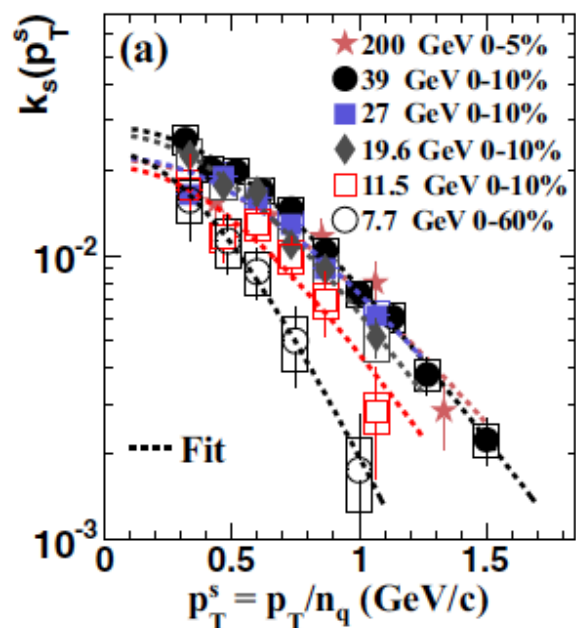
arXiv:1506.07605

System Evolution from Partonic to Hadronic Phase

$$k_s = N(\Omega)/N(\phi)$$



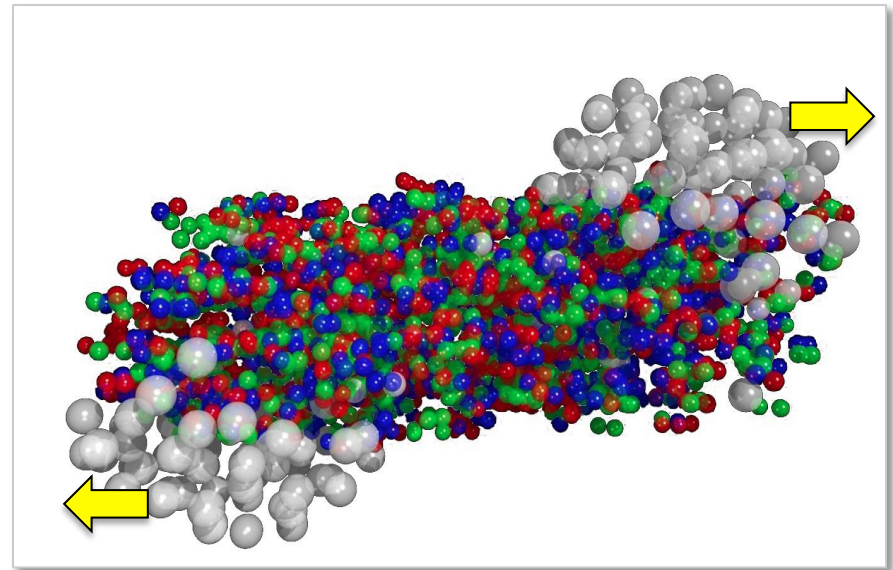
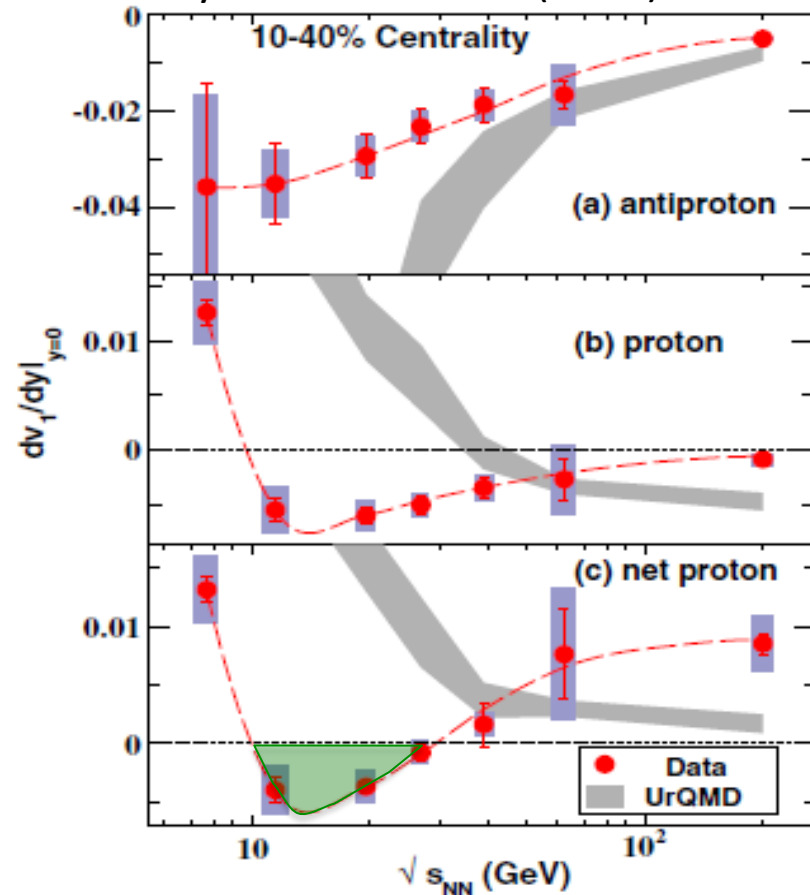
PRC93 (2016) 021903R



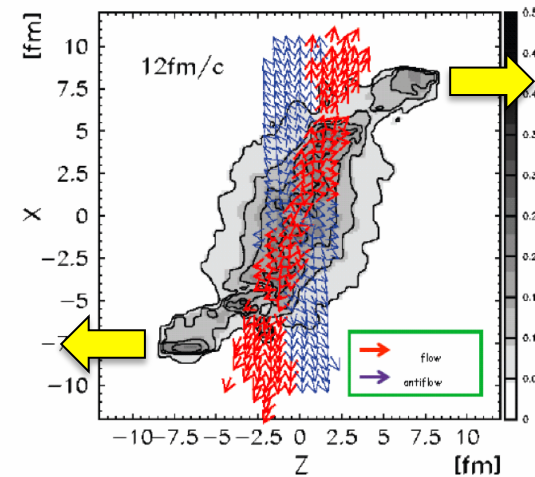
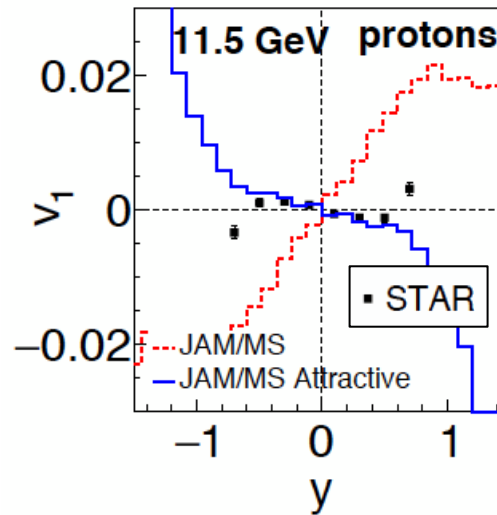
Directed flow (v_1)

negative slope of dv_1/dy for net-proton
softening of Equation of State

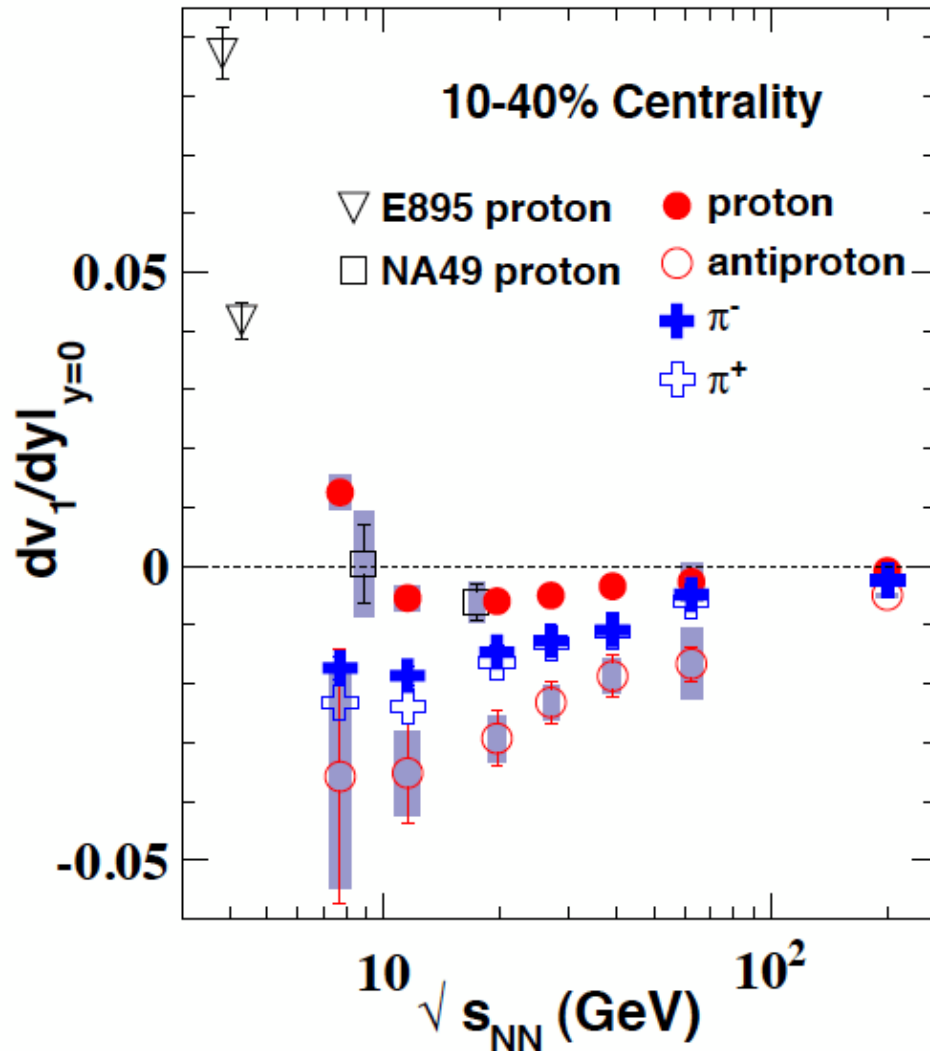
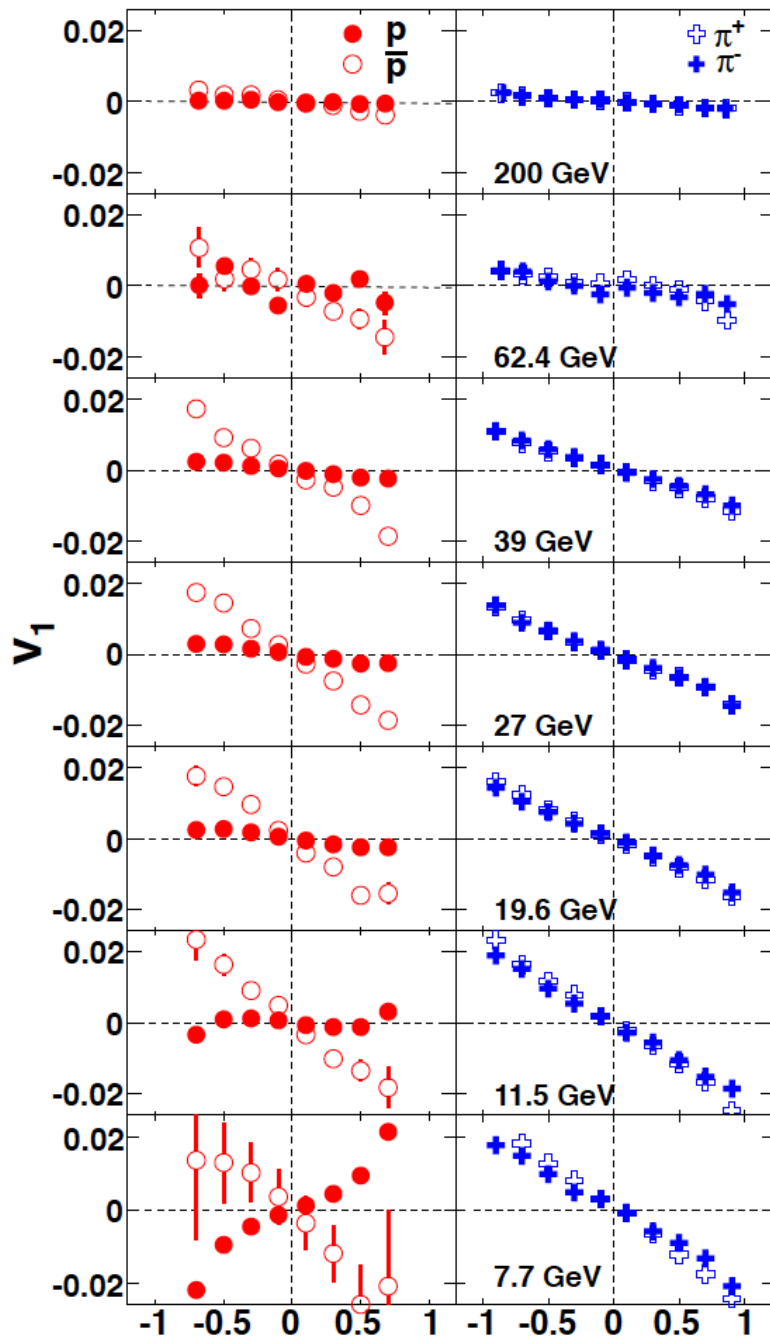
Phys. Rev. Lett. 112 (2014) 162301



arXiv : 1601.07692



J. Brachmann et al., PRC 61, 24909 (2000).



arXiv:1401.3043
 PRL112 (2014) 16, 162301

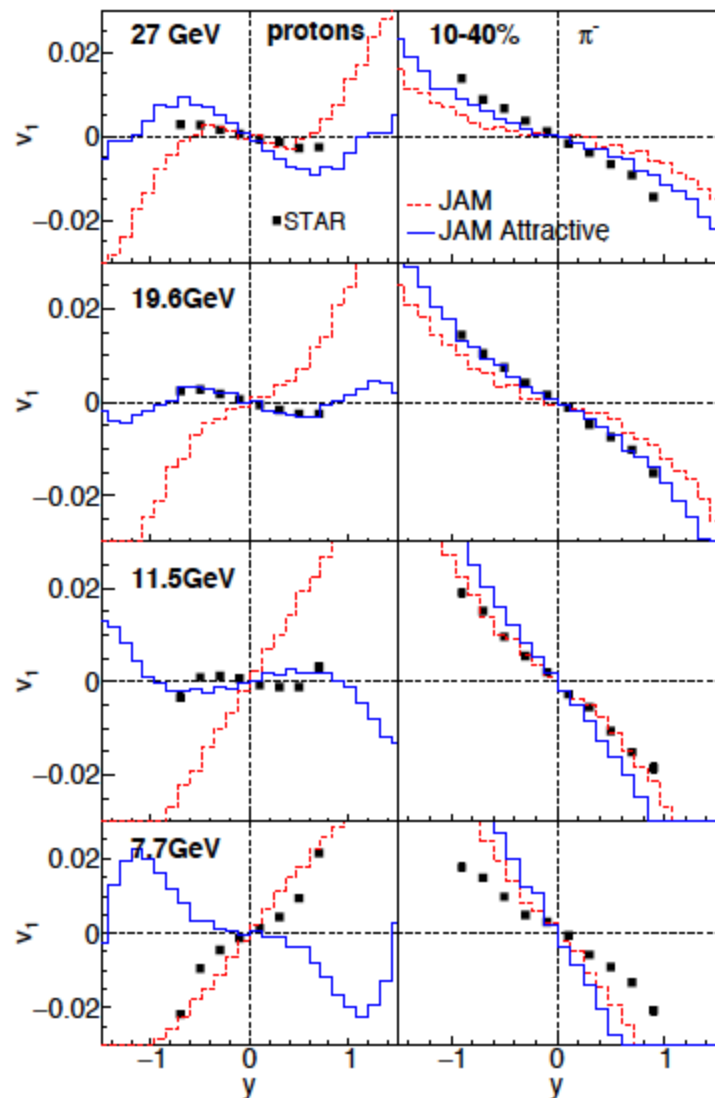


FIG. 1: Directed flows of protons and pions in mid-central Au+Au collisions (10-40%) at $\sqrt{s_{NN}} = 7.7 - 27$ GeV from JAM cascade mode (dashed lines), and JAM cascade with attractive orbits (solid lines) in comparison with the STAR data [1].

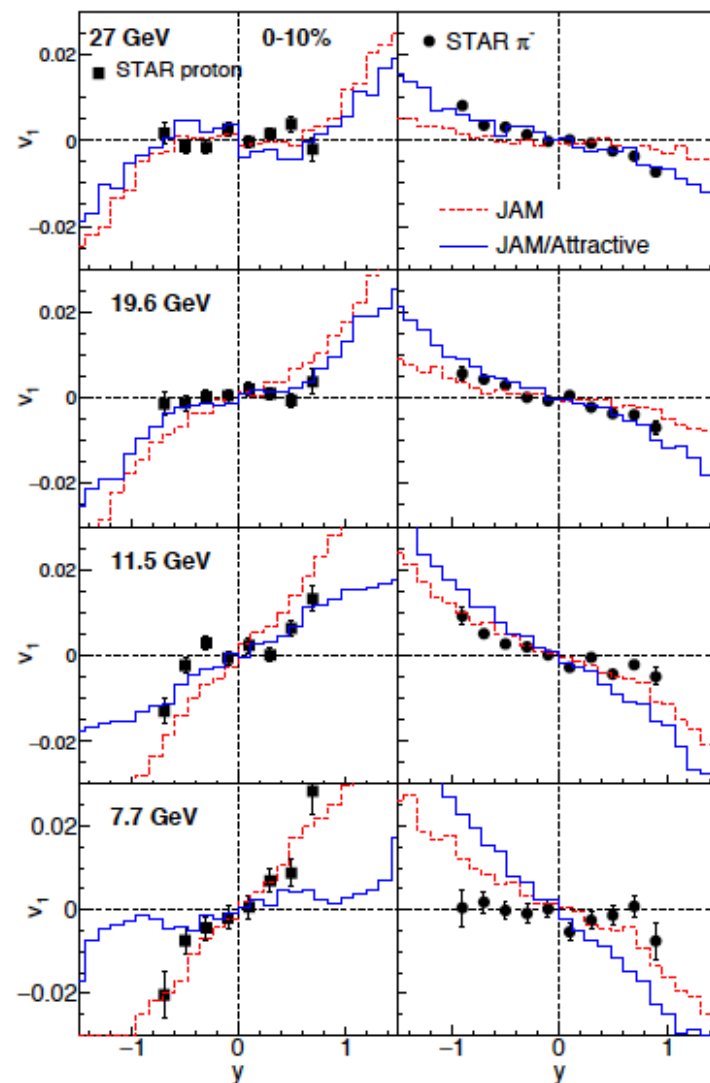
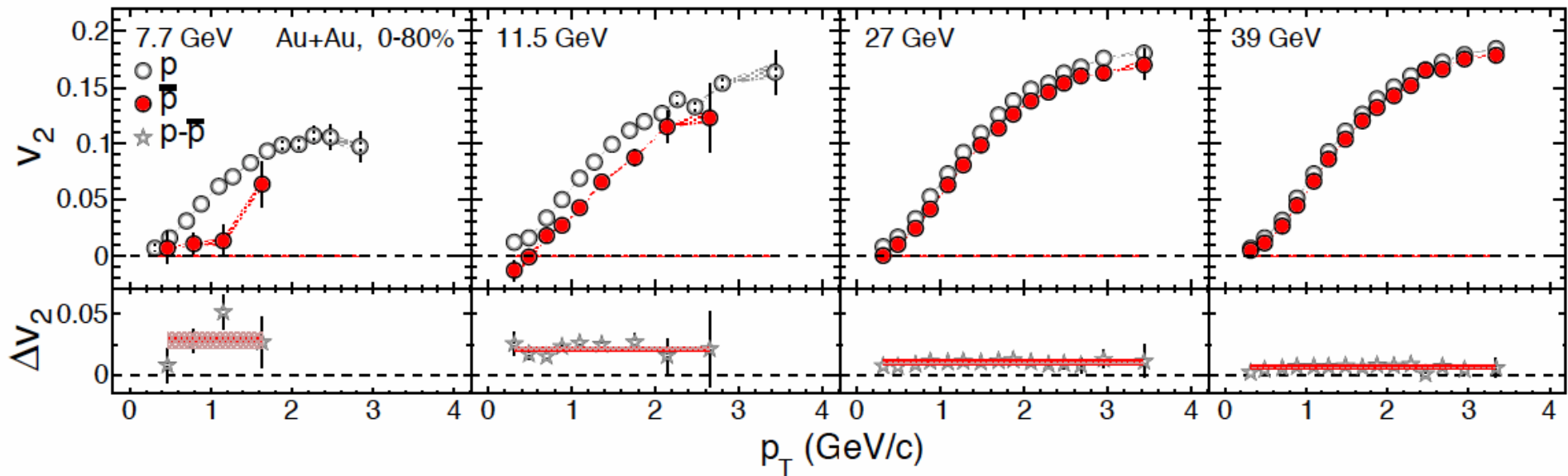
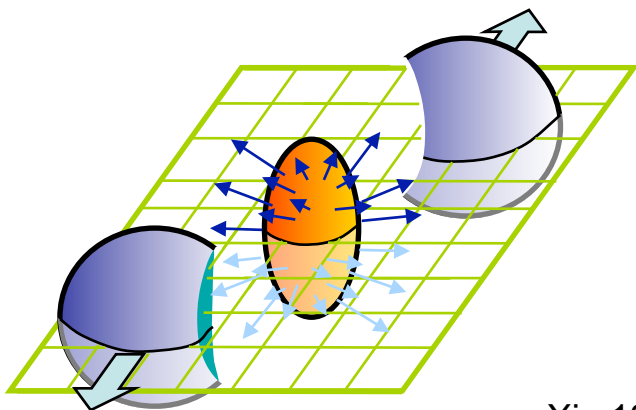


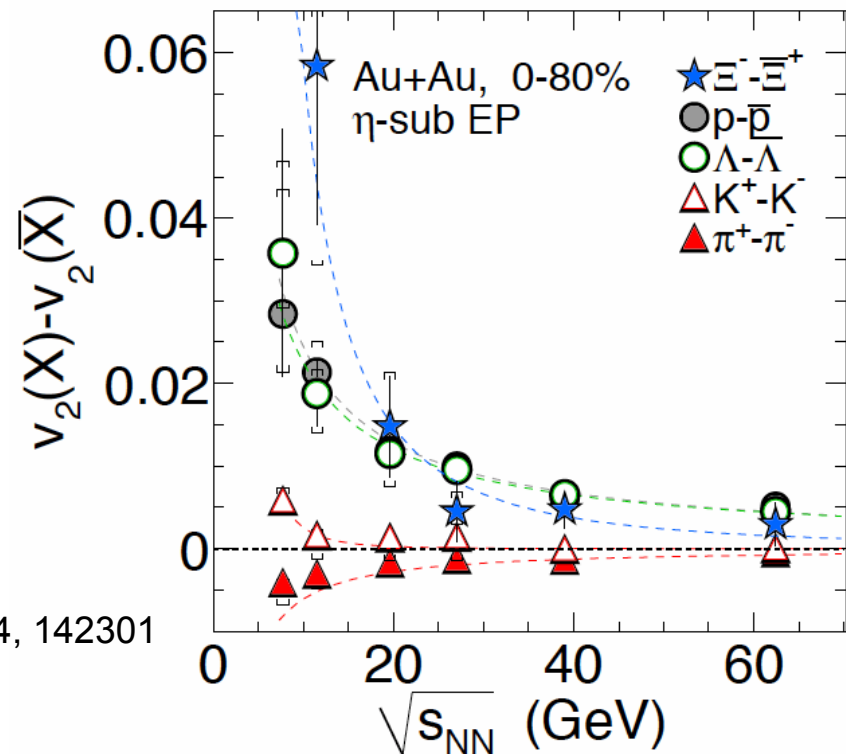
FIG. 2: Same as in Fig. 1, but for central collisions (0-10%).

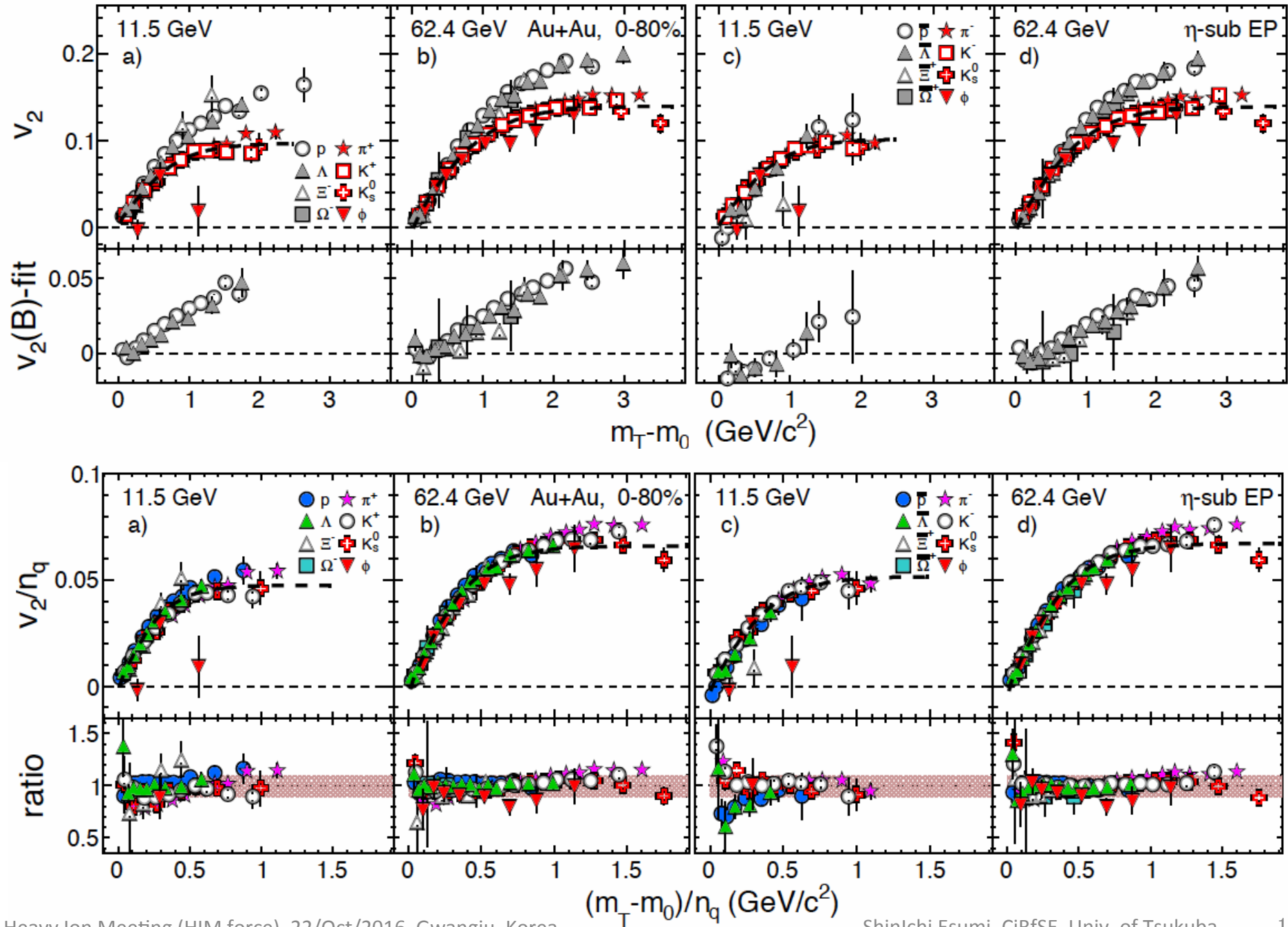


Elliptic Flow v_2



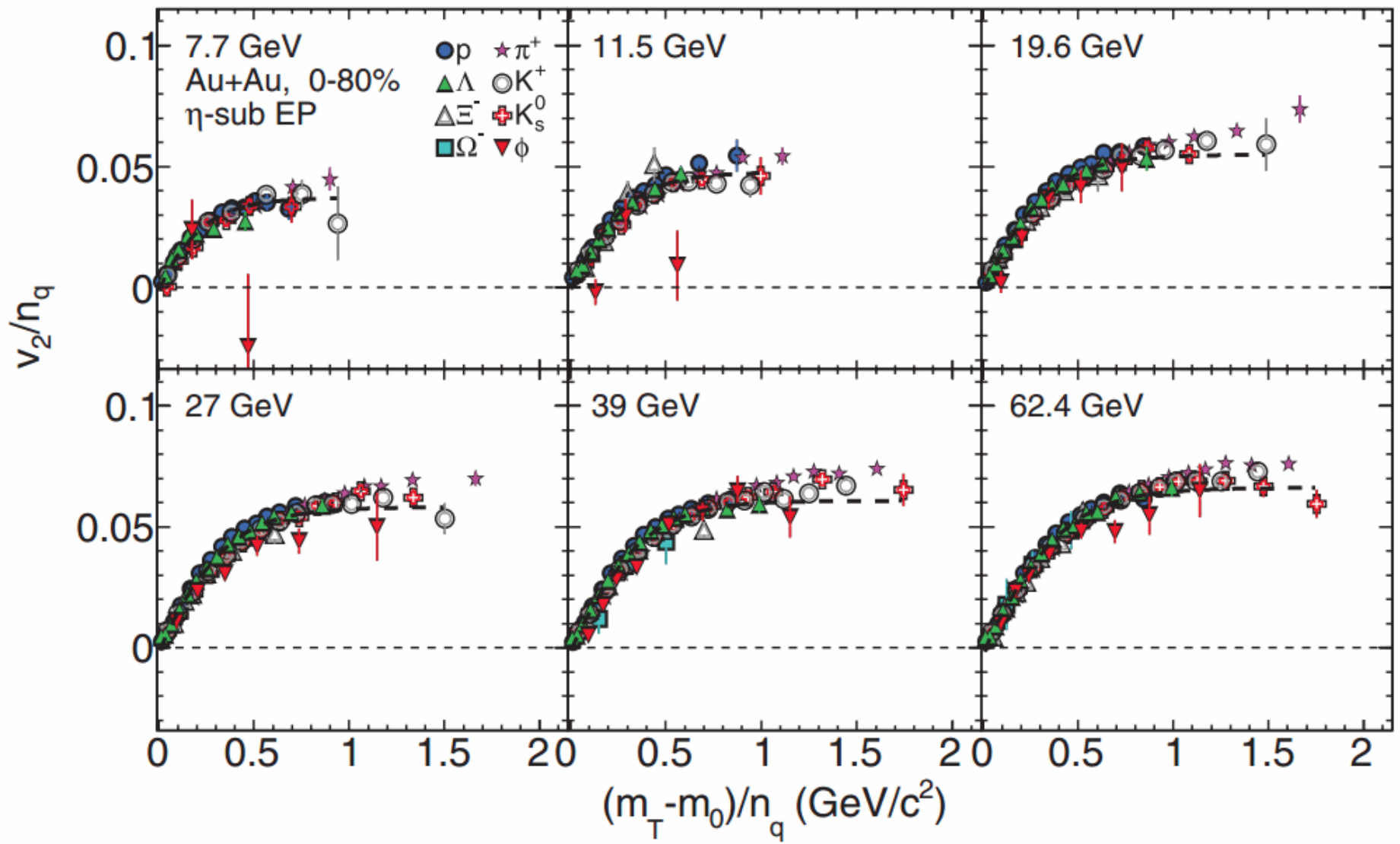
arXiv:1301.2347
PRL110 (2013) 14, 142301



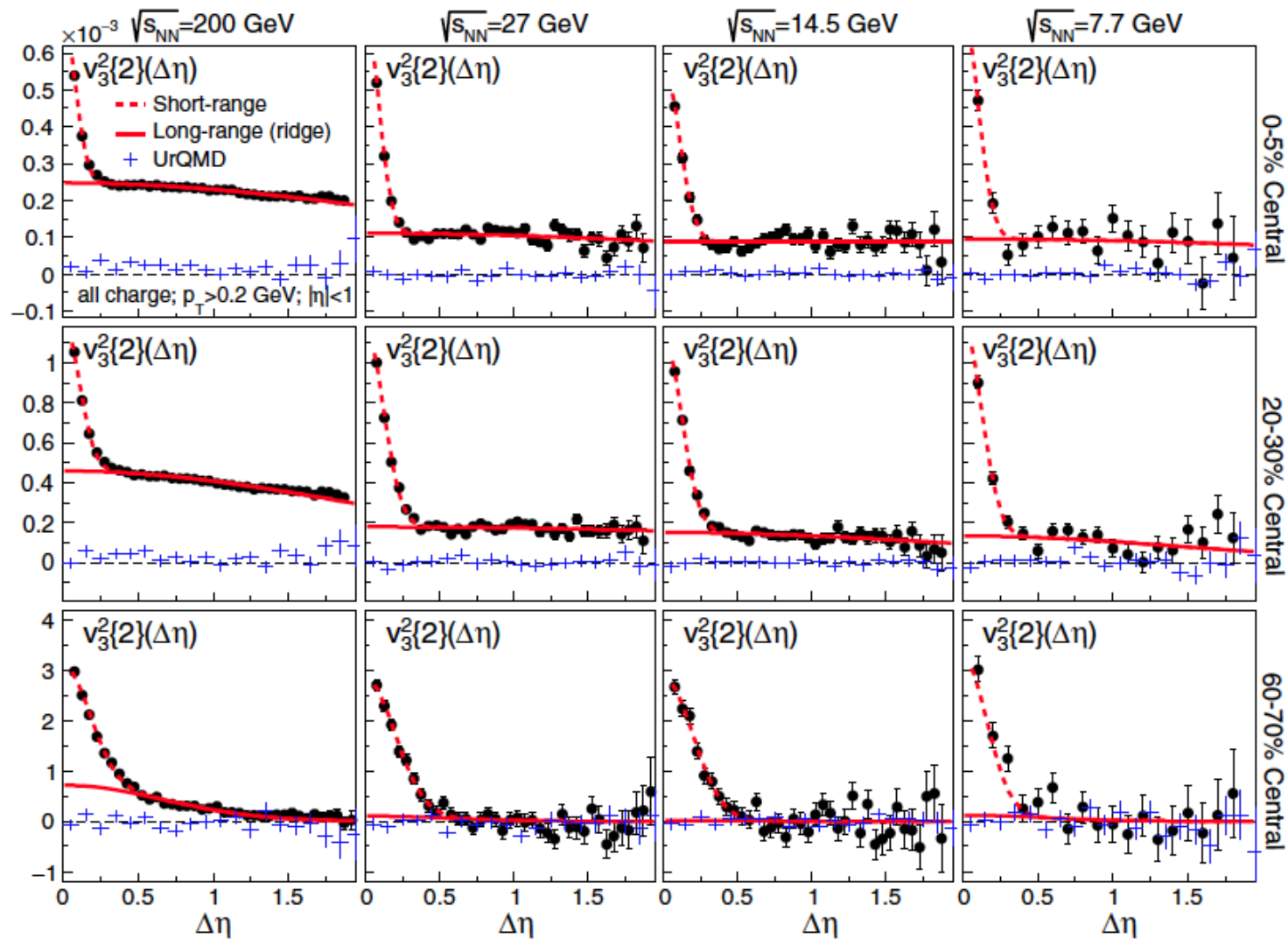


Elliptic Flow v_2 --- departure from quark number scaling ---

PRC88 (2013) 014902



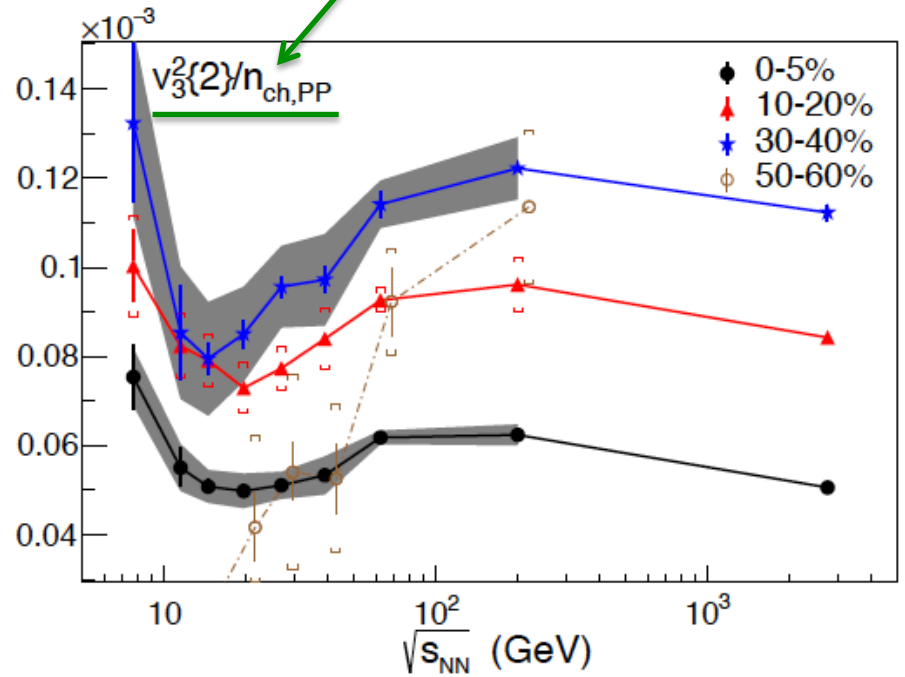
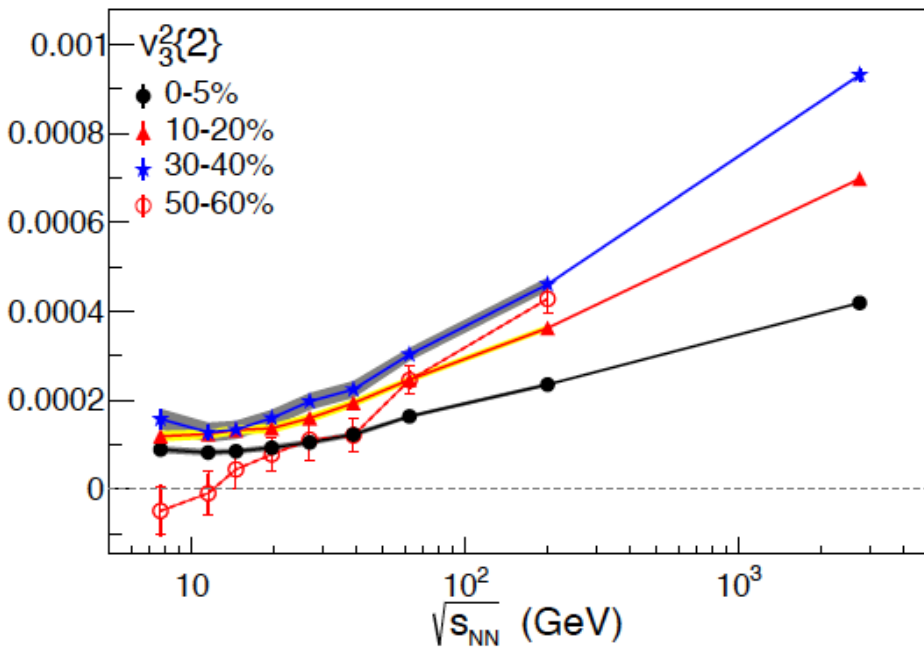
Beam energy dependence of v_3^2



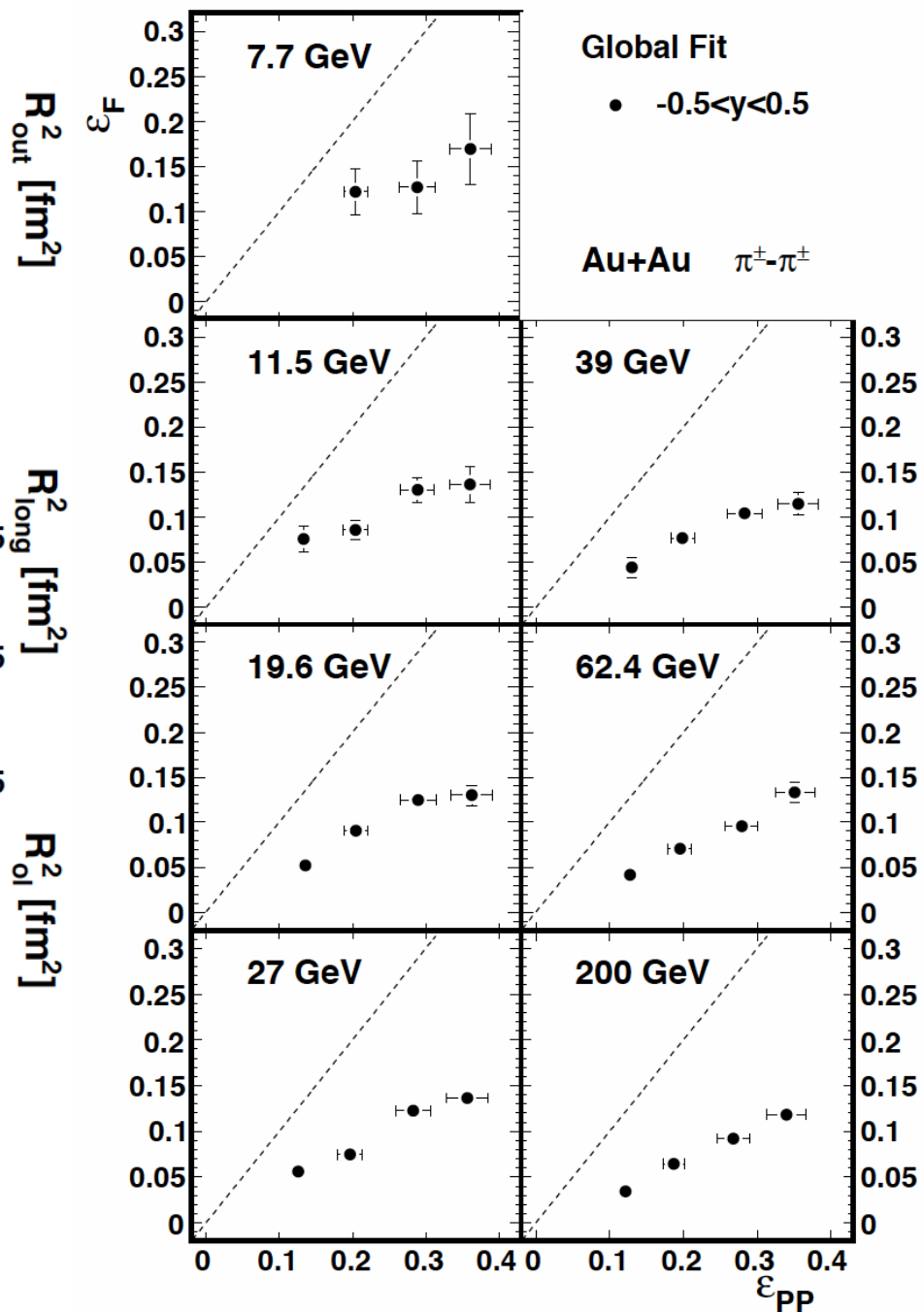
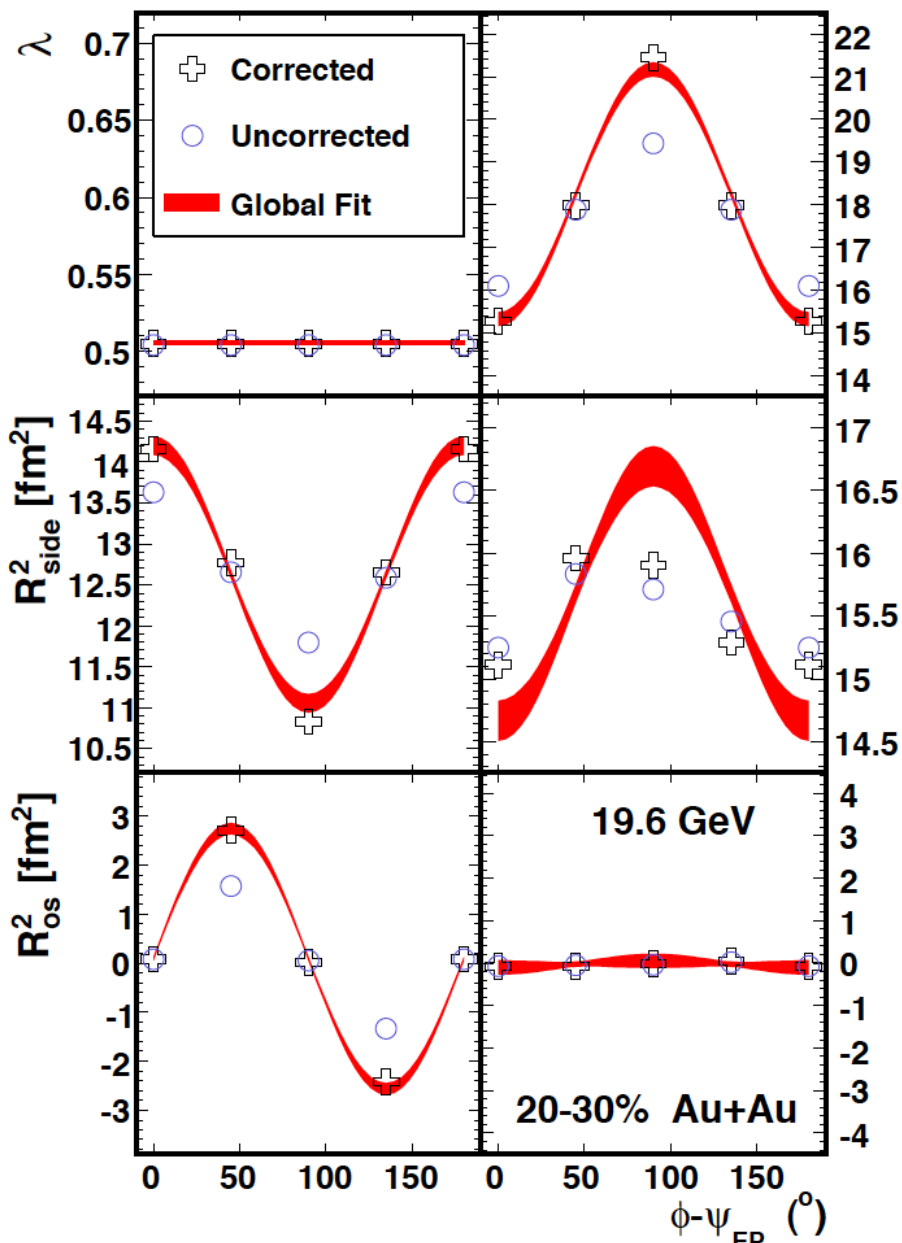
Beam energy dependence of $v_3^2/n_{\text{ch,PP}}$

PRL116 (2016) 112302

$$n_{\text{ch,PP}} = \frac{2}{N_{\text{part}}} dN_{\text{ch}}/d\eta.$$

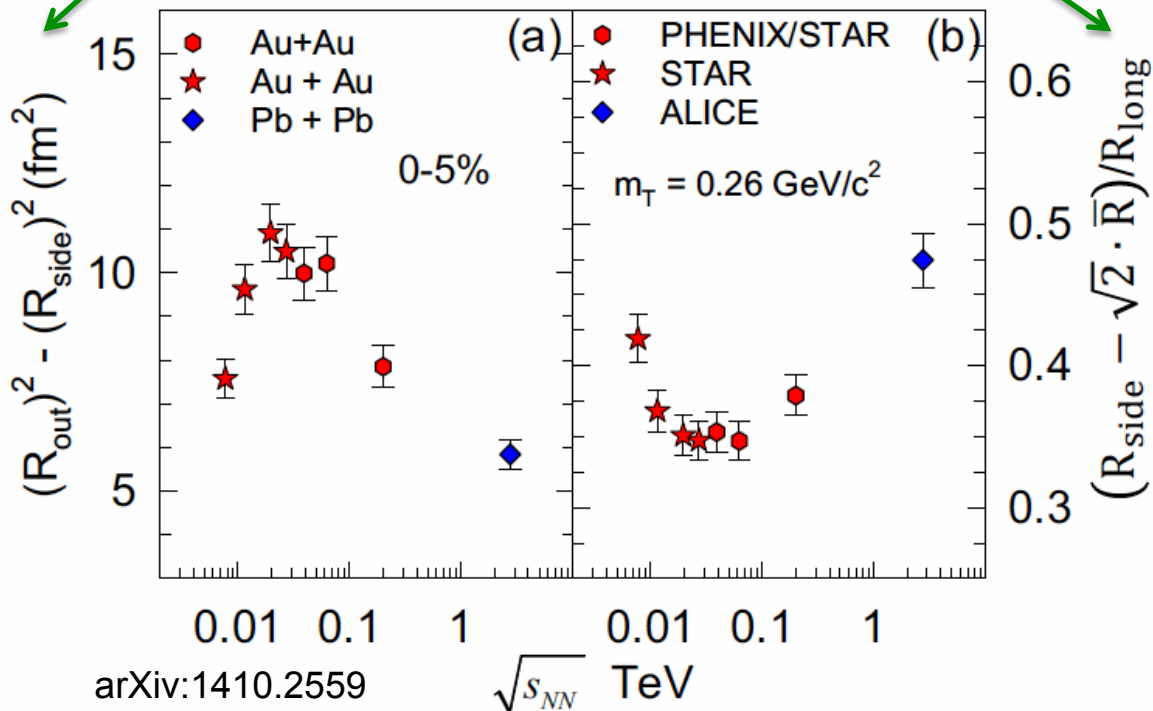
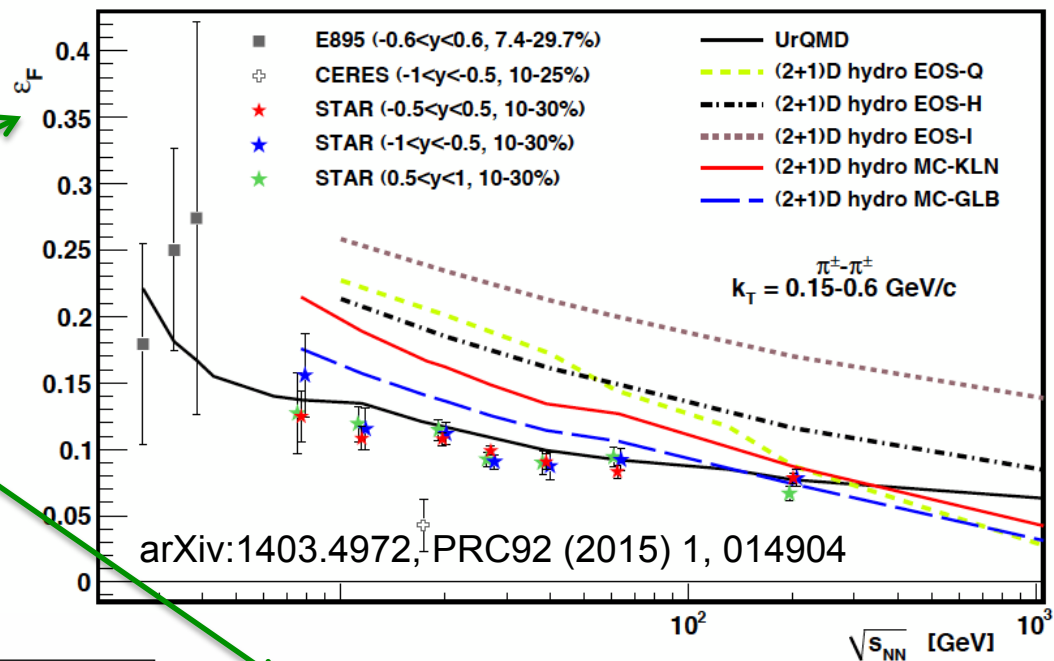


extraction of freeze-out eccentricity

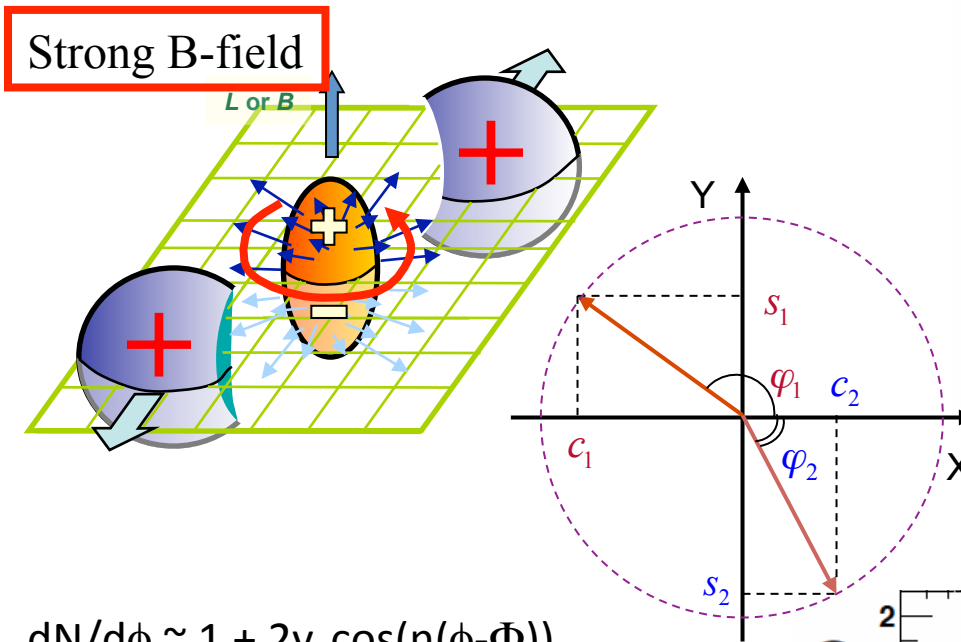


arXiv:1403.4972, PRC92 (2015) 1, 014904

Energy dependence of
 (1) freeze-out shape ϵ_{Final}
 (2) duration time
 (3) expansion velocity
 from HBT data



charge separation signal w.r.t. reaction plane from local parity violation

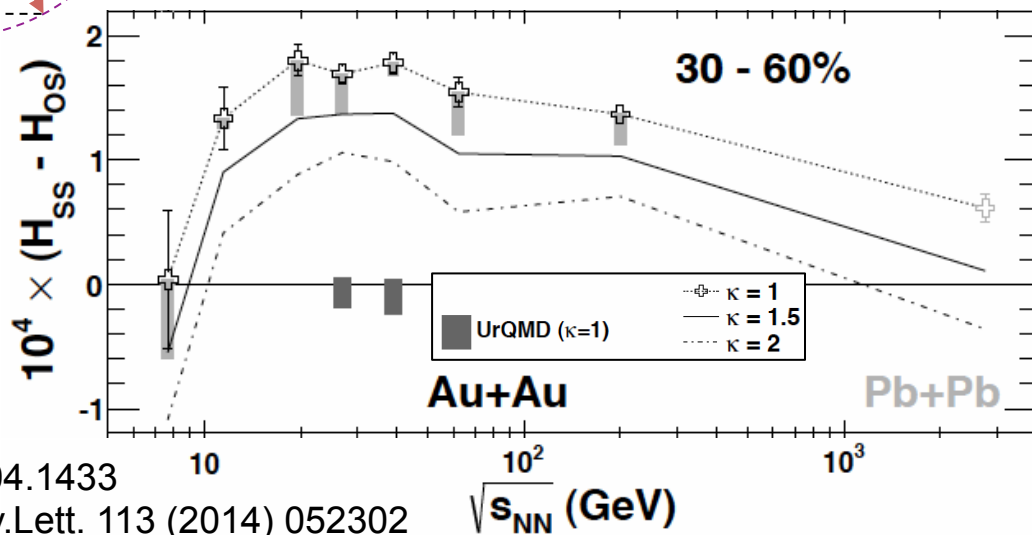
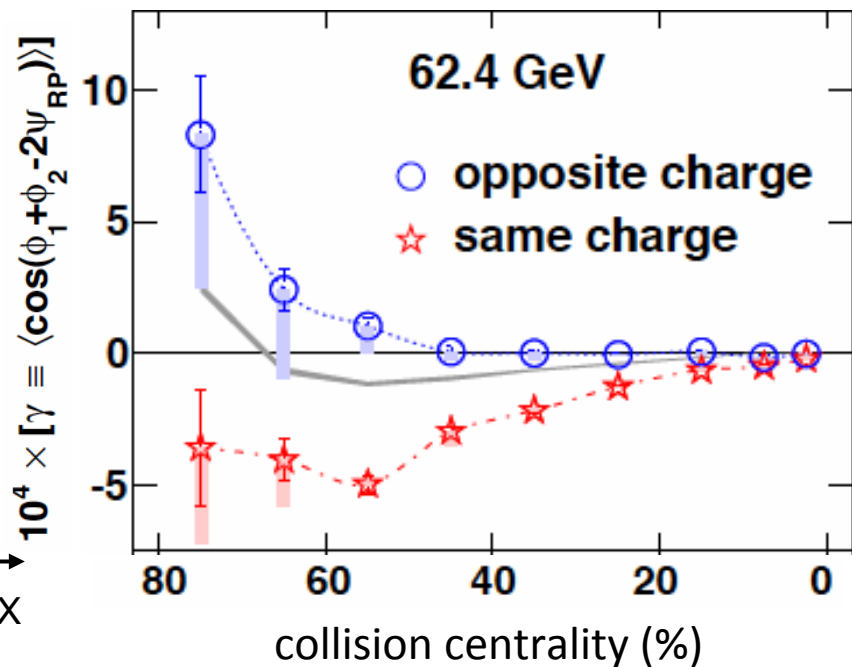


$$\frac{dN}{d\phi} \sim 1 + 2v_n \cos(n(\phi - \Phi)) + 2a_{+/-} \sin(\phi - \Phi)$$

$$\langle \cos(\phi_1 + \phi_2 - 2\Phi) \rangle \sim -\langle a_1 a_2 \rangle$$

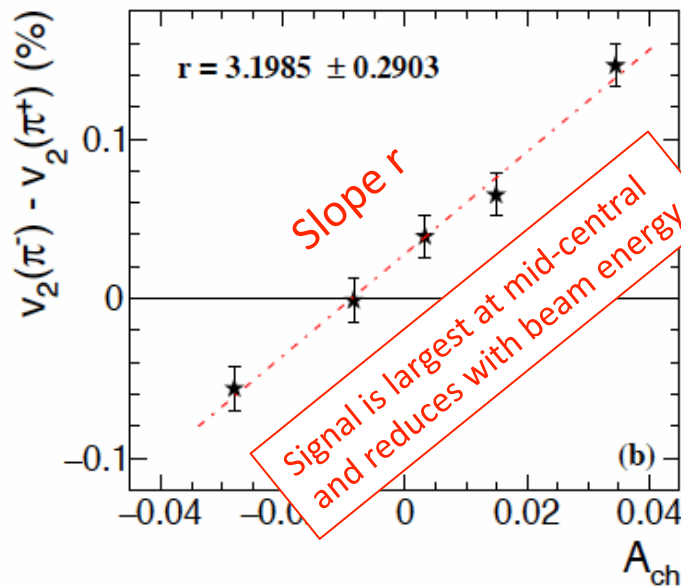
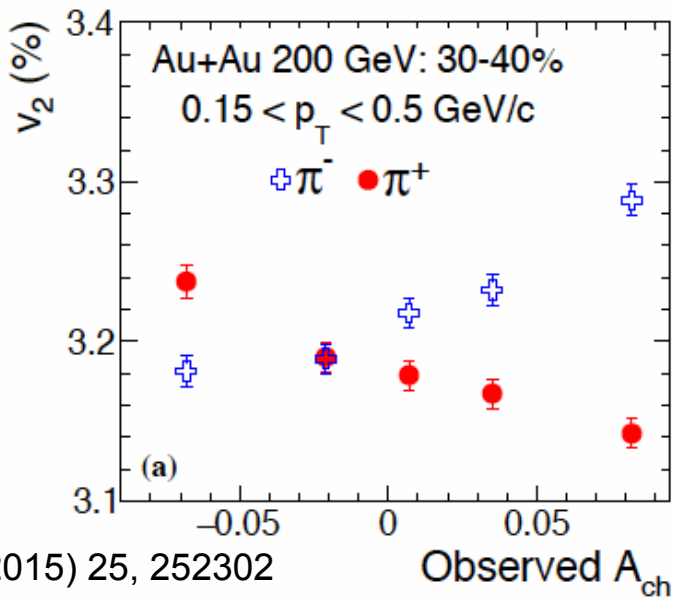
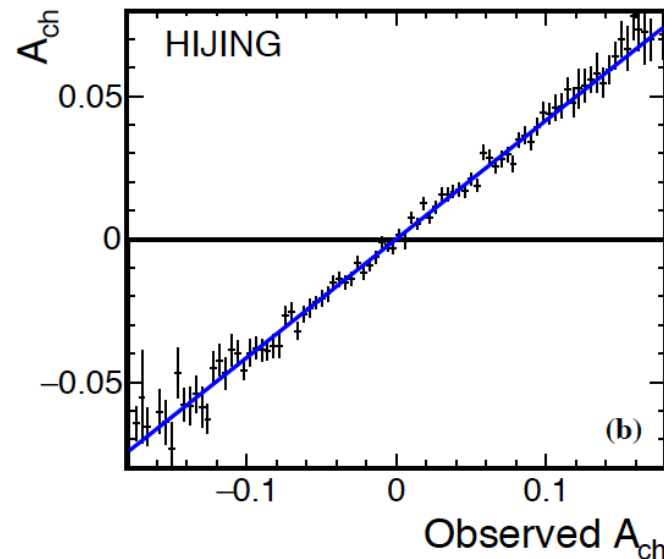
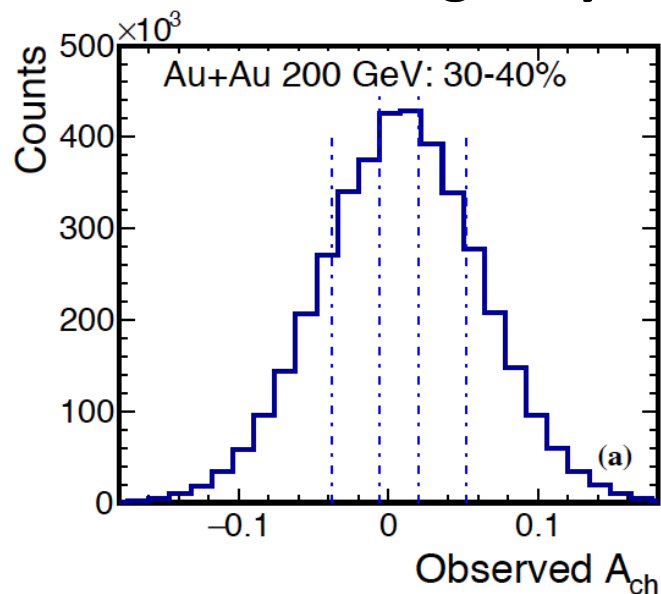
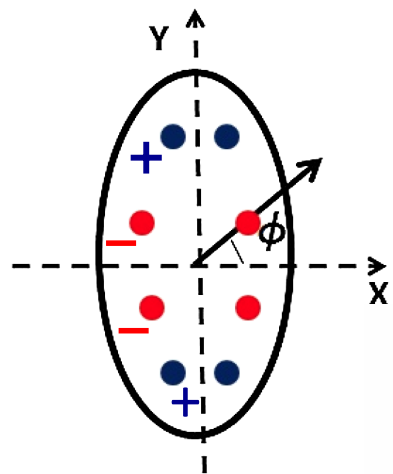
$$\gamma \equiv \langle \cos(\phi_1 + \phi_2 - 2\Psi_{RP}) \rangle = \kappa v_2 F - H$$

$$\delta \equiv \langle \cos(\phi_1 - \phi_2) \rangle = F + H,$$



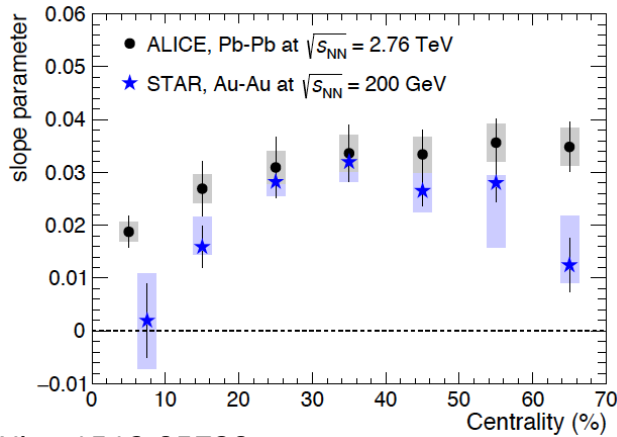
arXiv:1404.1433
Phys.Rev.Lett. 113 (2014) 052302

charge dependent v_2 w.r.t. charge asymmetry



arXiv:1504.02175
 Phys.Rev.Lett. 114 (2015) 25, 252302

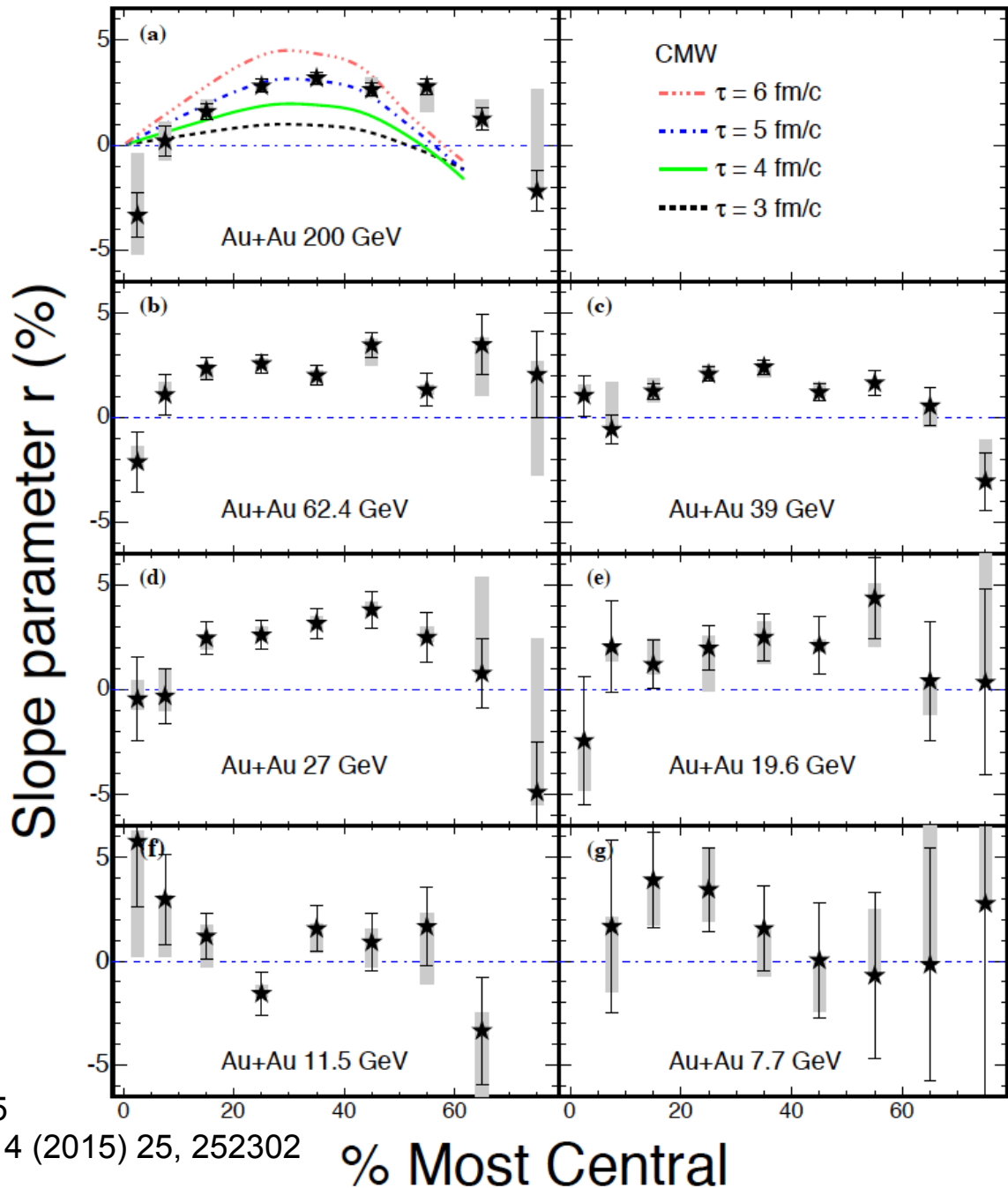
Slope :
 $r = \Delta v_2 / \Delta A_{ch}$



arXiv : 1512.05739

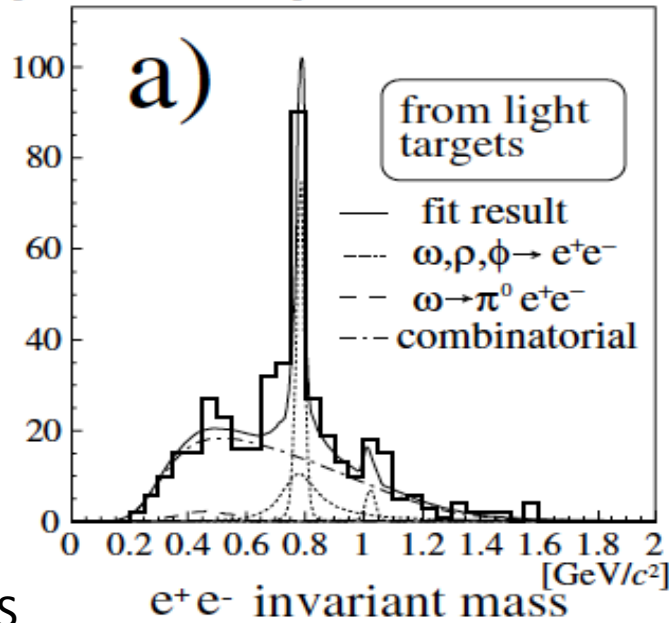
arXiv:1504.02175

Phys.Rev.Lett. 114 (2015) 25, 252302



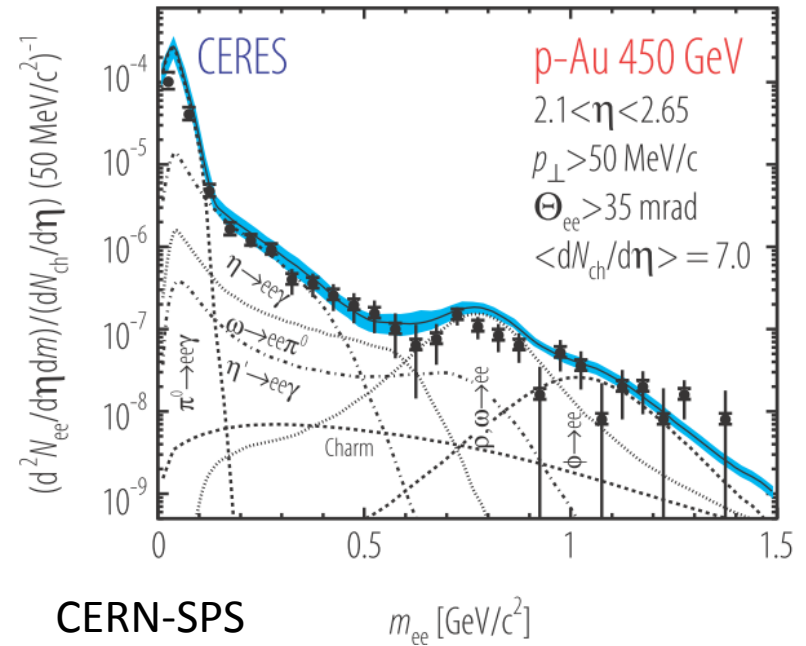
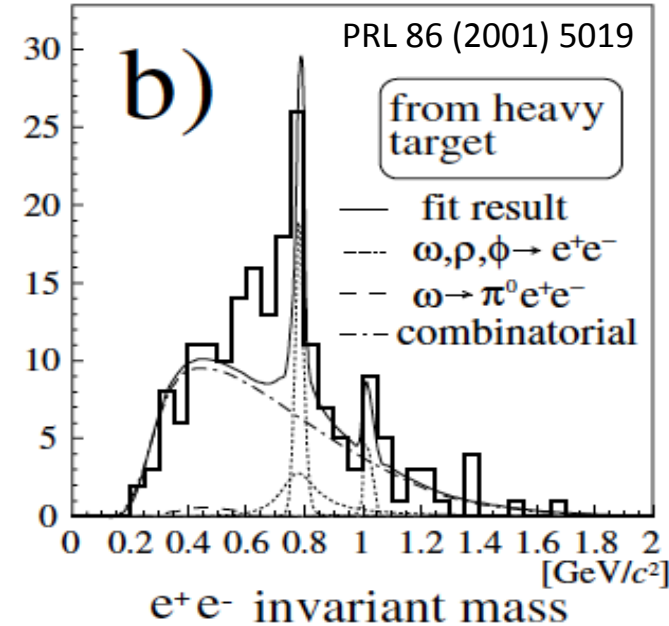
% Most Central

[events / 50MeV/c²]



KEK-PS

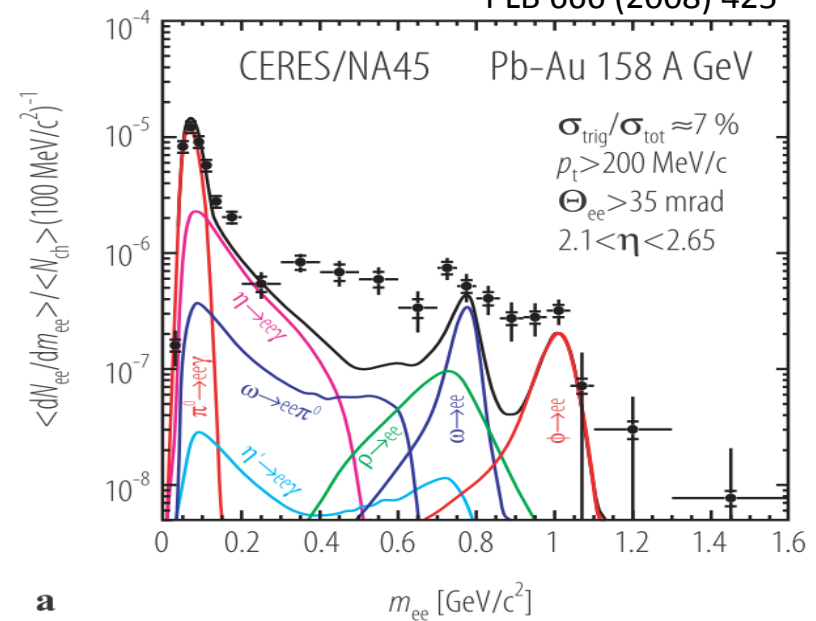
[events / 50MeV/c²]



CERN-SPS

m_{ee} [GeV/c²]

PLB 666 (2008) 425

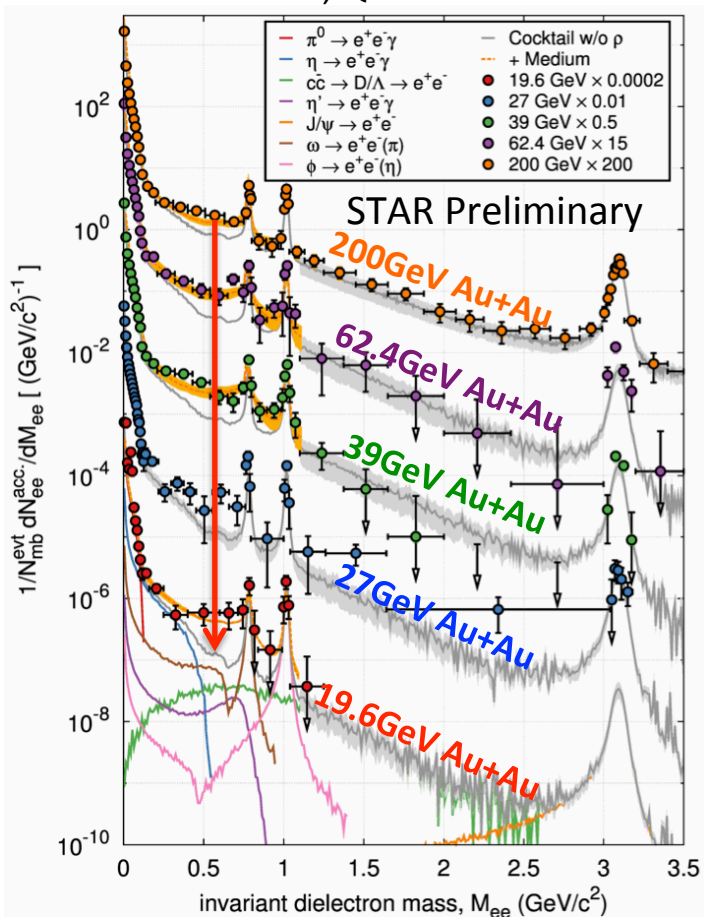


a

Low-mass ee-pair excess

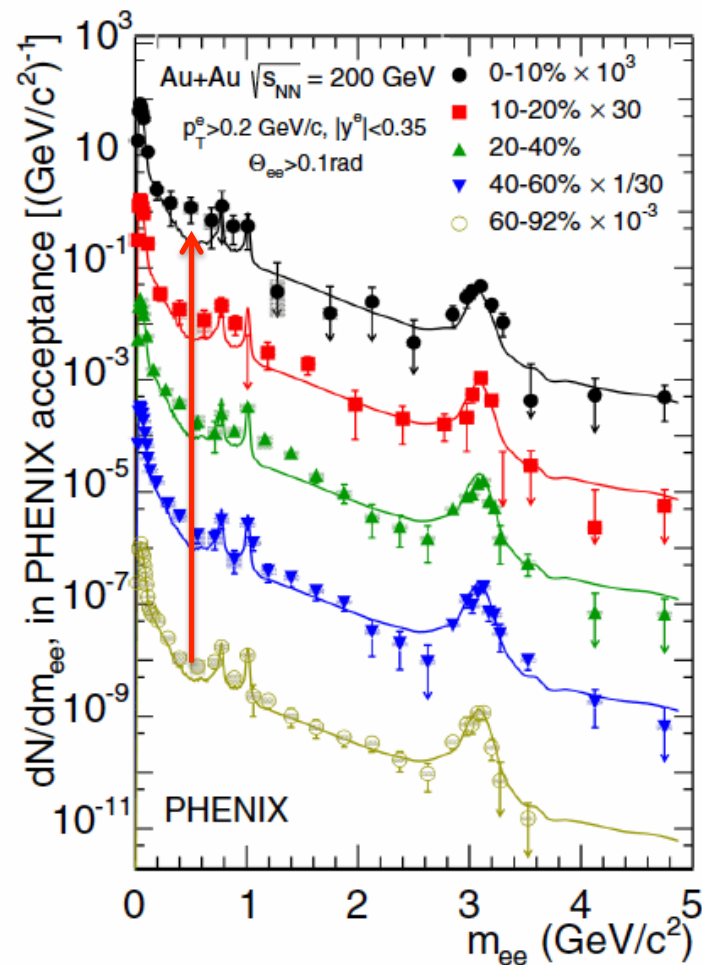
--- ρ shape modification ---
 --- duration time of QGP ---

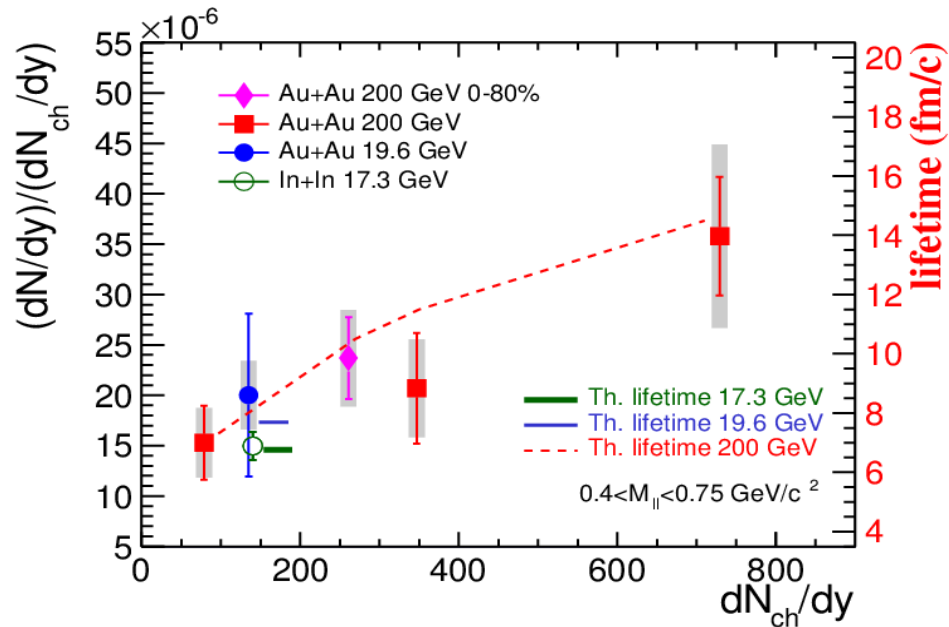
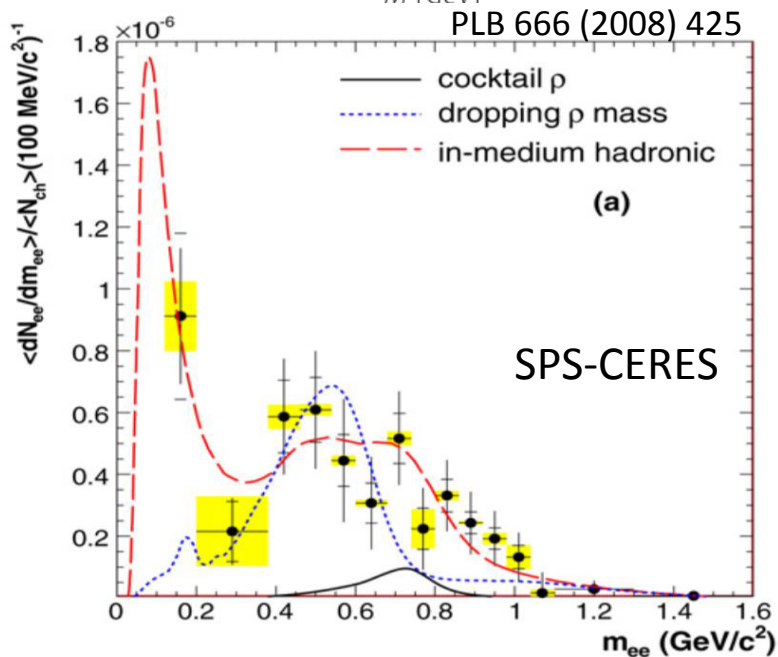
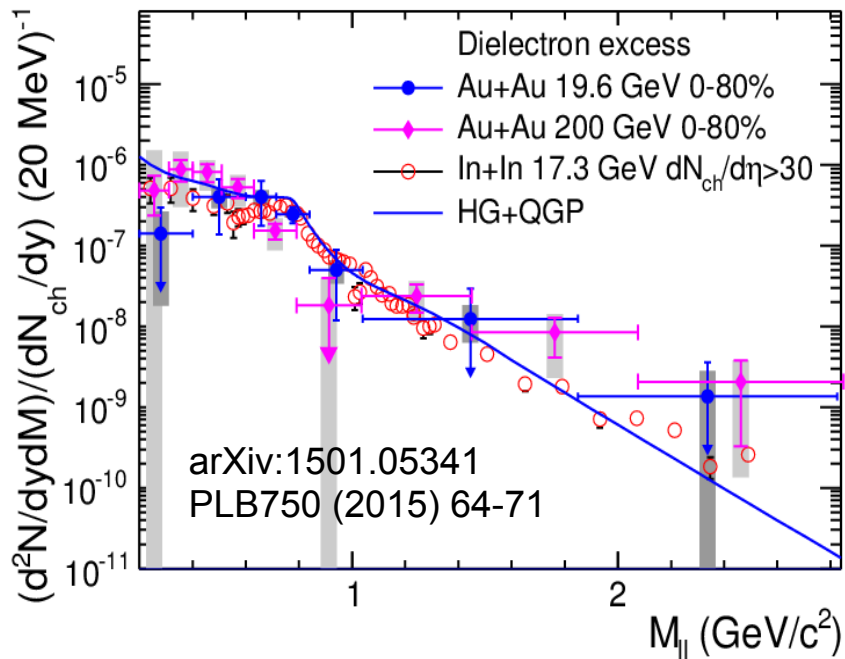
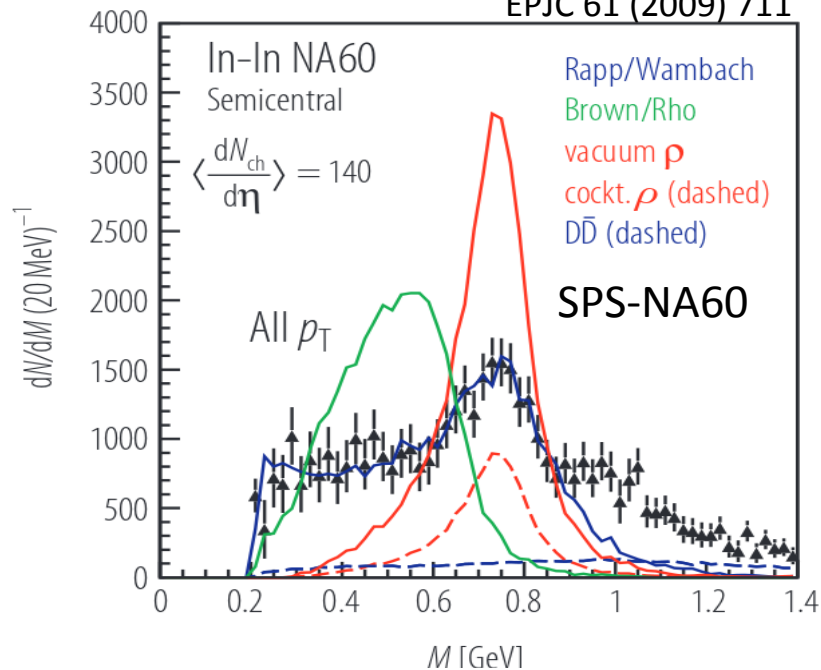
Patrick Huck, QM14



Long standing discrepancy between star and phenix has been resolved with an improved and updated analysis with Hadron Blind Detector (HBD) in phenix : Phys. Rev. C 93 (2016) 014904

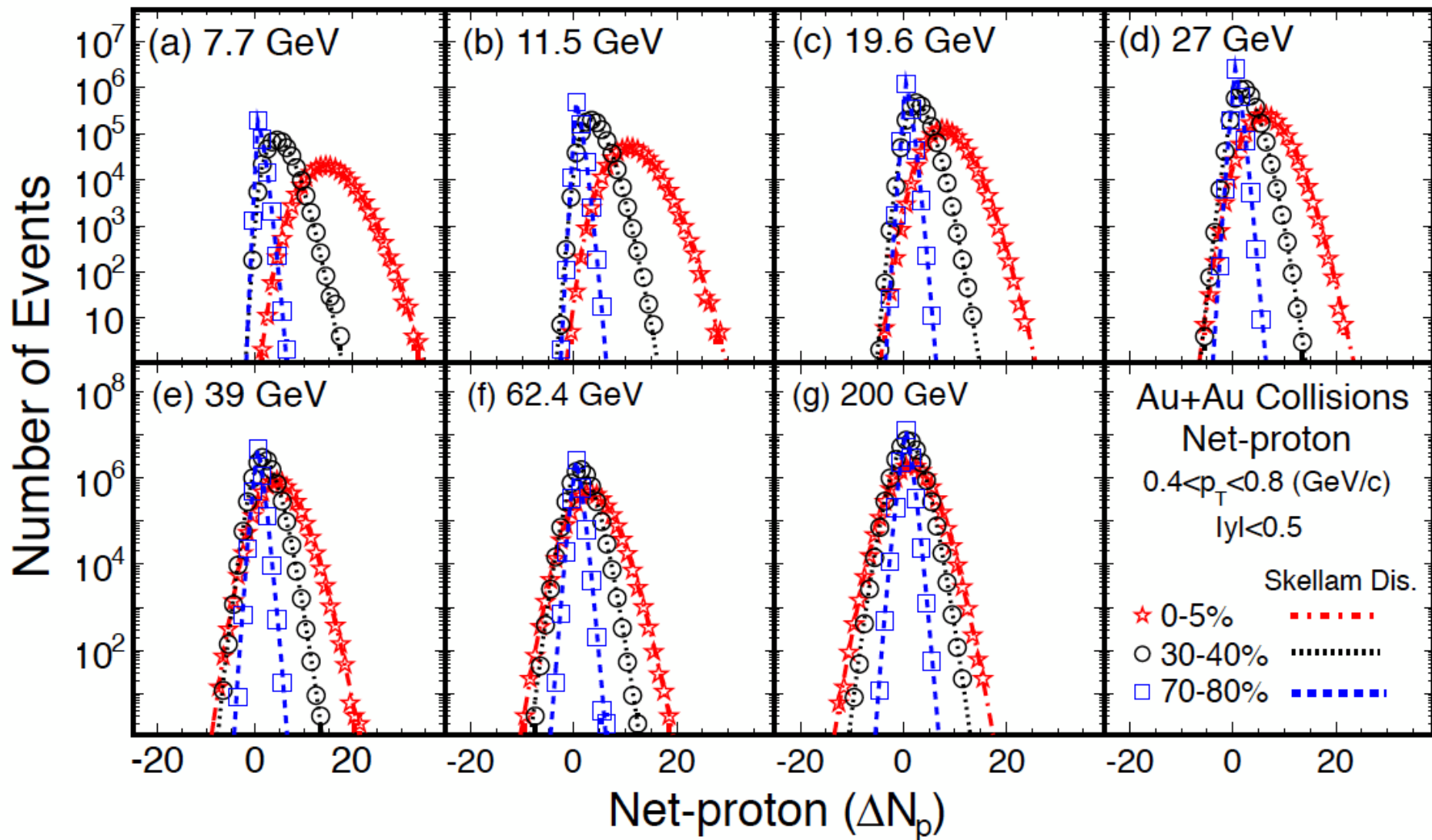
final results for 19.6, 200 Ge and comparison to SPS at Phys. Lett. B 750 (2015) 64





Shape of net-proton distribution

arXiv:1309.5681
Phys.Rev.Lett. 112 (2014) 032302





Observables: Higher Moments (fluctuations)

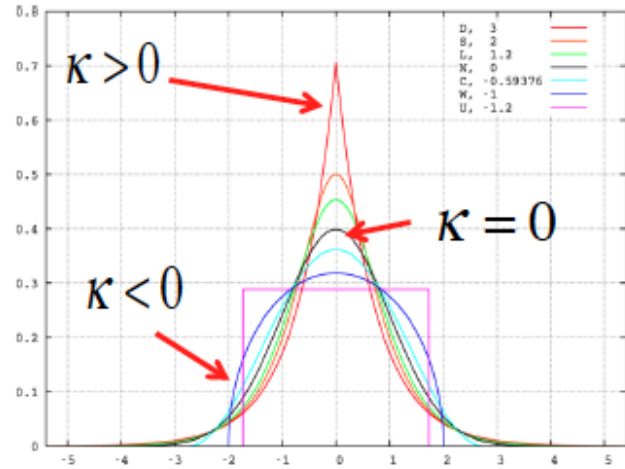
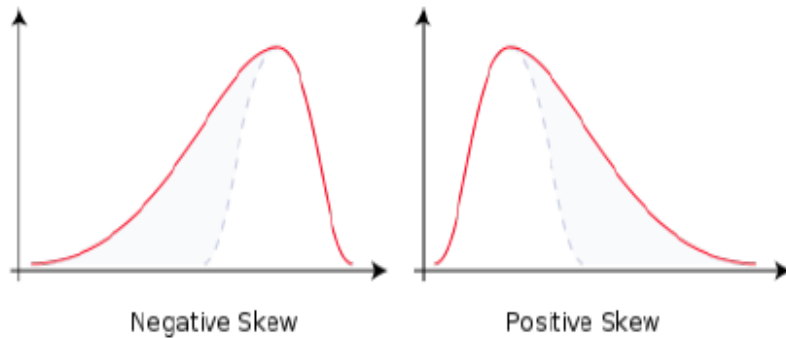
“Shape” of the fluctuations can be measured: non-Gaussian moments.

$$C_{1,x} = \langle x \rangle, C_{2,x} = \langle (\delta x)^2 \rangle,$$

$$C_{3,x} = \langle (\delta x)^3 \rangle, C_{4,x} = \langle (\delta x)^4 \rangle - 3 \langle (\delta x)^2 \rangle^2$$

$$S = \frac{C_{3,N}}{(C_{2,N})^{3/2}} = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$$

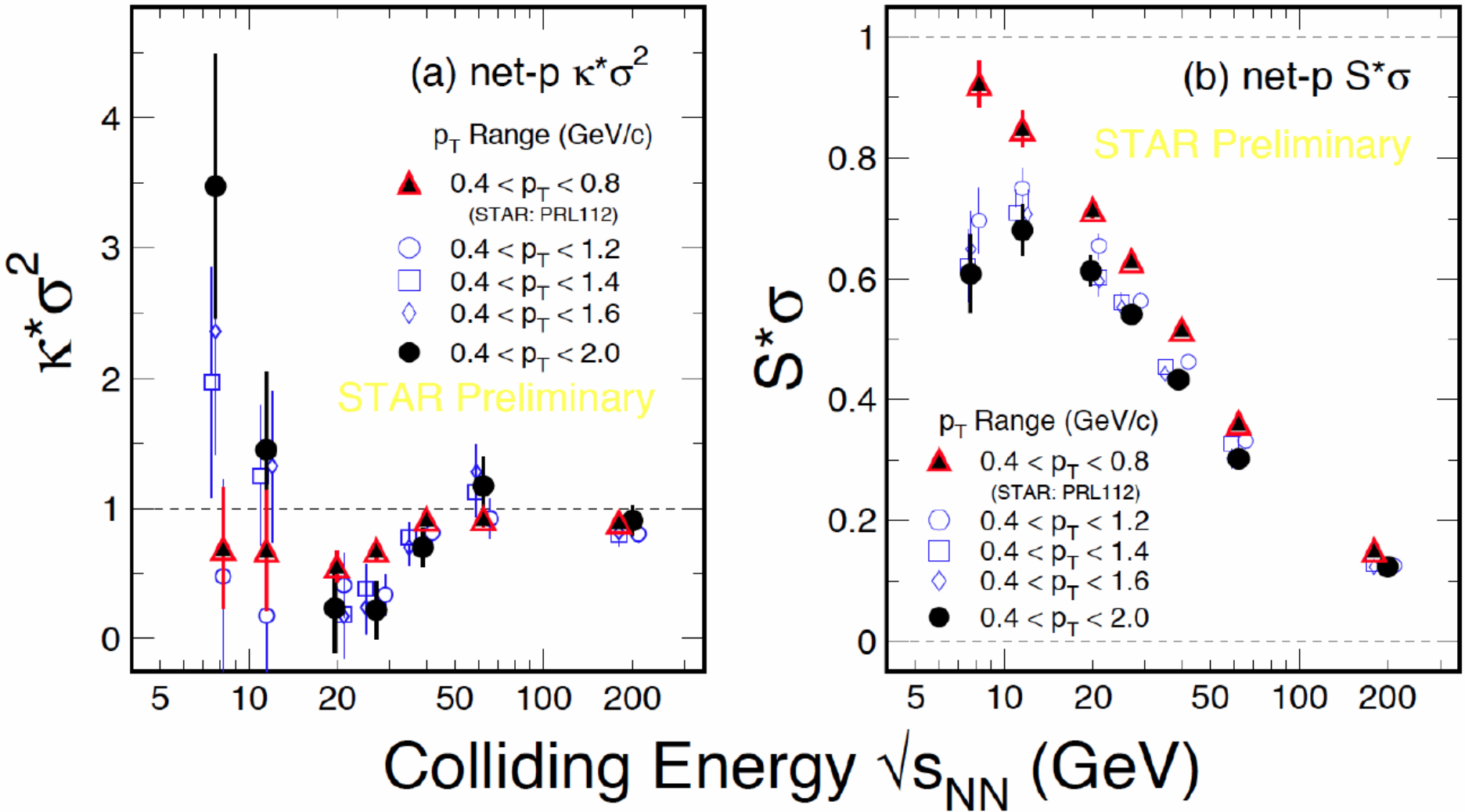
$$\kappa = \frac{C_{4,N}}{(C_{2,N})^2} = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$$

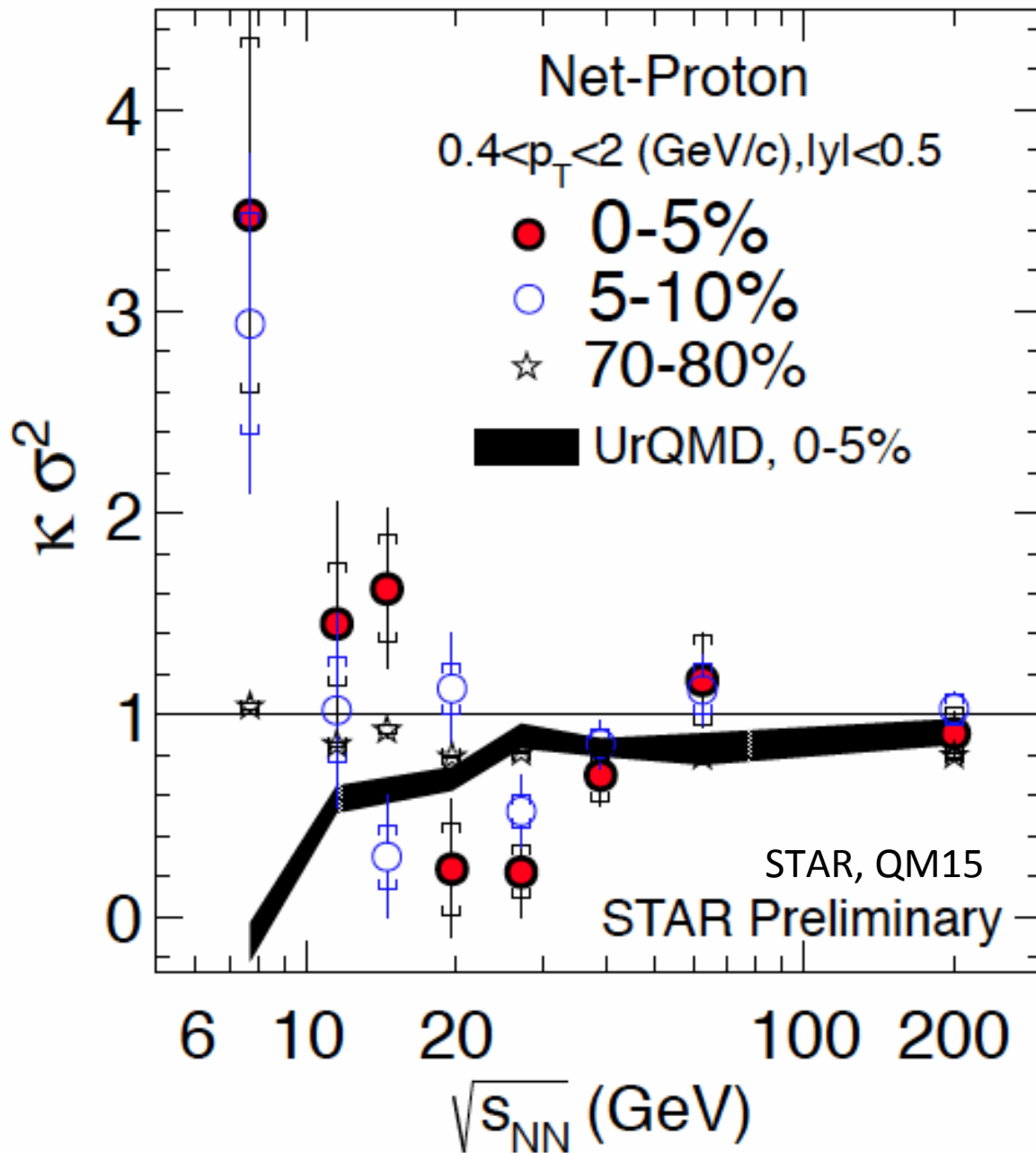


➤ **Susceptibility ratios** \Leftrightarrow **Cumulant Ratios (Cancel V dependence)**

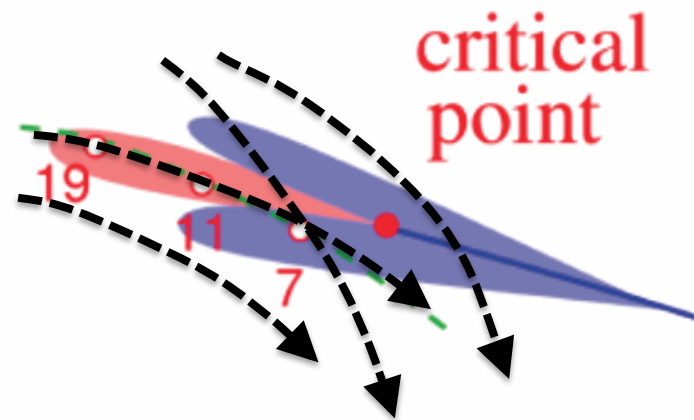
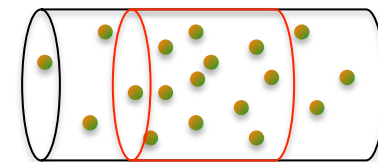
$$\frac{\chi_q^4}{\chi_q^2} = \kappa \sigma^2 = \frac{C_{4,q}}{C_{2,q}}$$

$$\frac{\chi_q^3}{\chi_q^2} = S \sigma = \frac{C_{3,q}}{C_{2,q}}, \quad (q=B, Q, S)$$





Possible critical signature



- large errors : comparable to the critical signal
- need for Beam Energy Scan Phase 2 (2019-)



Higher Order Fluctuations of Conserved Quantities

1. Higher sensitivity to correlation length (ξ) and probe non-gaussian fluctuations near the Critical Point.

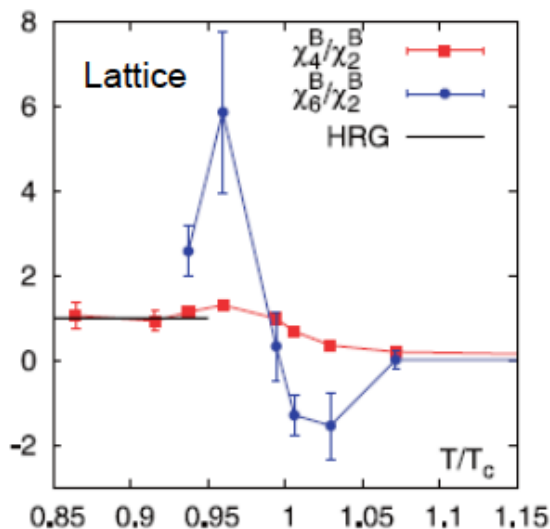
$$\langle (\delta N)^3 \rangle_c \approx \xi^{4.5}, \quad \langle (\delta N)^4 \rangle_c \approx \xi^7$$

M. A. Stephanov, *Phys. Rev. Lett.* 102, 032301 (2009).

M. A. Stephanov, *Phys. Rev. Lett.* 107, 052301 (2011).

M. Asakawa, S. Ejiri and M. Kitazawa, *Phys. Rev. Lett.* 103, 262301 (2009).

2. Direct connection to the susceptibility of the system.



$$\chi_q^{(n)} = \frac{1}{VT^3} \times C_{n,q} = \frac{\partial^n (p/T^4)}{\partial (\mu_q)^n}, q = B, Q, S$$

S. Ejiri et al, *Phys.Lett. B* 633 (2006) 275.

Cheng et al, *PRD* (2009) 074505. B. Friman et al., *EPJC* 71 (2011) 1694.

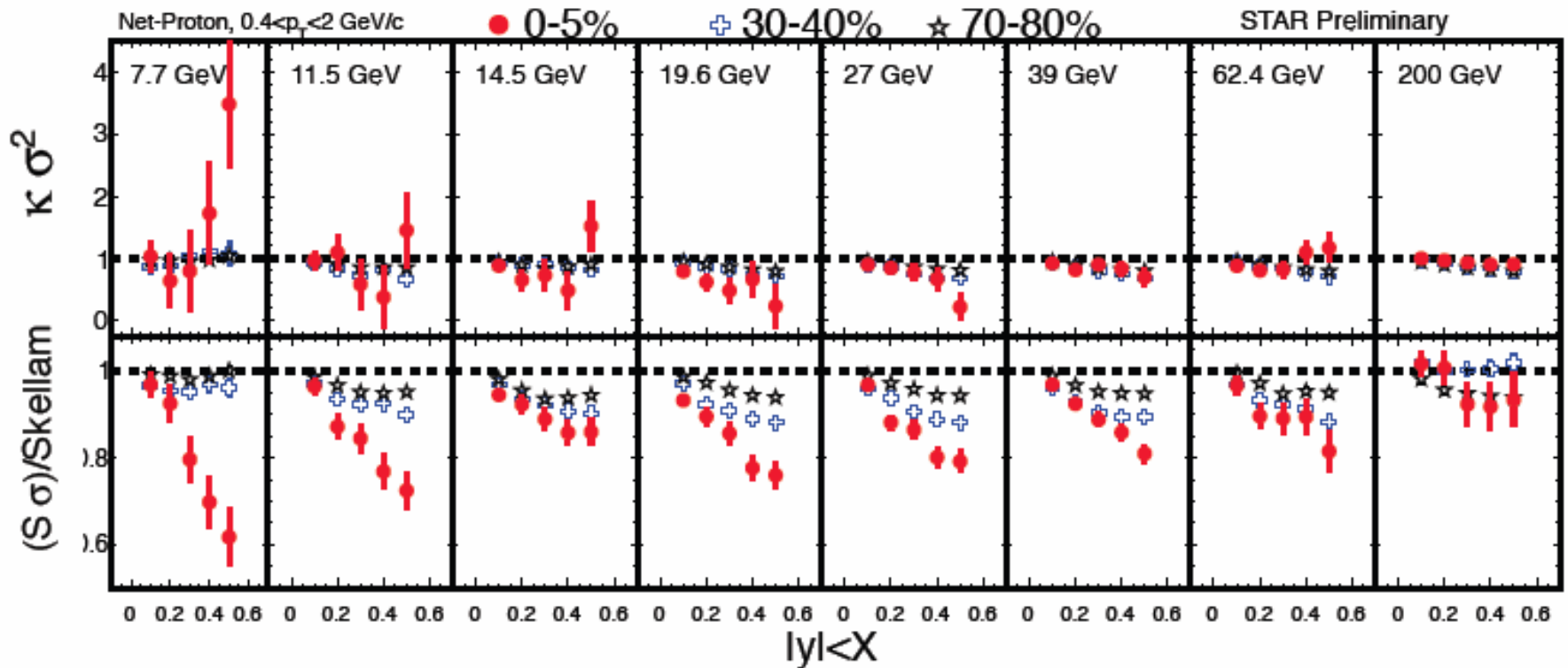
F. Karsch and K. Redlich, *PLB* 695, 136 (2011).

S. Gupta, et al., *Science*, 332, 1525(2012).

A. Bazavov et al., *PRL*109, 192302(12) // S. Borsanyi et al., *PRL*111, 062005(13) // P. Alba et al., *arXiv:1403.4903*



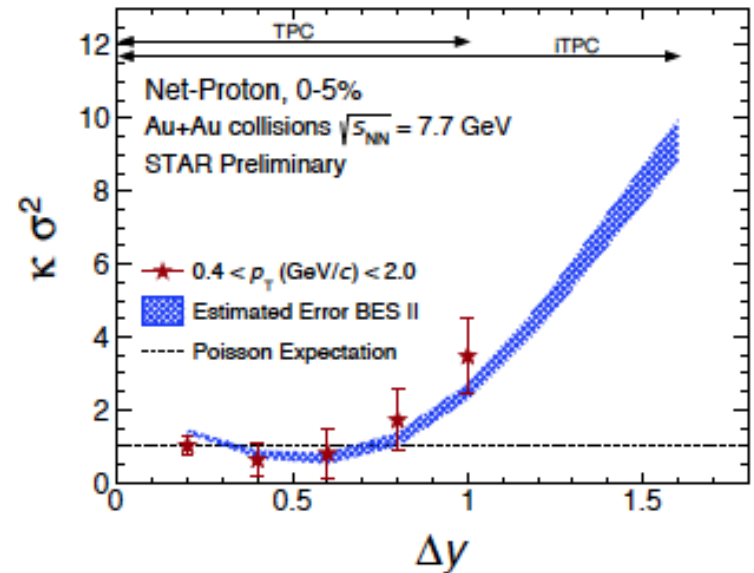
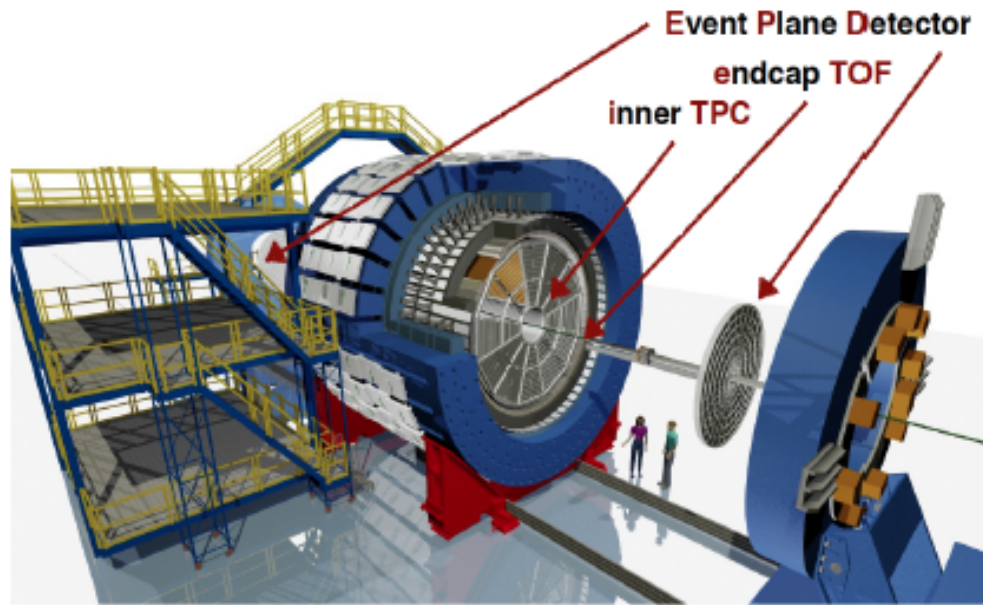
Rapidity Window Dependence



Significant rapidity window dependence are observed.
Large acceptance is crucial for the fluctuation measurement.



STAR Upgrades and BES Phase-II (2019-2020)



iTPC proposal: <http://drupal.star.bnl.gov/STAR/starnotes/public/sn0619>
 BES-II whitepaper: <http://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>

Larger rapidity acceptance crucial for further critical point search with net-protons

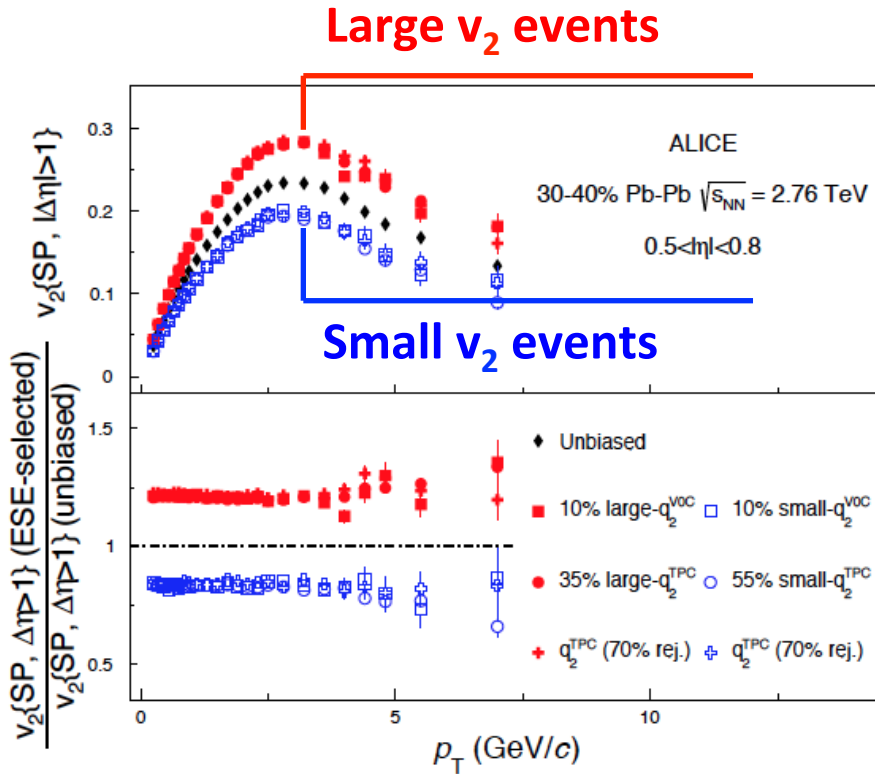
- Electron cooling upgrade will provide increased luminosity ~ 3 -10 times.
- Inner TPC(iTPC) upgrade : $|\eta| < 1$ to $|\eta| < 1.5$. Better dE/dx resolution.
- Forward Event Plane Detector (EPD): Centrality and Event Plane Determination. $1.8 < |\eta| < 4.5$

End Cap MRPC-TOF from Fair-CBM (fixed target and coll. modes)

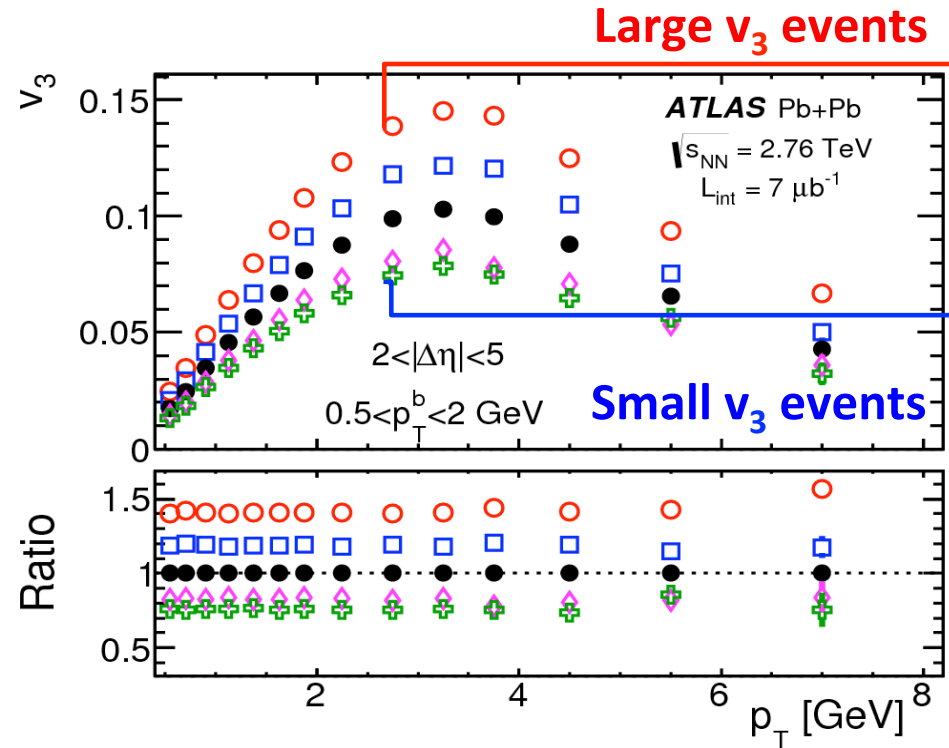
2nd half starts here, on flow and correlation studies including small systems...

Event Shape Engineering (ESE), Event Shape Selection

--- for a given centrality ---



PRC93 (2016) 034916



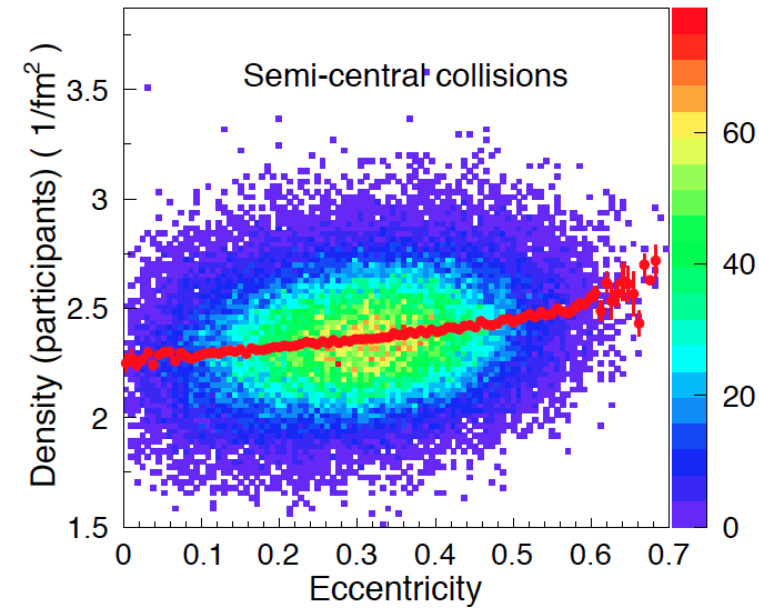
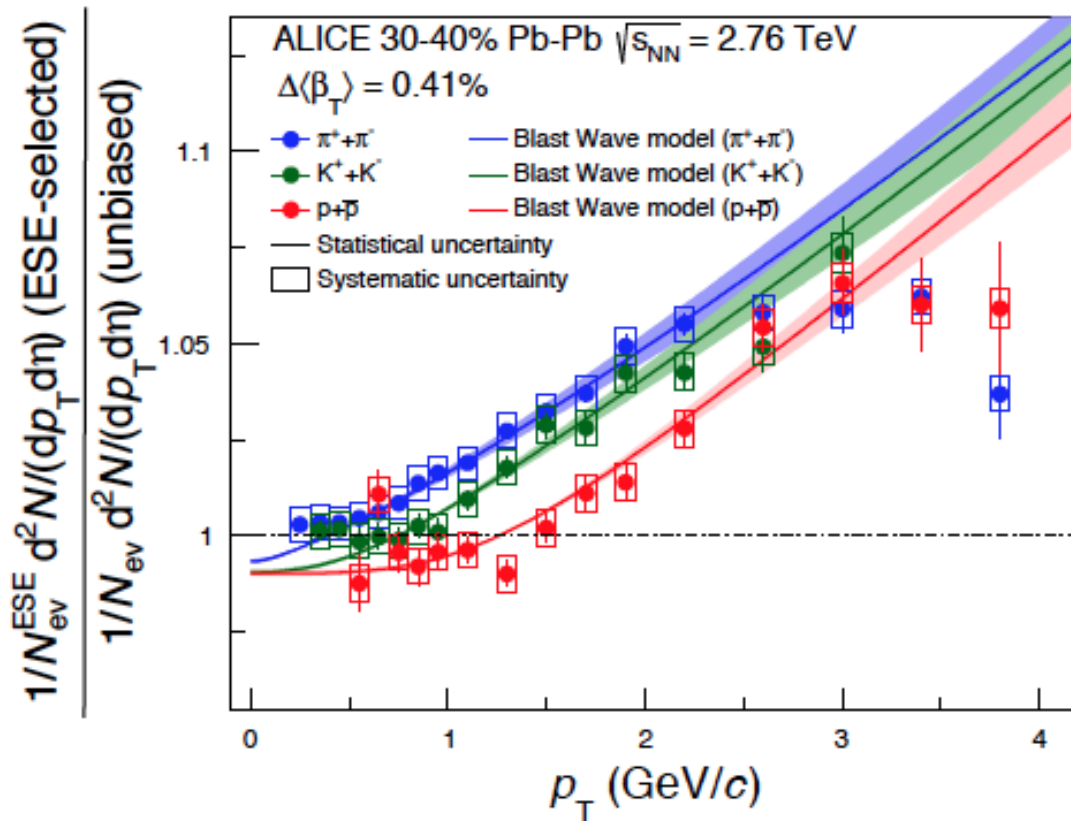
PRC92 (2015) 034903

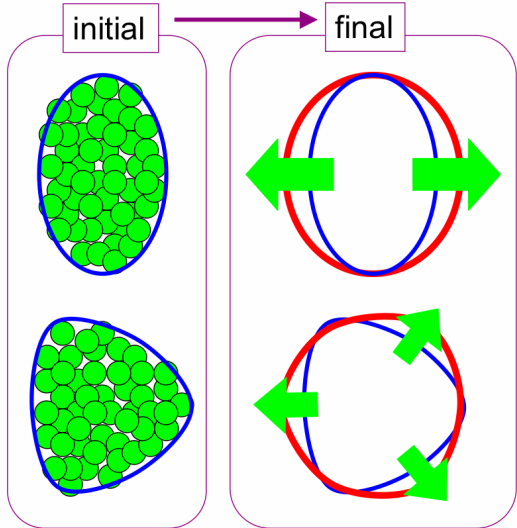
flat p_T dependence -> indicative for an initial geometry

Applications of ESE

- correlation between radial (β_T) and elliptic (v_2) flows
- correlation between HBT eccentricity ($\varepsilon_2^{\text{final}}$) and v_2
- correlation between di-jet w.r.t. Φ_2 and v_2

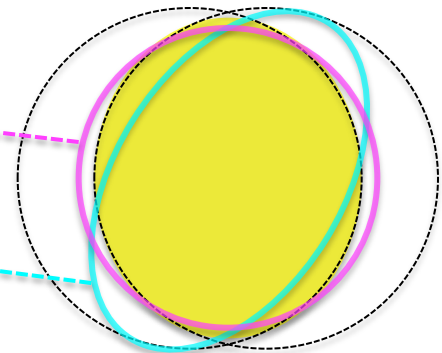
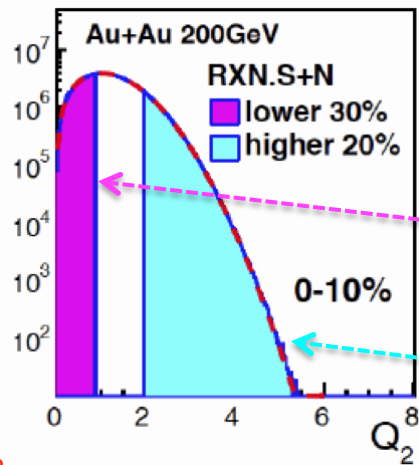
PRC93 (2016) 034916



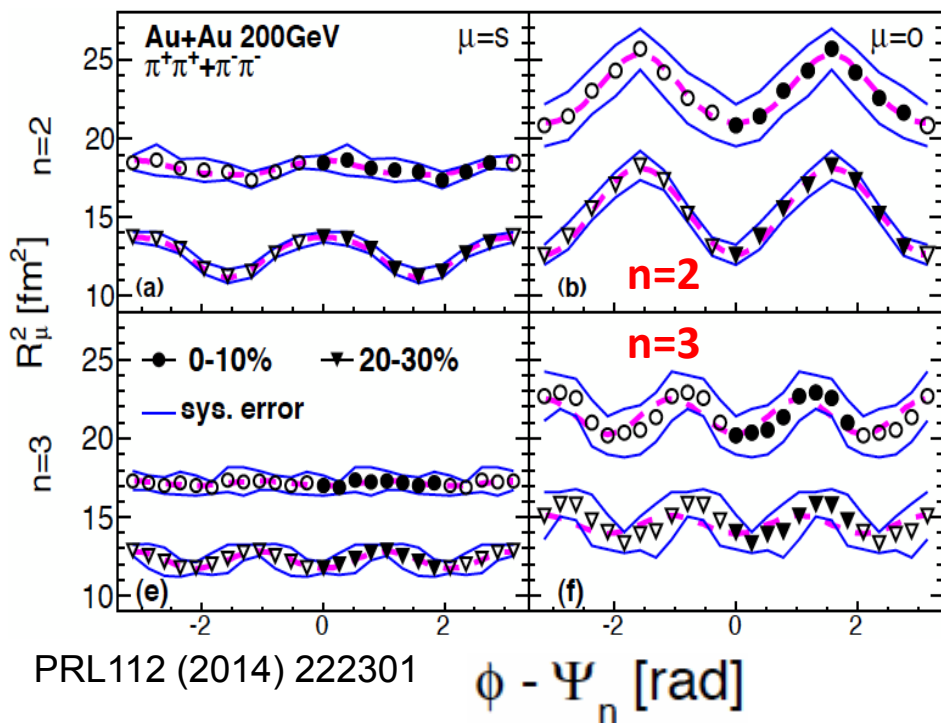


ESE application to HBT

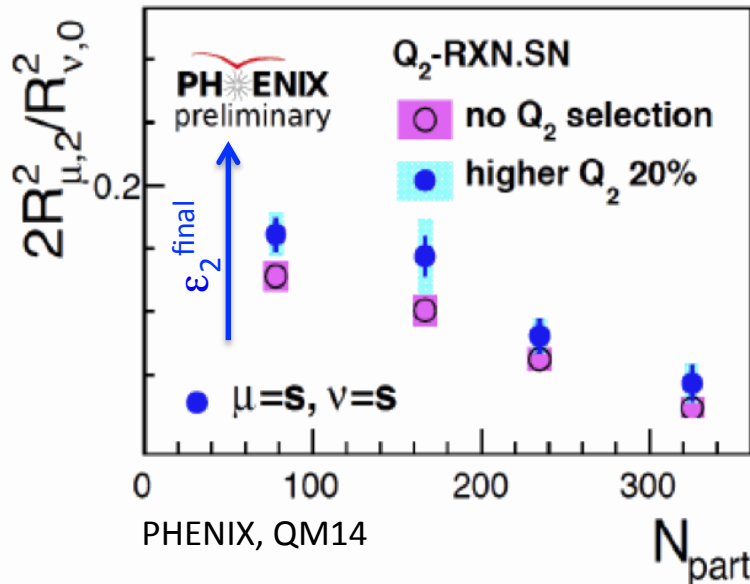
$$\text{relation : } \varepsilon_2^{\text{initial}} - v_2 - \varepsilon_2^{\text{final}}$$



Elliptic and Triangular shape : $R^{\text{HBT}}_{\phi_2}$, $R^{\text{HBT}}_{\phi_3}$



$\varepsilon_{\text{final}}$ via HBT interferometry

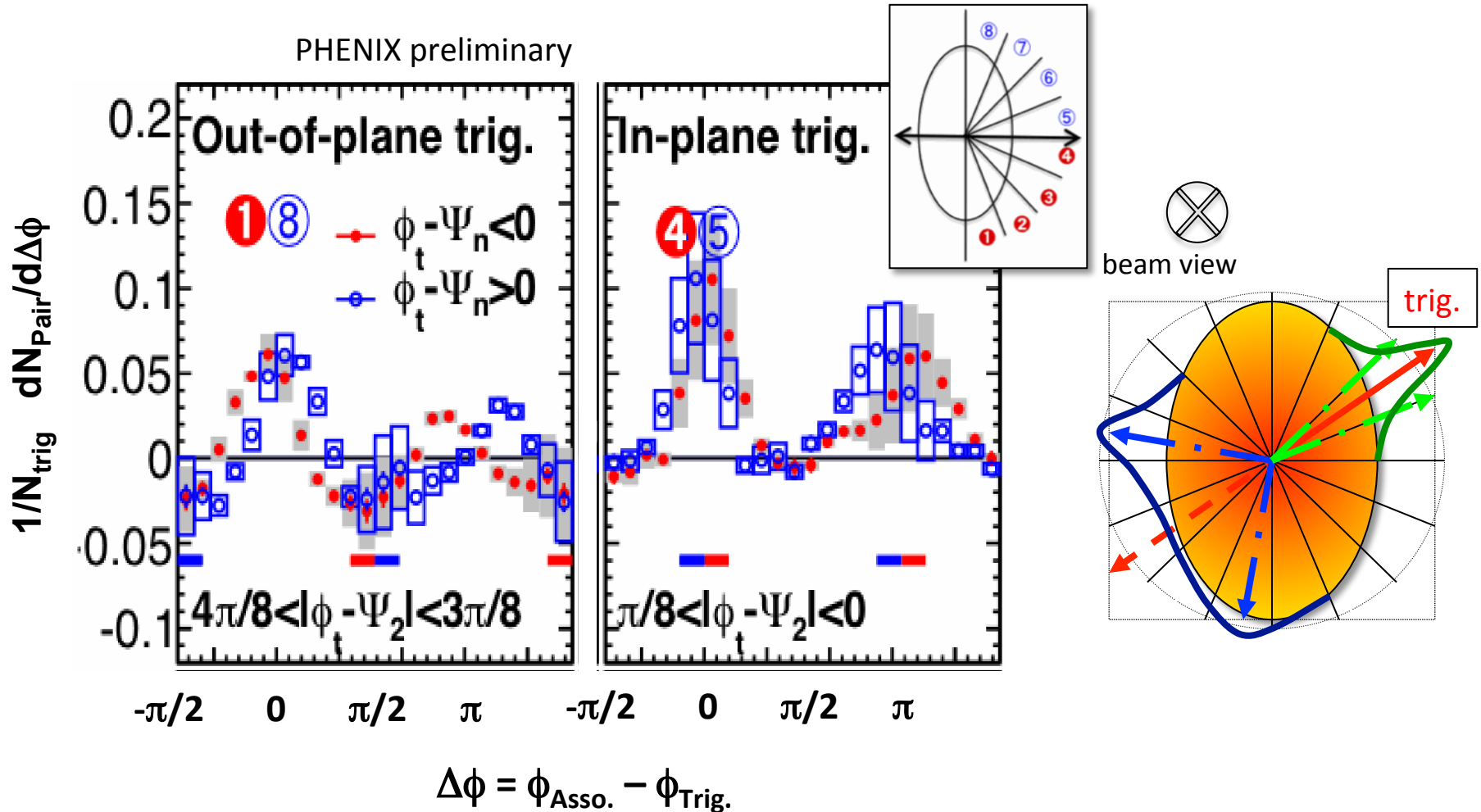


PRL112 (2014) 222301

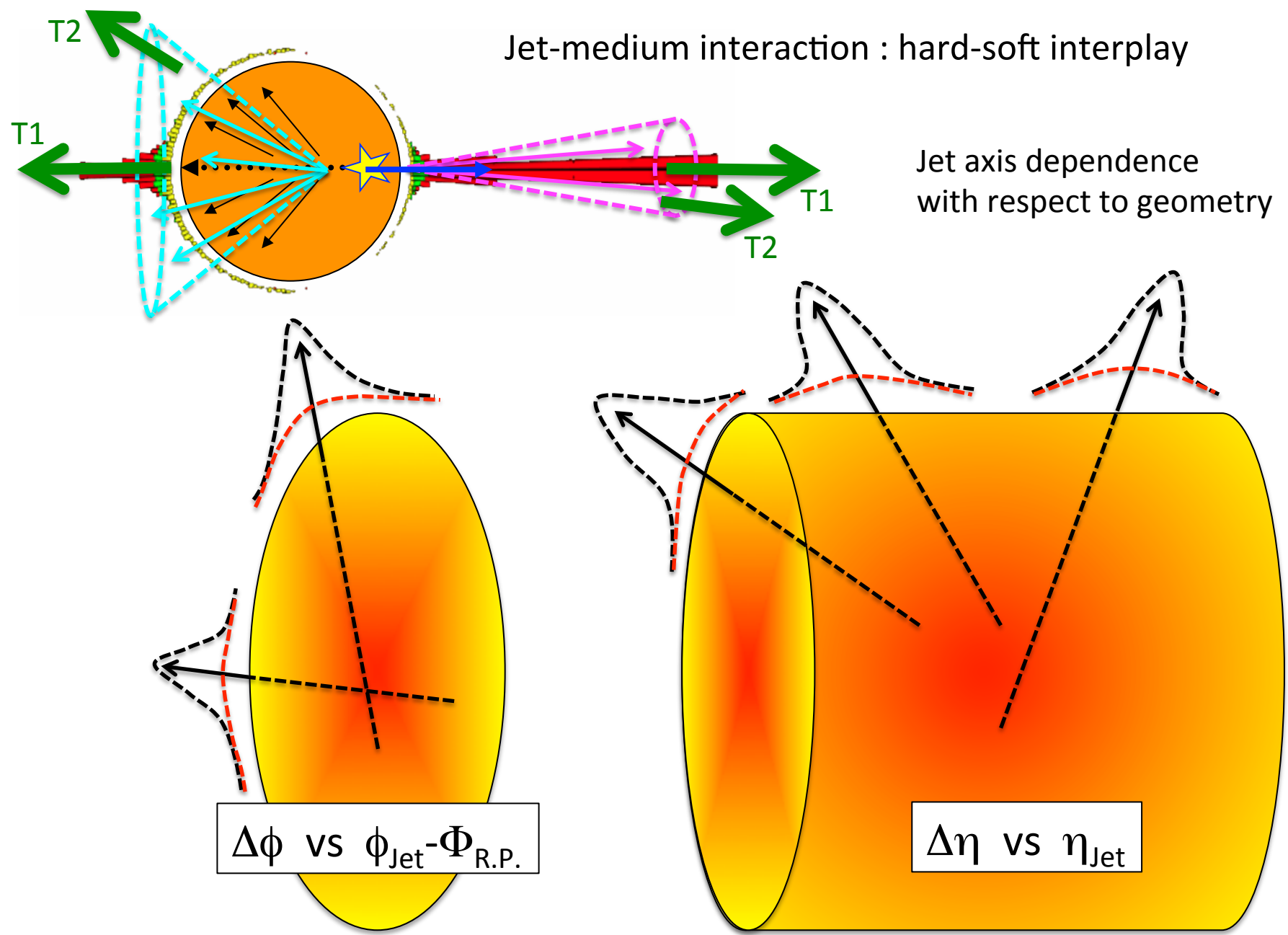
$\phi - \Psi_n$ [rad]

Possible application (on going) of ESE

Shape and flow relation to the jet modification



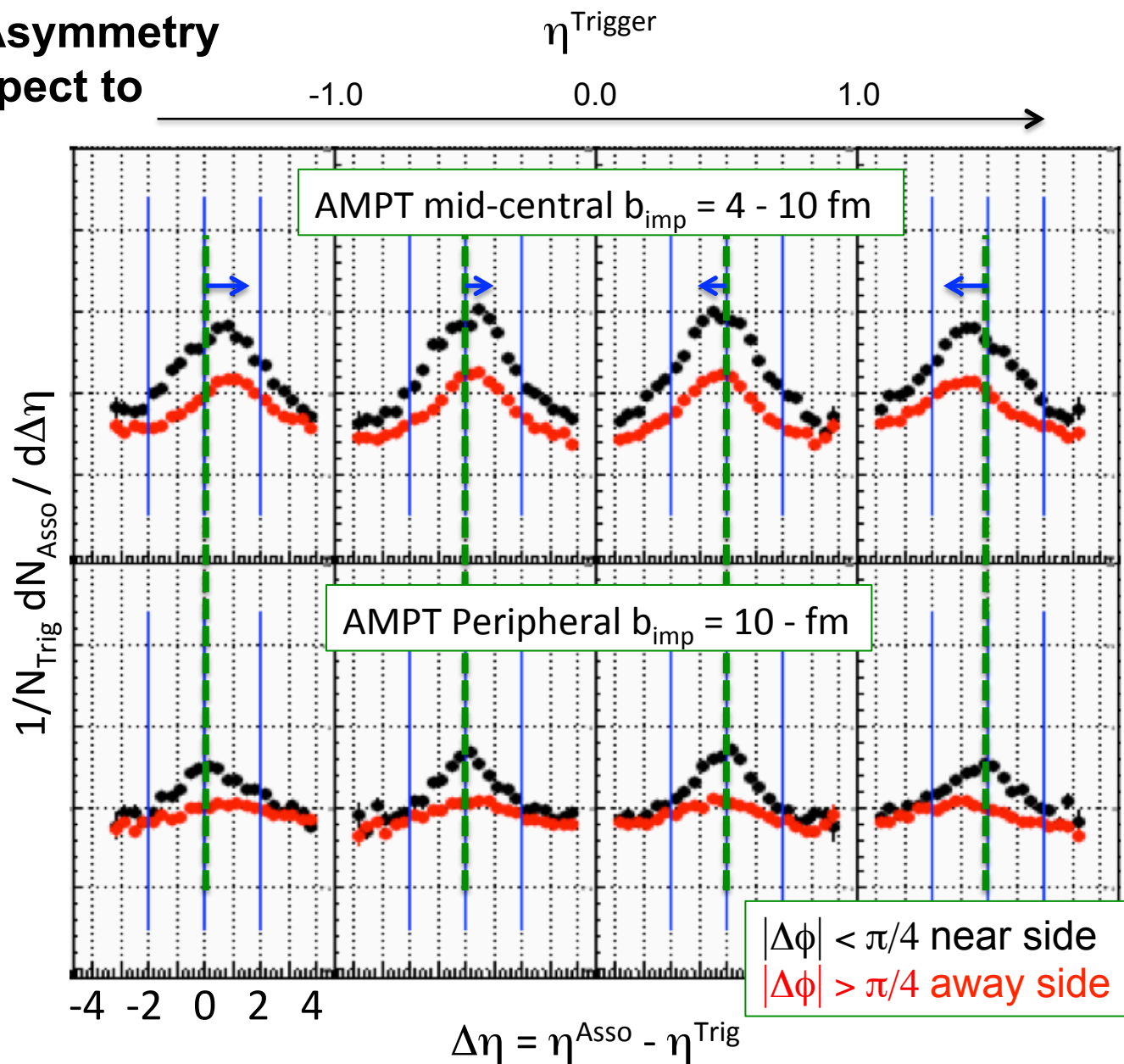
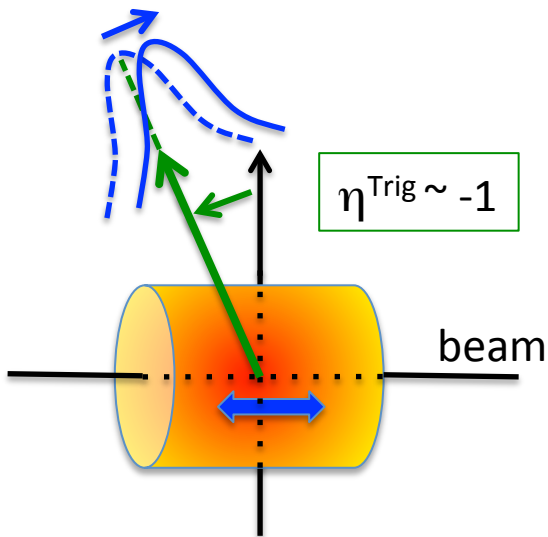
Jet-medium interaction : hard-soft interplay

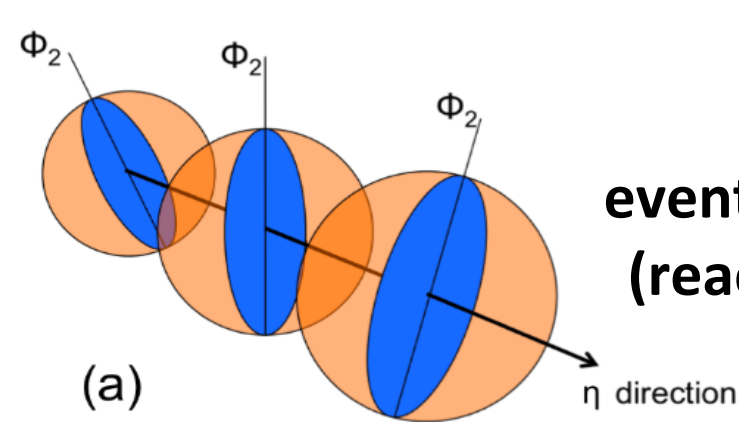


Forward-Backward Asymmetry in $\Delta\eta$ Shape with respect to Trigger η

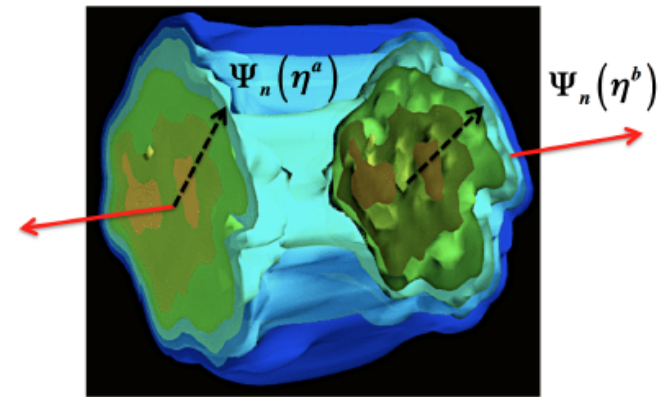
(associate yield per trigger with AMPT simulation)

Forward-backward asymmetry is visible in AMPT simulation. Near side $\Delta\eta$ peak is backward shifted w.r.t. trigger η direction.



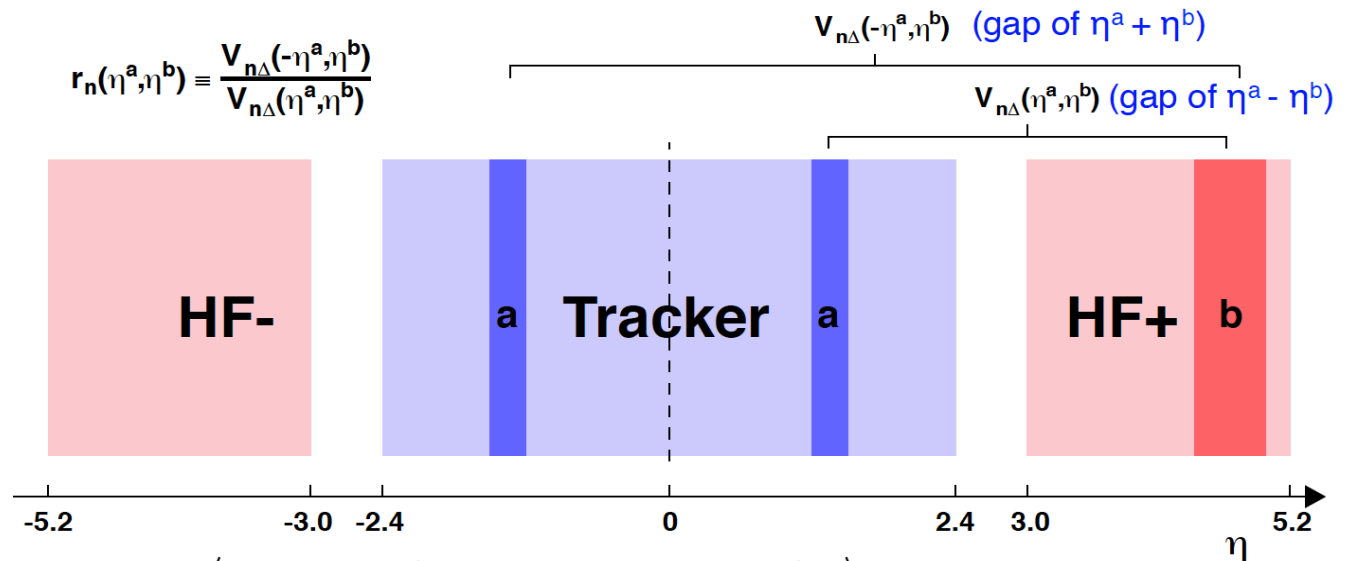


η dependent event plane fluctuation (reaction plane twist)



$$v_{n\Delta}(\eta^a, \eta^b) = \langle v_n(\eta^a)v_n(\eta^b) \rangle \longrightarrow v_{n\Delta}(\eta^a, \eta^b) = \langle v_n(\eta^a)v_n(\eta^b) \cos(n\Psi_n(\eta^a) - n\Psi_n(\eta^b)) \rangle$$

$$r_n(\eta^a, \eta^b) = \frac{V_{n\Delta}(-\eta^a, \eta^b)}{V_{n\Delta}(\eta^a, \eta^b)}$$

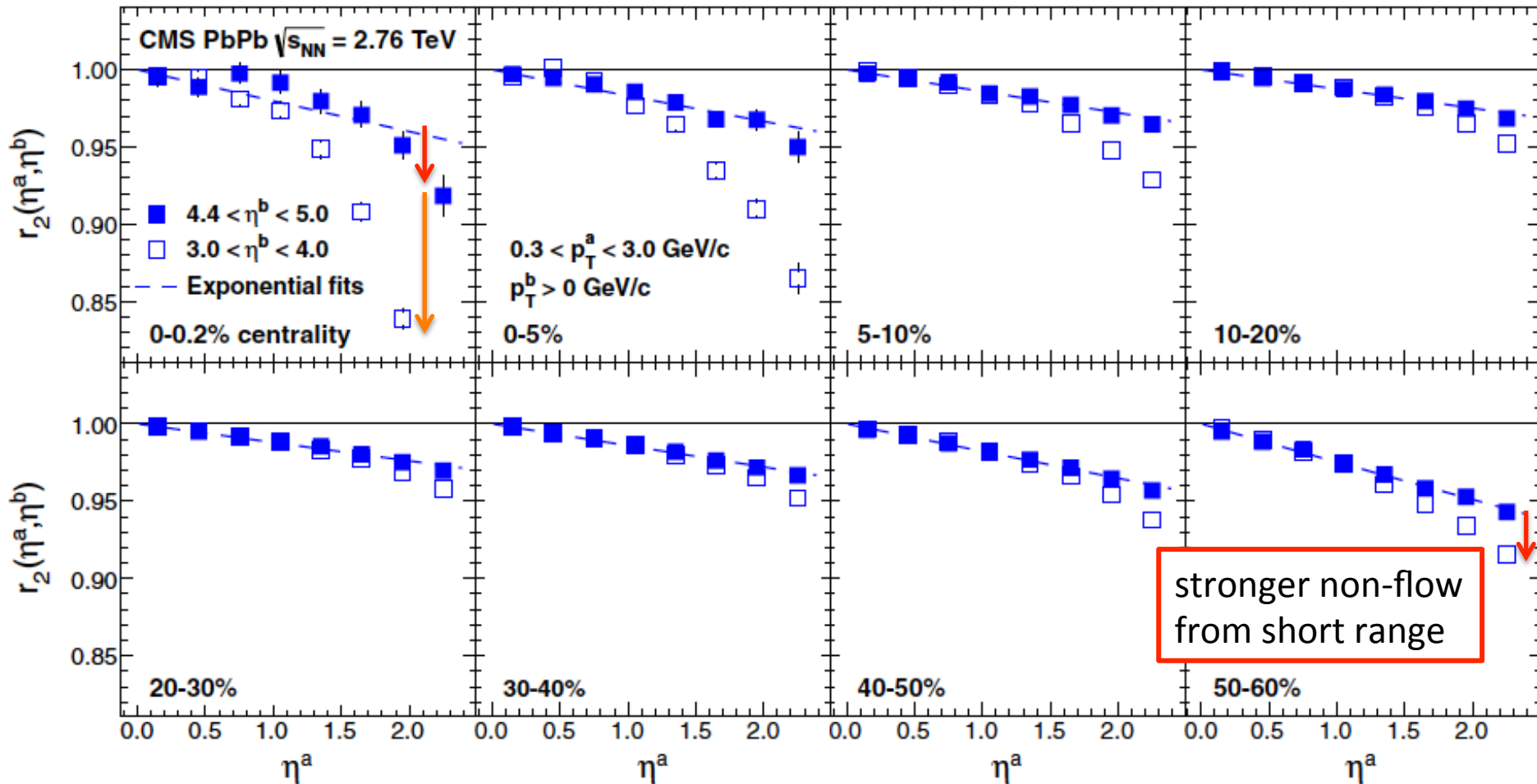


$$r_n(\eta^a, \eta^b) = \frac{\langle v_n(-\eta^a)v_n(\eta^b) \cos[n(\Psi_n(-\eta^a) - \Psi_n(\eta^b))] \rangle}{\langle v_n(\eta^a)v_n(\eta^b) \cos[n(\Psi_n(\eta^a) - \Psi_n(\eta^b))] \rangle} \sim \langle \cos[n(\Psi_n(\eta^a) - \Psi_n(-\eta^a))] \rangle$$

CMS, QM15

Stronger de-correlation of E.P. with η -gap

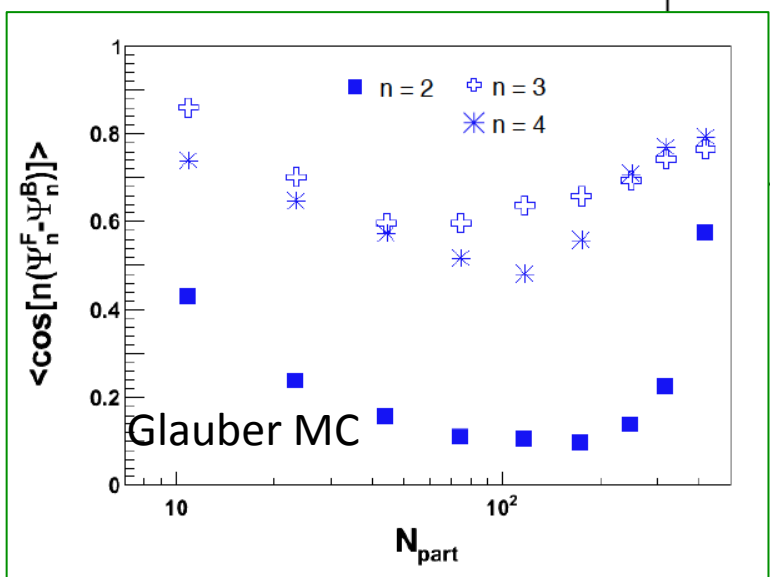
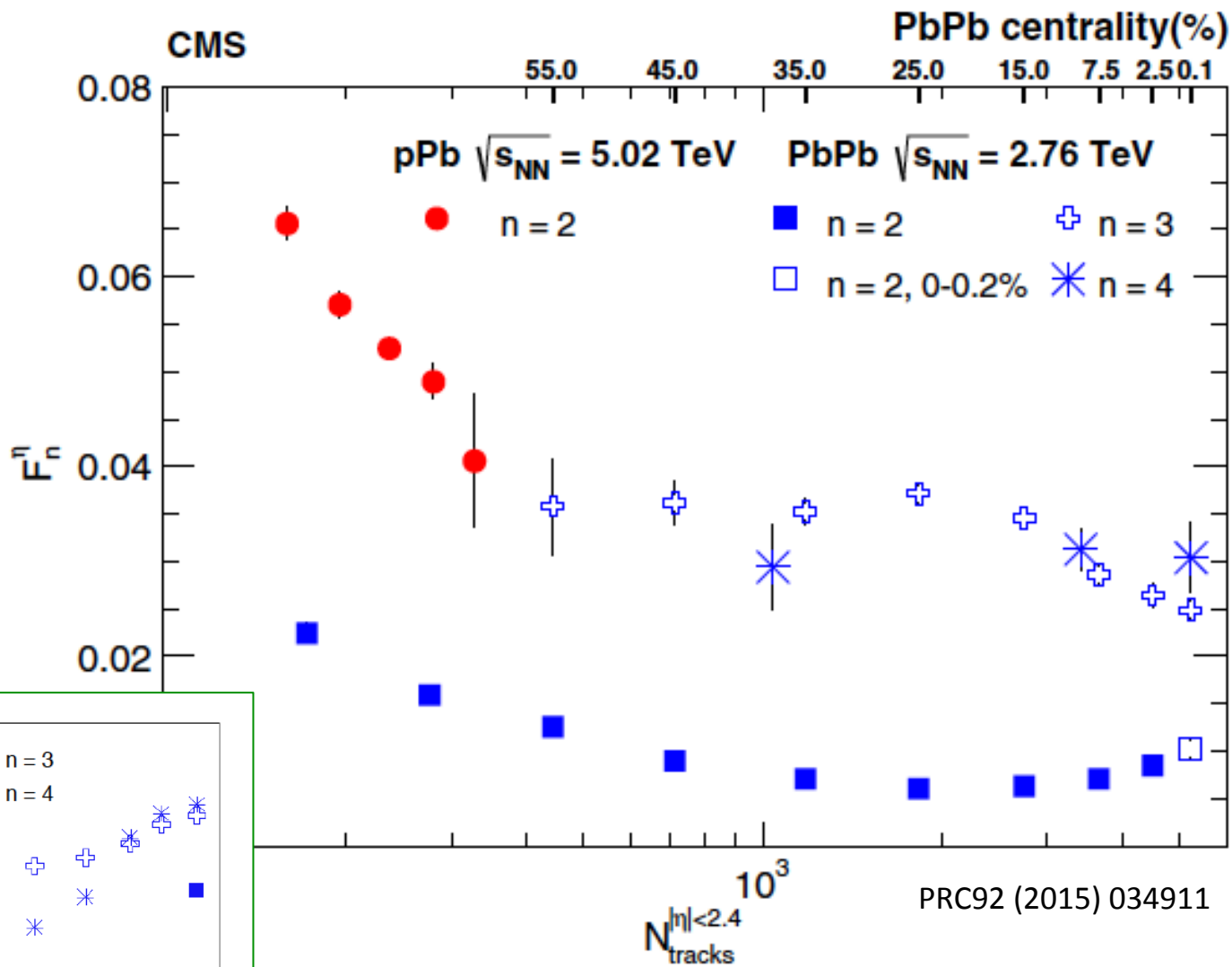
PRC92 (2015) 034911



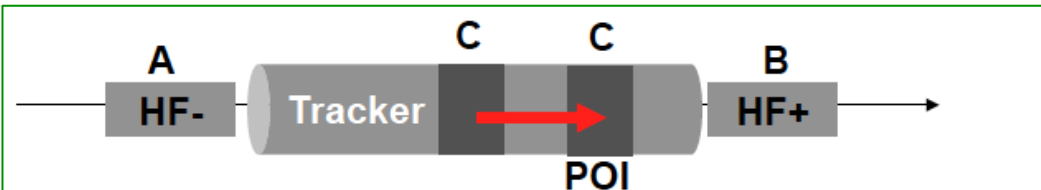
$$r_n(\eta^a, \eta^b) = e^{-2F_n^\eta \eta^a} \sim 1 - 2F_n^\eta \eta^a$$

extract : F_n^η

Extracted F_n^η Parameter



η dependence of v_n or de-correlation of E.P.



POI :
particle of interest

➤ Decorrelation effects [arXiv:1503.01692]

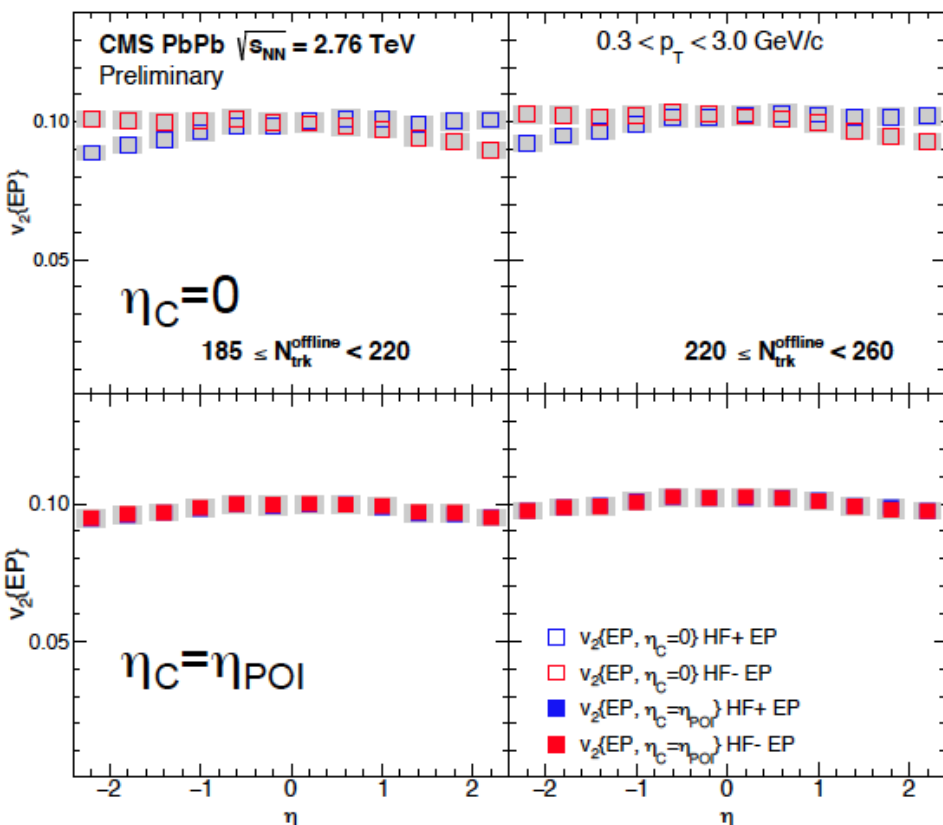
$$\cos\left[2\left\{\Psi_n(\eta_1) - \Psi_n(\eta_2)\right\}\right] = e^{-F_n^\eta |\eta_1 - \eta_2|}$$

2-par correlation 3-sub method gives v_n at A/B, or look at resolution of A/B, that would vary with C location...

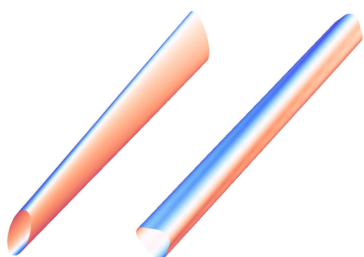


$$R_A(\eta_{POI}) = \sqrt{\frac{\langle \cos[n(\Psi_n^A - \Psi_n^B)] \rangle \langle \cos[n(\Psi_n^A - \Psi_n^C)] \rangle}{\langle \cos[n(\Psi_n^B - \Psi_n^C)] \rangle}} \quad (\eta_C = \eta_{POI})$$

Pb+Pb



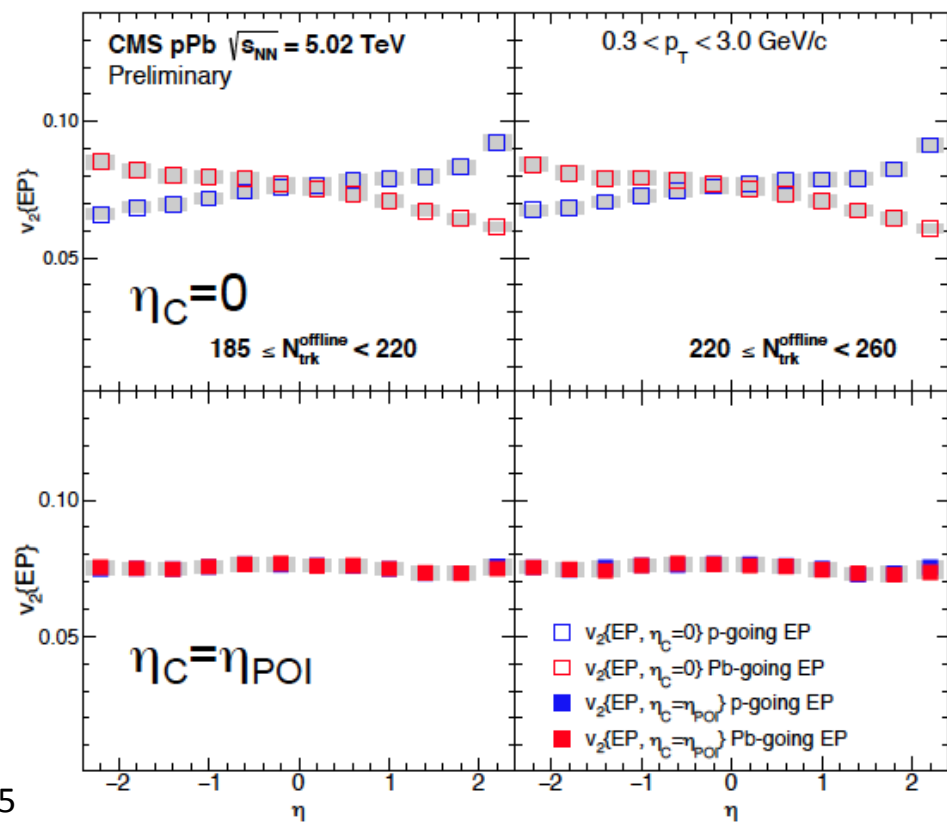
Torqued fireball



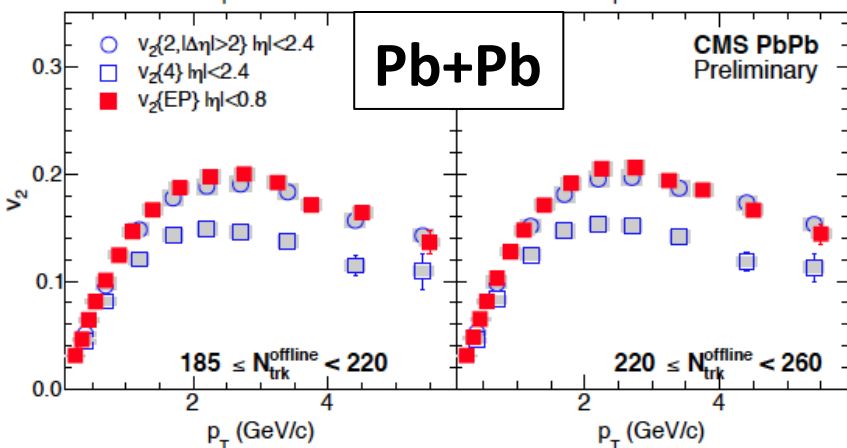
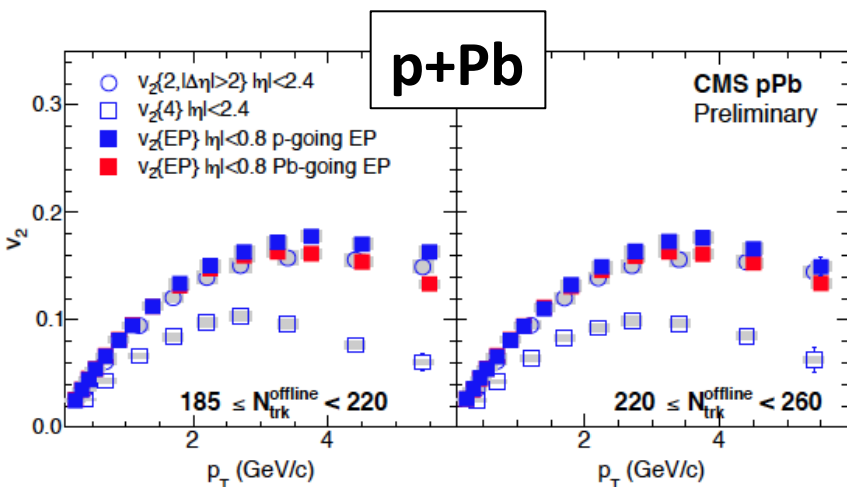
Bozek et.al., arXiv:1011.3354

CMS, QM15

p+Pb



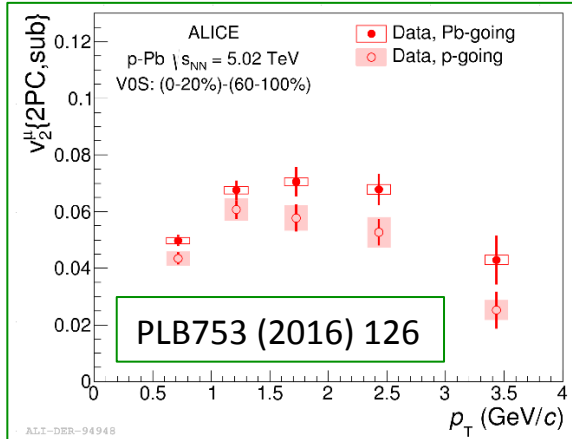
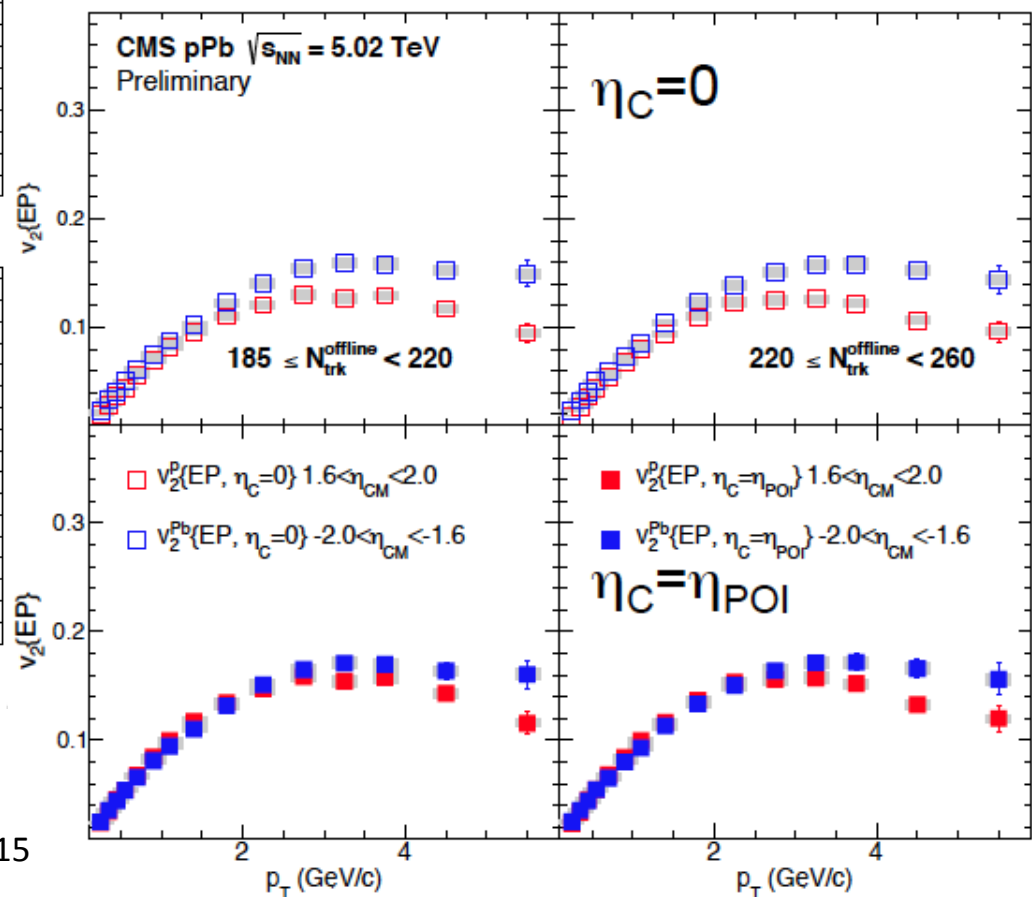
$v_2(|\eta|<0.8)$

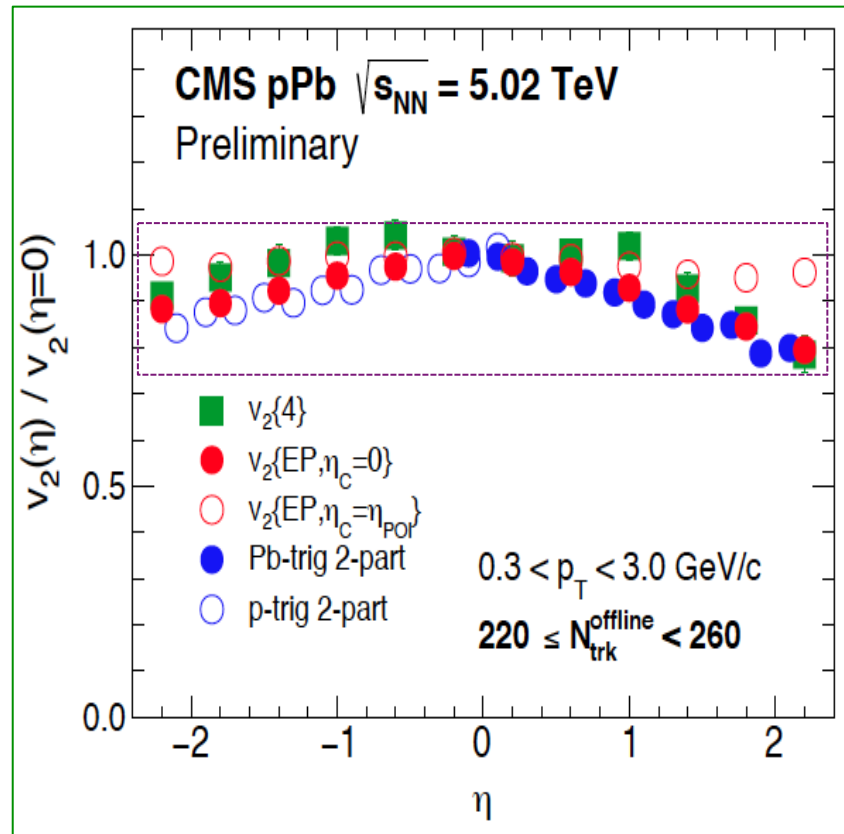
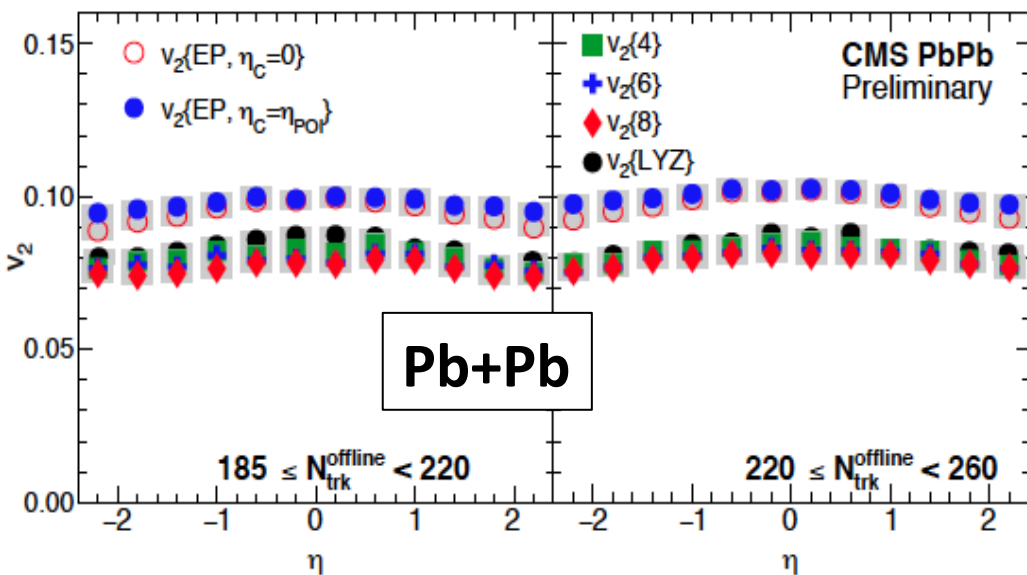
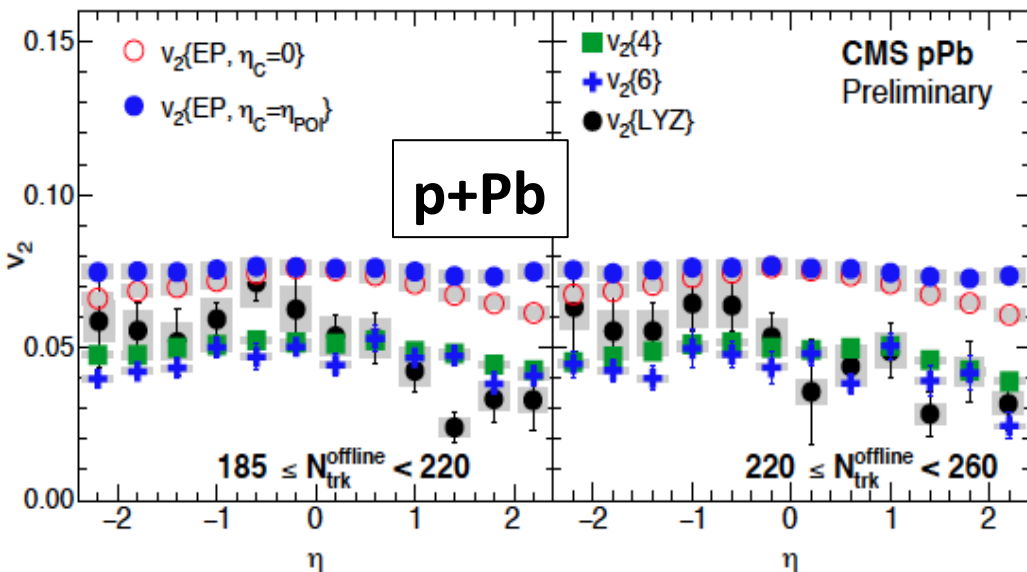


CMS, QM15

p+Pb

$v_2(1.6<|\eta|<2.0)$



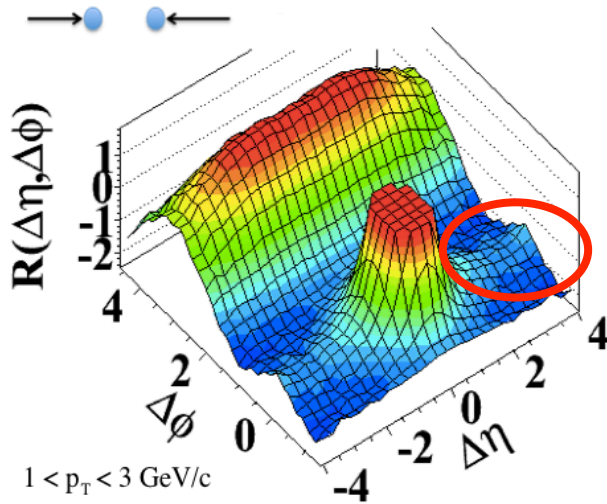


η dependence of v_2

CMS, QM15

Ridge/ v_n (collective expansion?) in $pp^{(\text{high mult.})}$, pA, AA at LHC

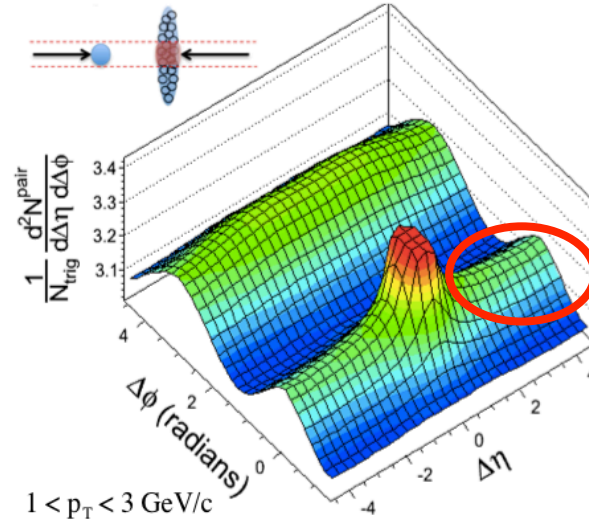
(a) $pp \sqrt{s} = 7 \text{ TeV}, N_{\text{trk}}^{\text{offline}} \geq 110$



$1 < p_T < 3 \text{ GeV}/c$

JHEP 09 (2010) 091

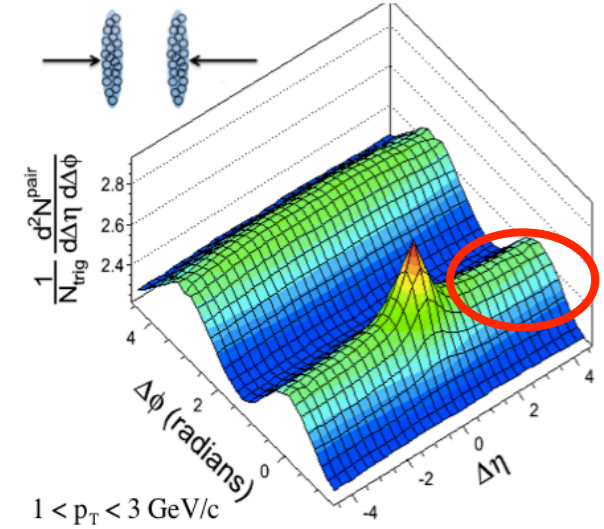
(b) $pPb \sqrt{s_{NN}} = 5.02 \text{ TeV}, 220 < N_{\text{trk}}^{\text{offline}} \leq 260$



$1 < p_T < 3 \text{ GeV}/c$

PLB 724 (2013) 213

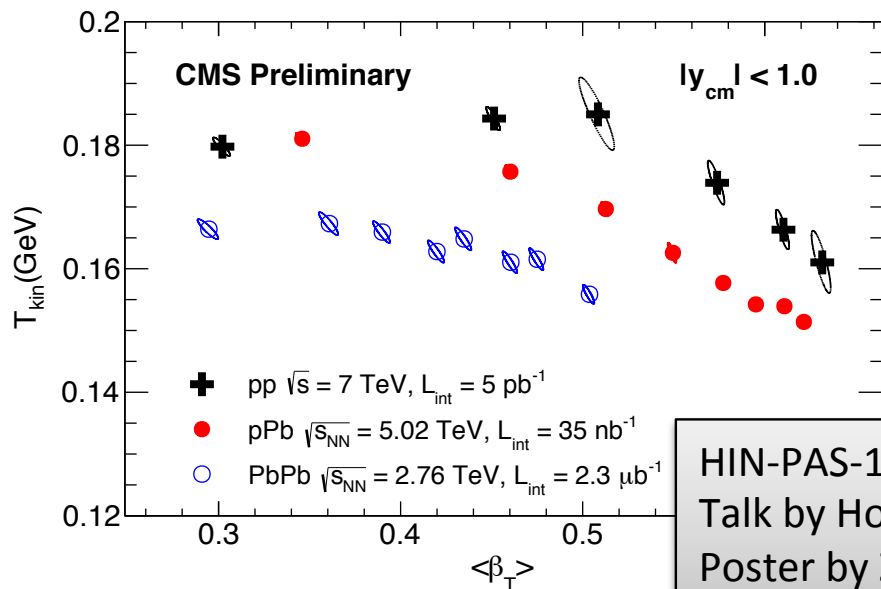
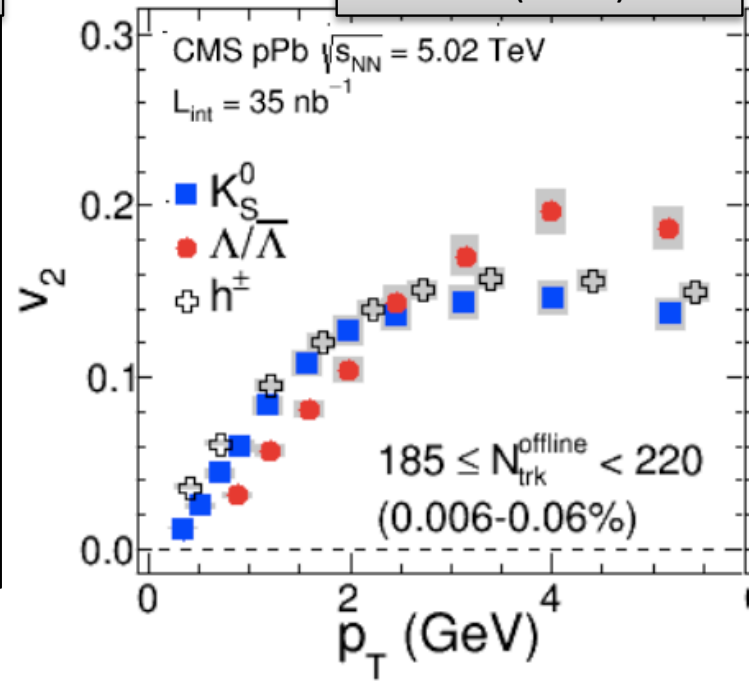
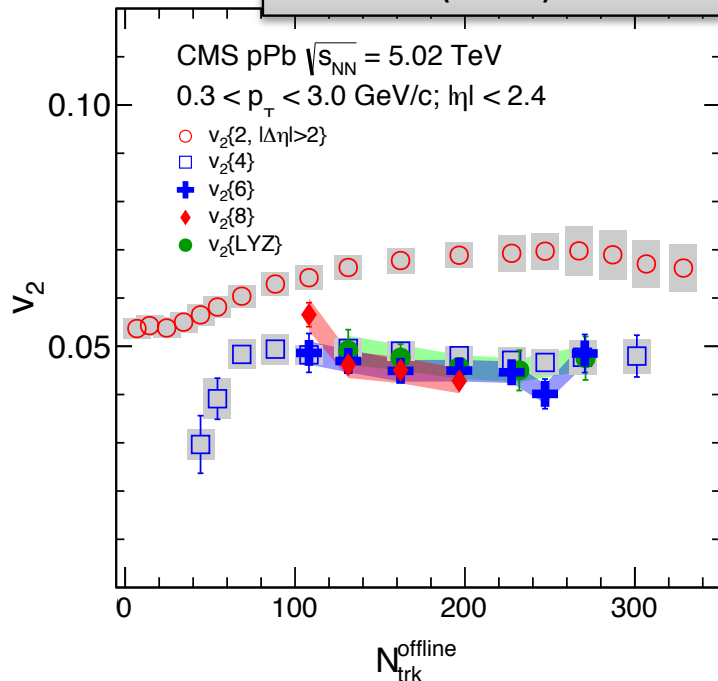
(c) $PbPb \sqrt{s_{NN}} = 2.76 \text{ TeV}, 220 < N_{\text{trk}}^{\text{offline}} \leq 260$



$1 < p_T < 3 \text{ GeV}/c$

PLB 724 (2013) 213

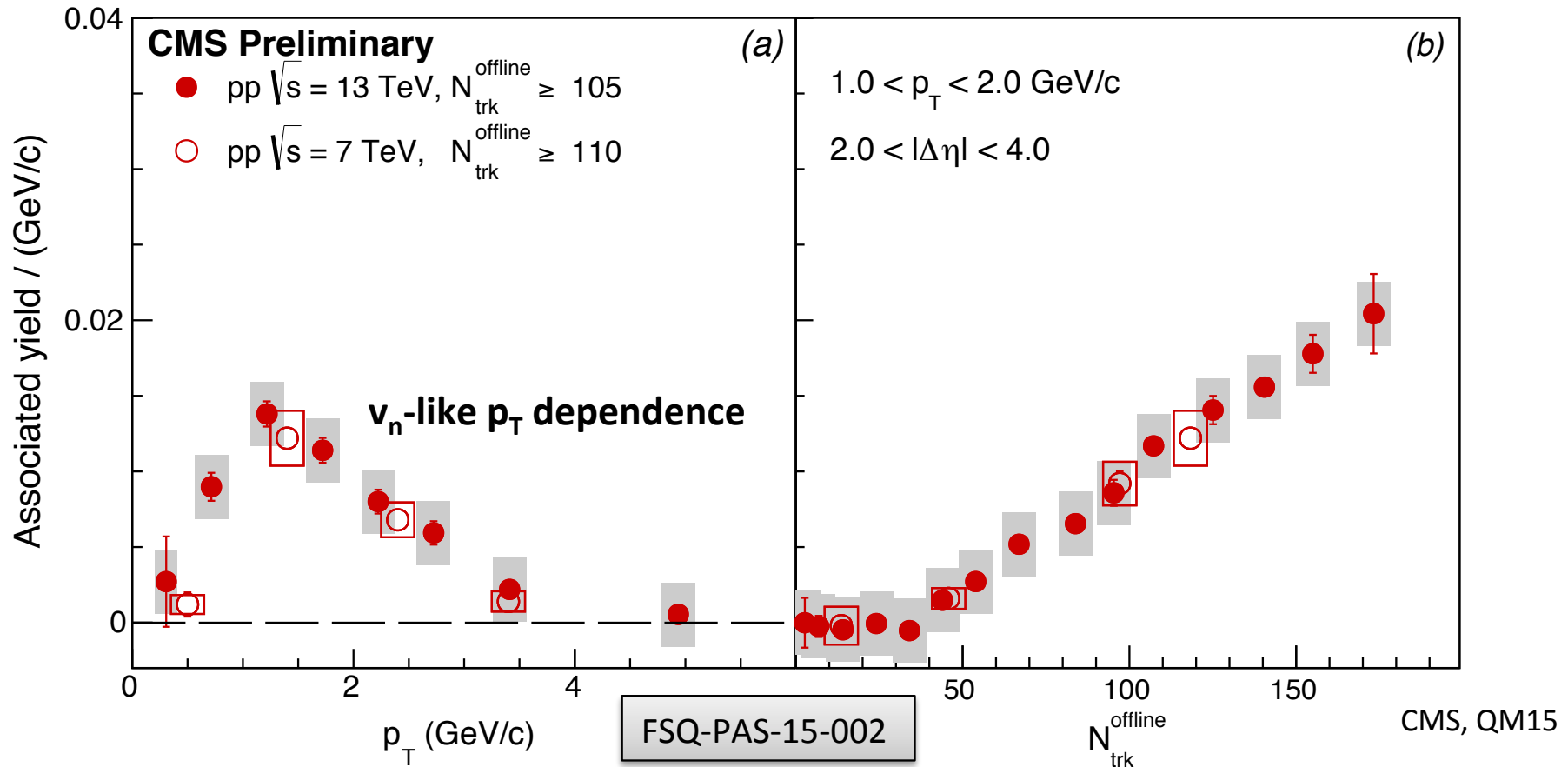
CMS, QM15

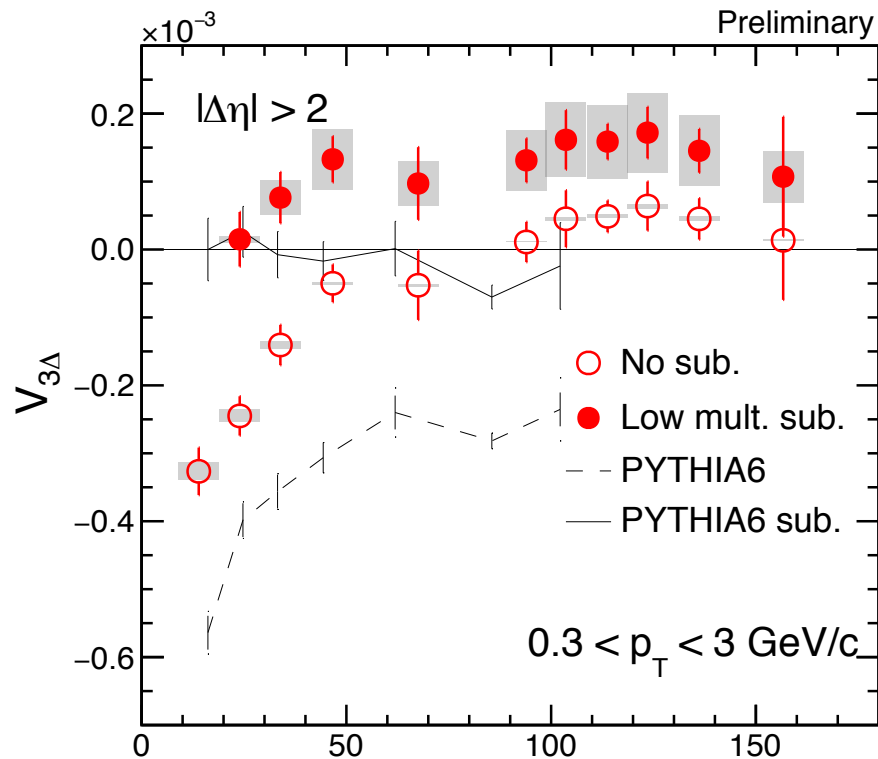
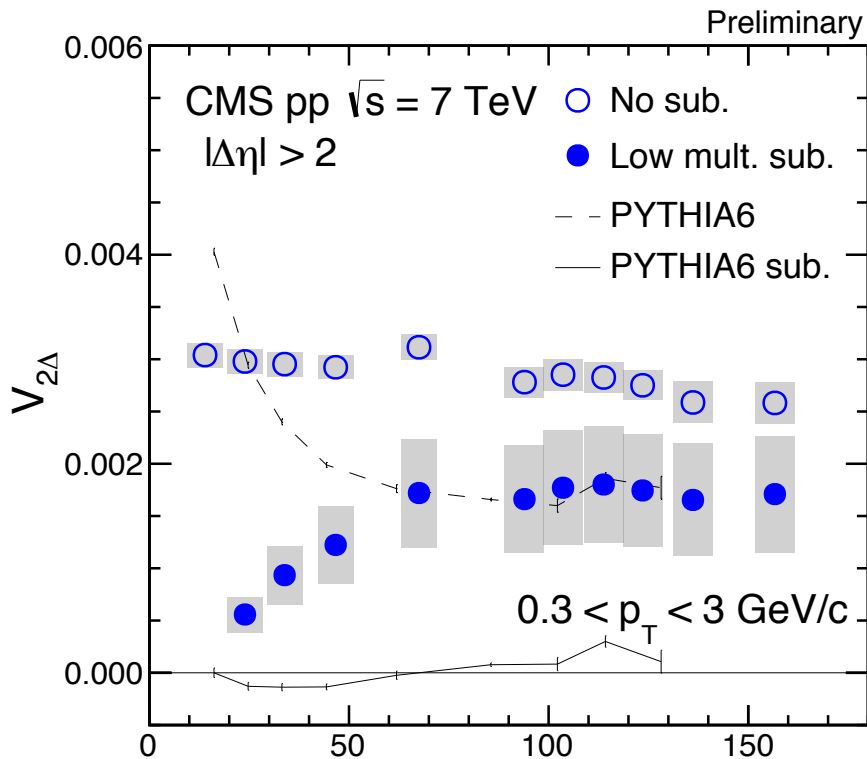


HIN-PAS-15-006
 Talk by Hong Ni
 Poster by Z. Tu (#0214)

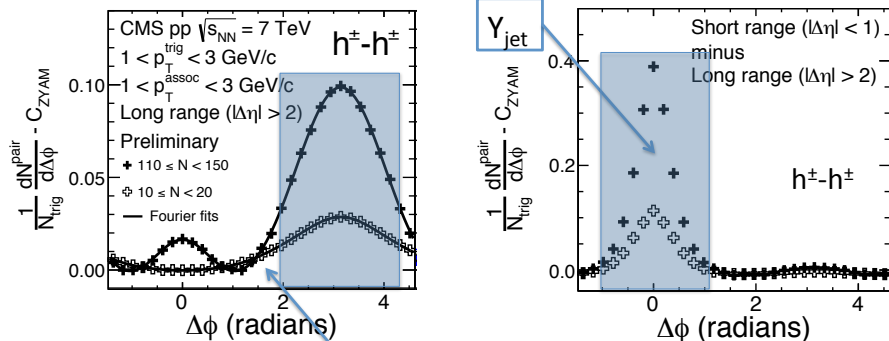
3 Supporting Facts of Collective Expansion in pA at LHC

Ridge Yield vs (p_T , beam energy, multiplicity) in pp at LHC





❖ Bias to more jet contribution when selecting high multiplicity



❖ Calibrating the bias by near-side jet yield Y_{jet}

low multiplicity subtraction to remove jet contribution:

$$V_{n\Delta}^{sub} \times N_{assoc}^{high} = V_{n\Delta}^{high} \times N_{assoc}^{high} - V_{n\Delta}^{low} \times N_{assoc}^{low} \times \frac{Y_{jet}^{high}}{Y_{jet}^{low}}$$

CMS-FSQ-PAS-15-002

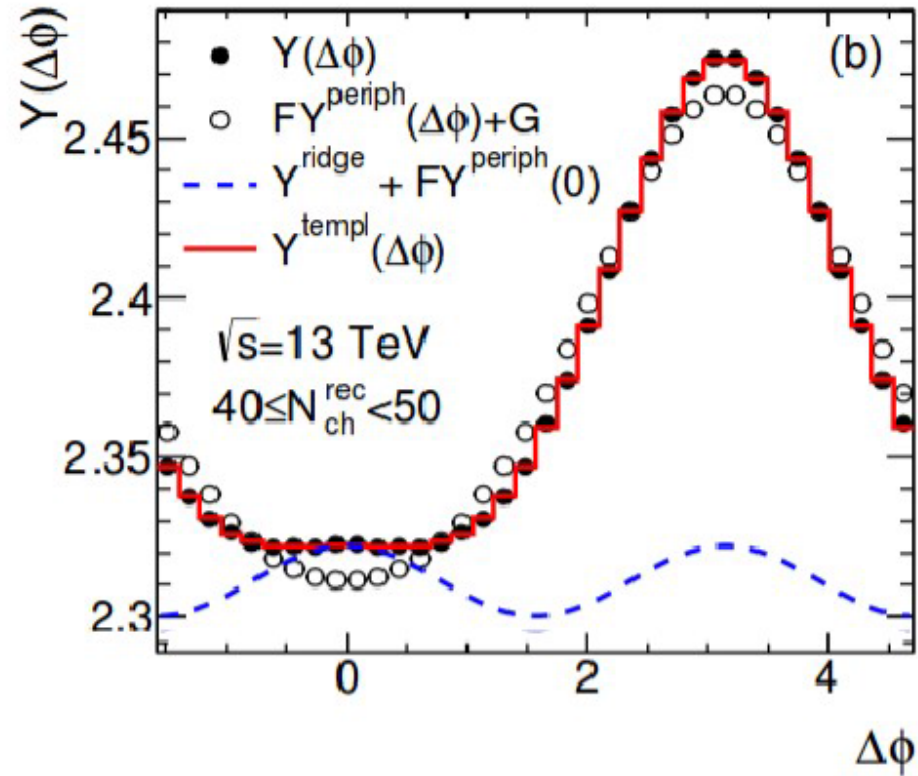
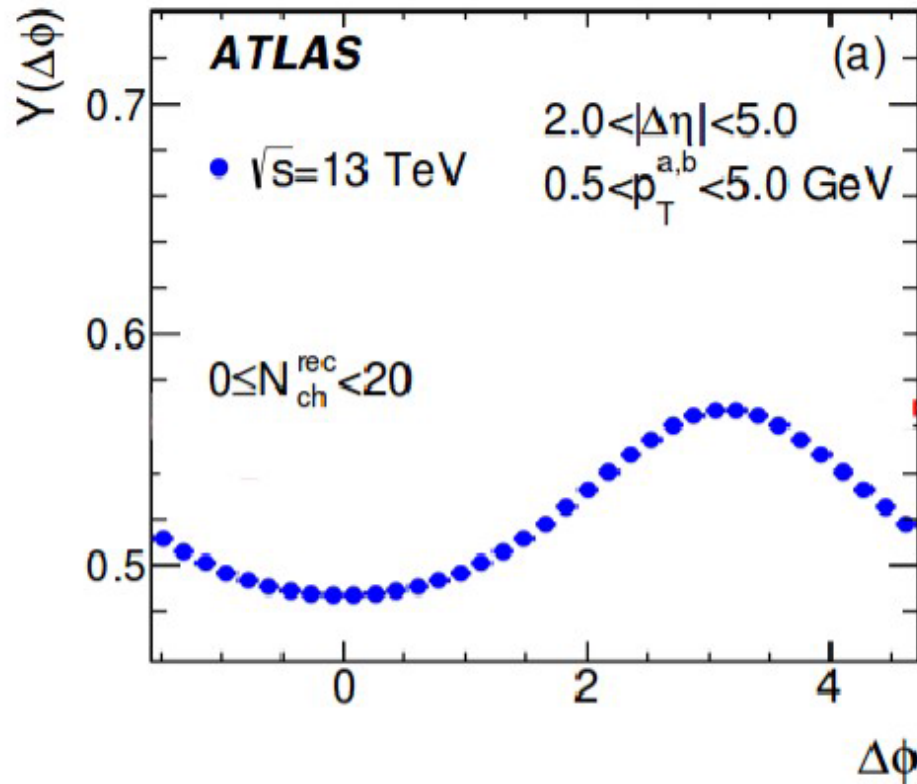
$N_{trk}^{offline}$

**Multiplicity dependence
of v_n with/without
low mult. subtraction**
--- comparison with pythia6 M.C. ---

CMS, QM15

ATLAS ways of pp analysis

arXiv:1509.04776
PRL116 (2016) 172301

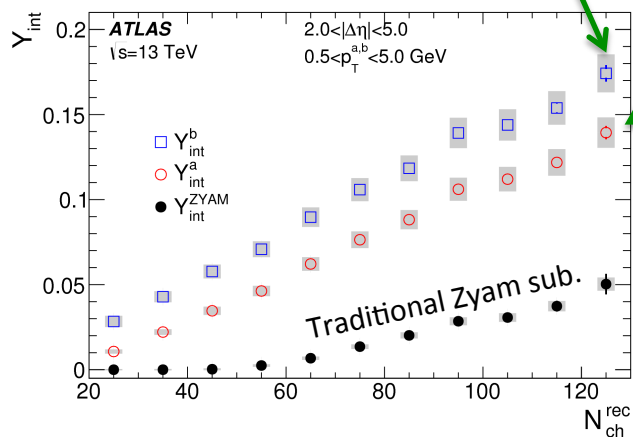
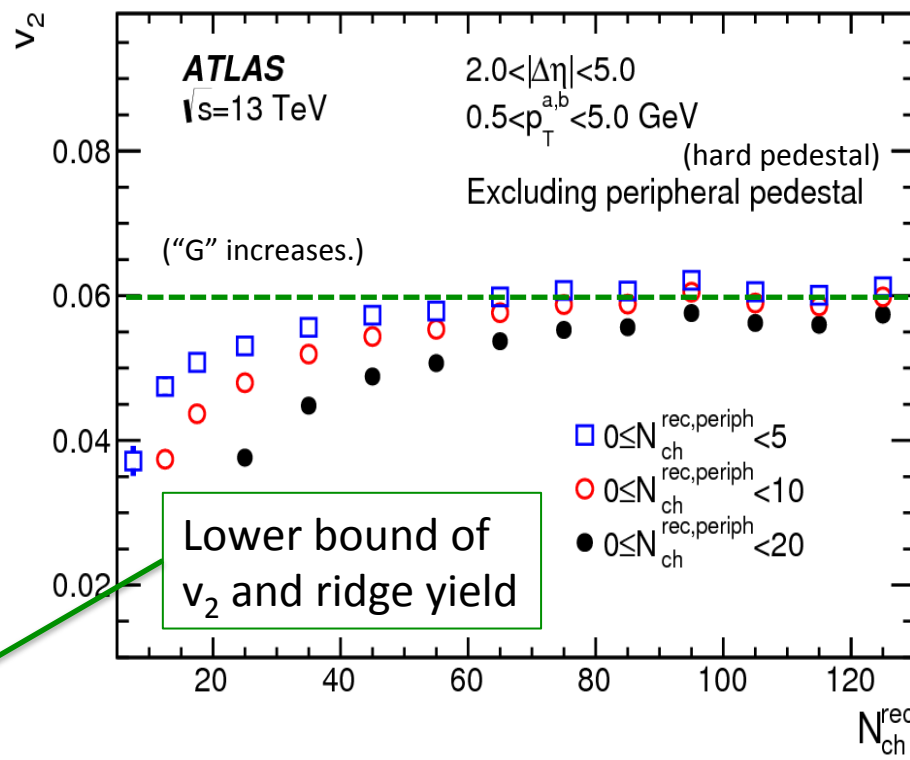
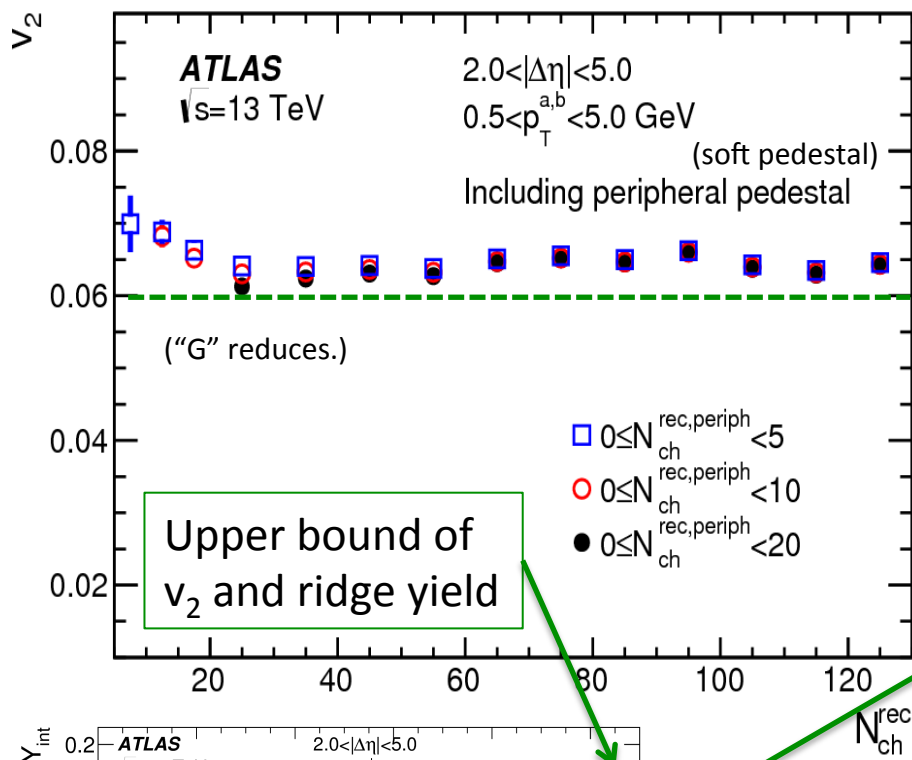


Template fitting

$$Y^{templ}(\Delta\phi) = FY^{periph}(\Delta\phi) + Y^{ridge}(\Delta\phi),$$

$$Y^{ridge}(\Delta\phi) = G[1 + 2v_{2,2} \cos(2\Delta\phi)],$$

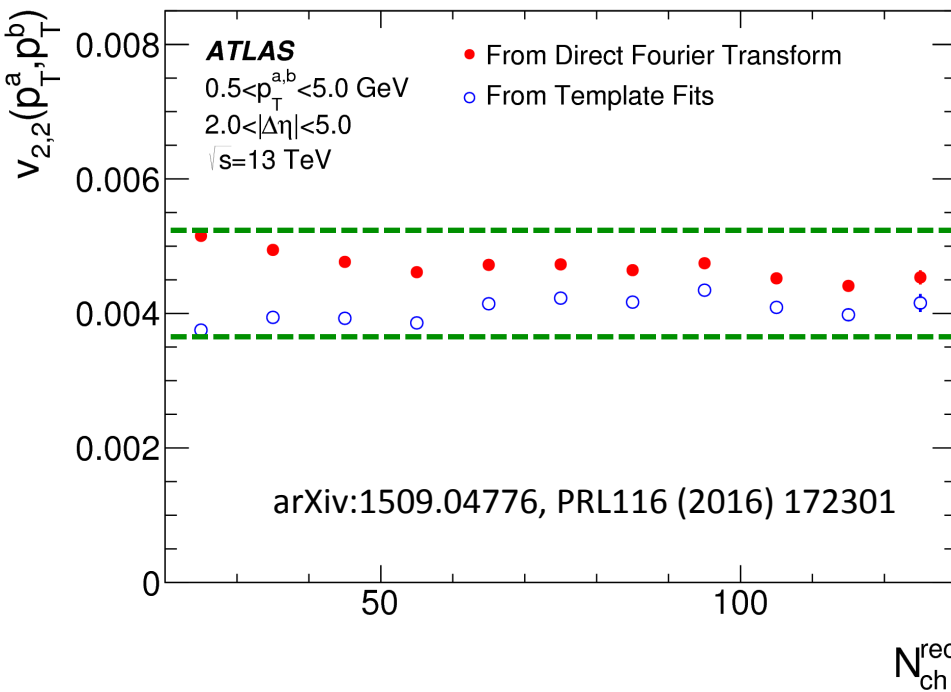
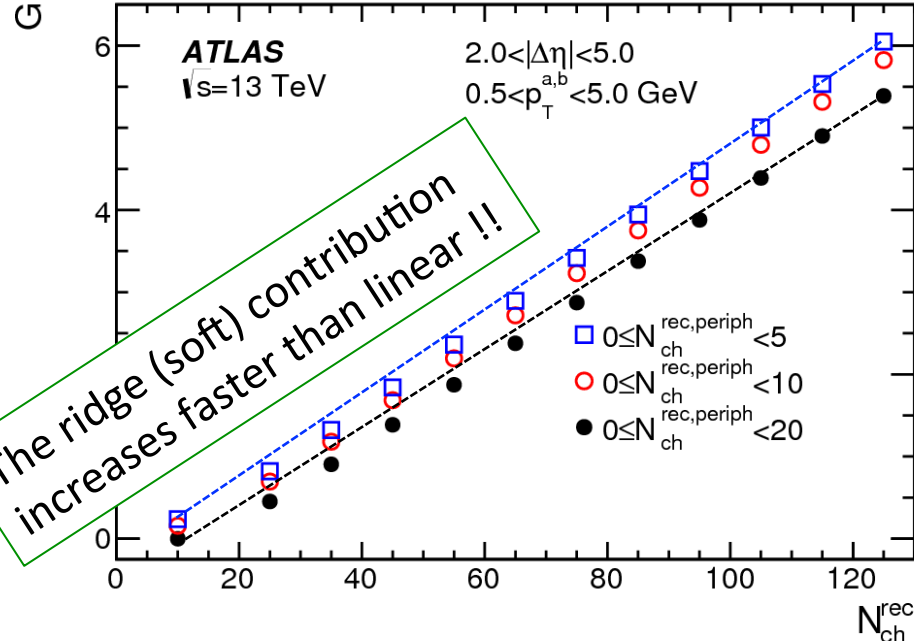
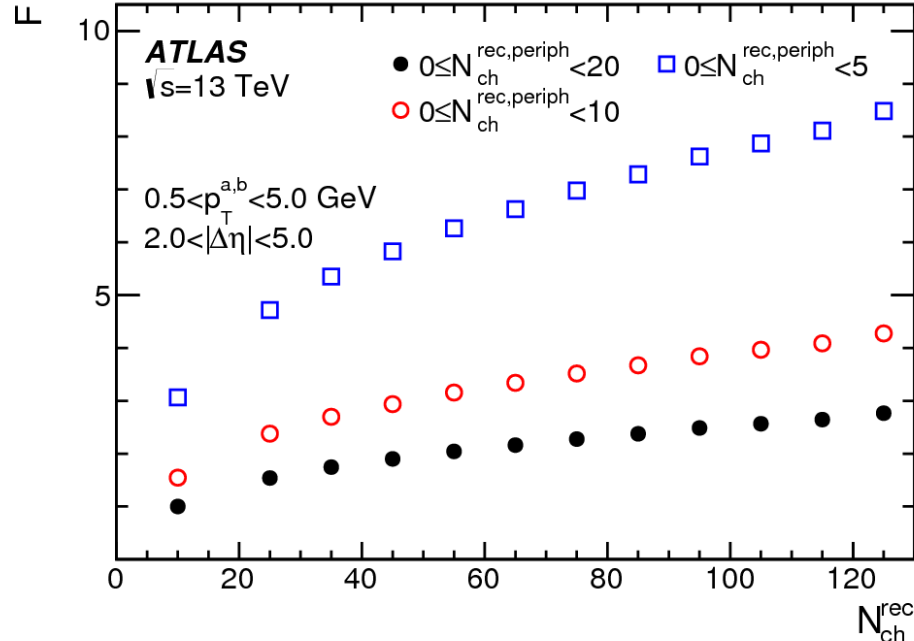
$$Y^{periph}(\Delta\phi) = Y^{hard}(\Delta\phi) + G_0[1 + 2v_{2,2}^0 \cos(2\Delta\phi)],$$



$$Y^{templ}(\Delta\phi) = FY^{periph}(\Delta\phi) + Y^{ridge}(\Delta\phi),$$

$$Y^{ridge}(\Delta\phi) = G[1 + 2v_{2,2} \cos(2\Delta\phi)],$$

$$Y^{periph}(\Delta\phi) = Y^{hard}(\Delta\phi) + G_0[1 + 2v_{2,2}^0 \cos(2\Delta\phi)],$$



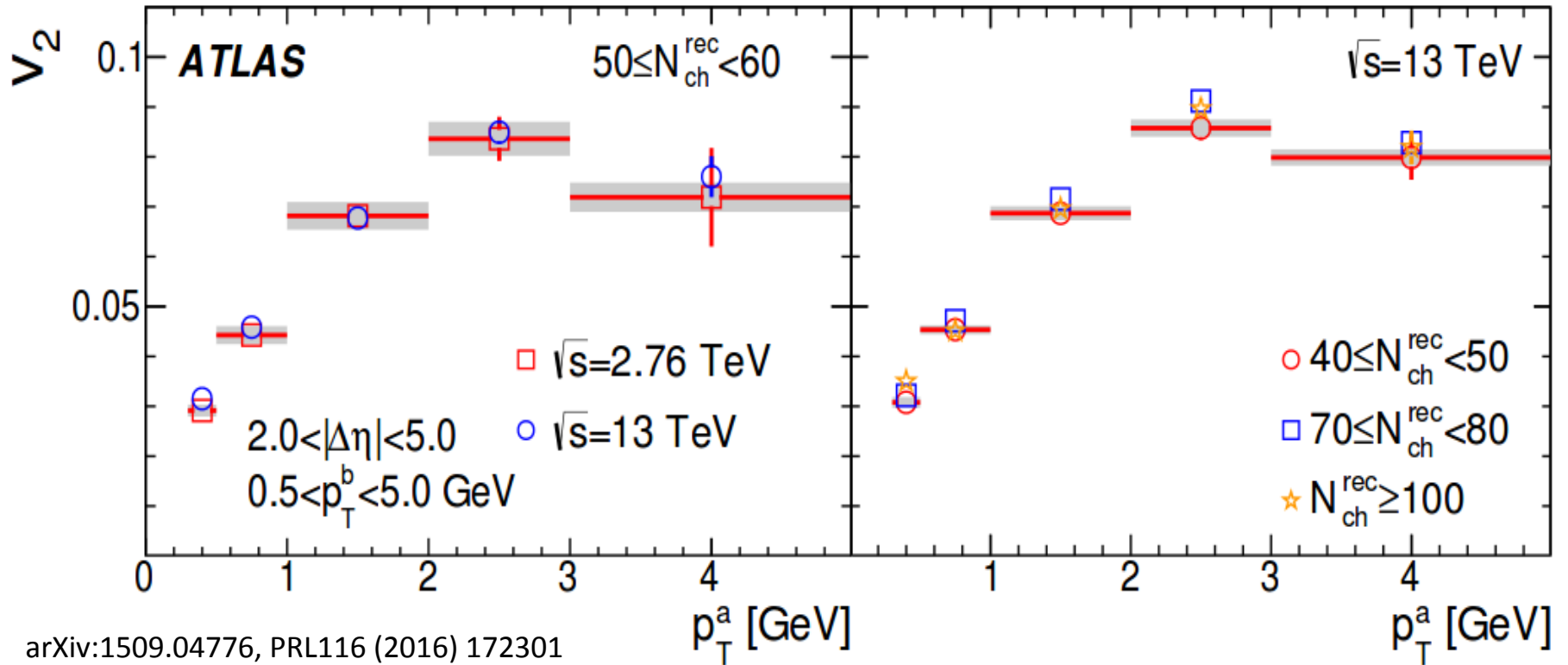
$$Y^{templ}(\Delta\phi) = F Y^{periph}(\Delta\phi) + Y^{ridge}(\Delta\phi),$$

$$Y^{ridge}(\Delta\phi) = G [1 + 2v_{2,2} \cos(2\Delta\phi)],$$

$$Y^{periph}(\Delta\phi) = Y^{hard}(\Delta\phi) + G_0 [1 + 2v_{2,2}^0 \cos(2\Delta\phi)],$$

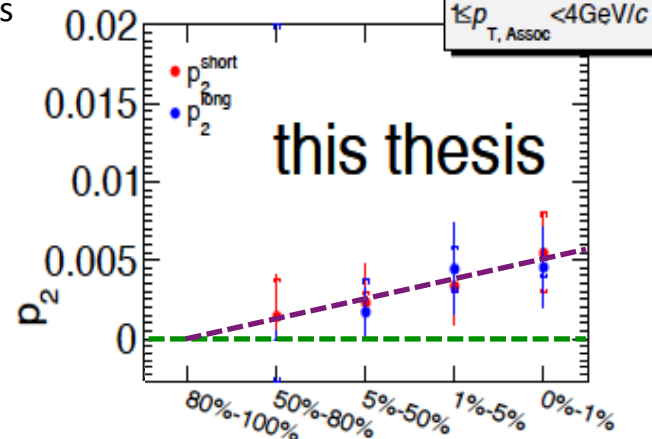
- Reference fitting ($C_2 - C_{Ref.} + 1$)
 v_2 is defined w.r.t. the total integral based on no separation btw. hard/soft.?

similar p_T dependence of v_2 to the larger systems
 no (or very weak) dependence of v_2 on energy and multiplicity

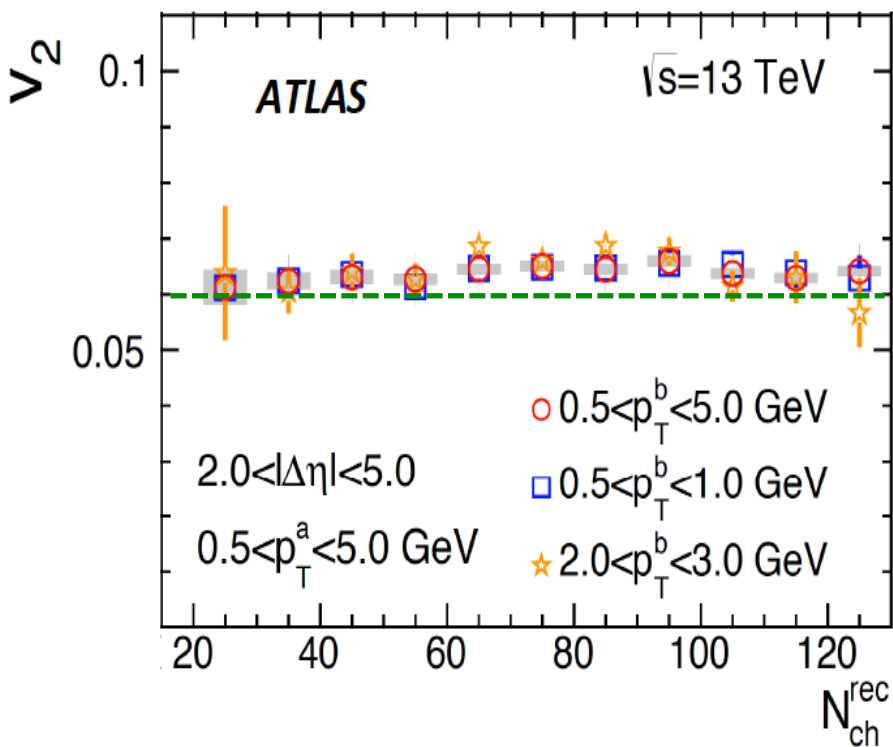


$1 \leq p_{T, \text{Trig}} < 4 \text{ GeV}/c$
 $1 \leq p_{T, \text{Assoc}} < 4 \text{ GeV}/c$

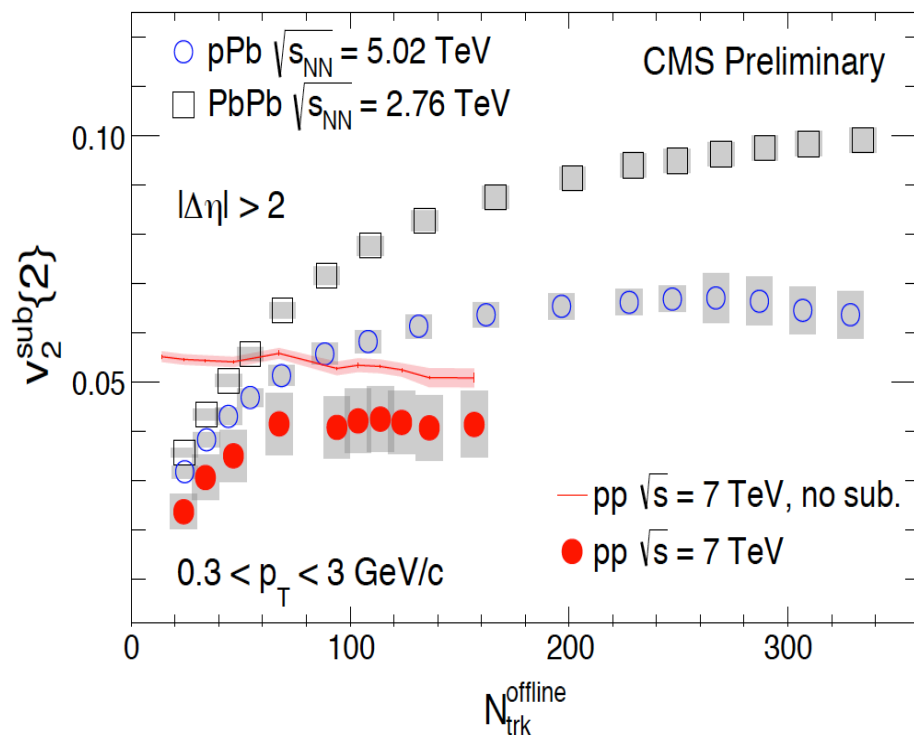
Multiplicity dependence of v_2 in pp at LHC with various methods



arXiv:1509.04776, PRL116 (2016) 172301

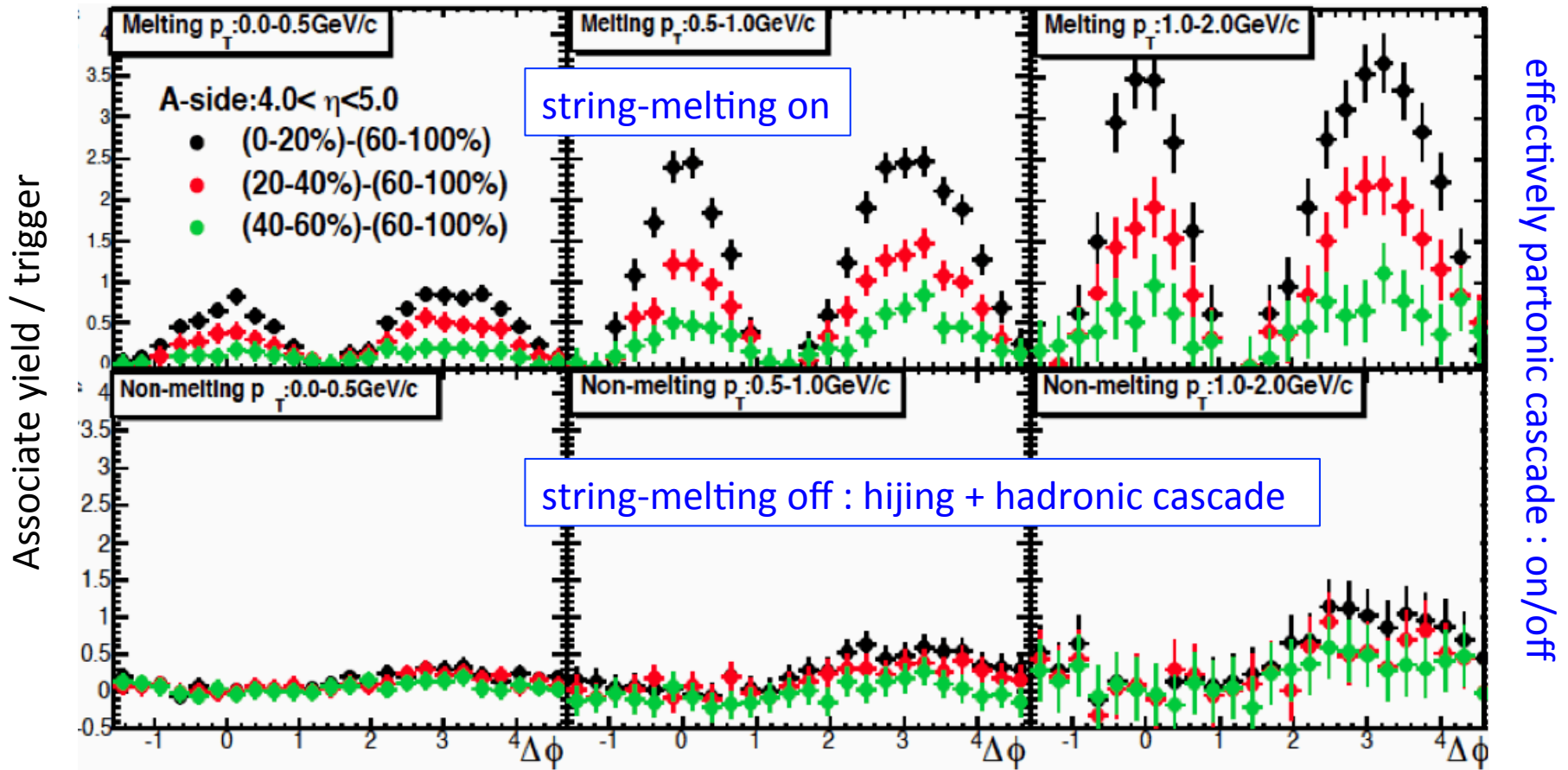


CMS, QM15



AMPT simulation p+Pb 5TeV (string-melting on/off)

for ALICE backward-central $\Delta\phi$ correlation ($|\Delta\eta|=3\sim 6$)



JPS 2014/Mar,
Kazuki Oshima,
Univ. of Tsukuba

p_T/η cuts are chosen for ALICE TPC-VOA acceptance.

TPC : $|\eta| < 1$
VOA : $3 < \eta < 5$ (Pb-going side)
VOC : $-4 < \eta < -2$ (p-going side)

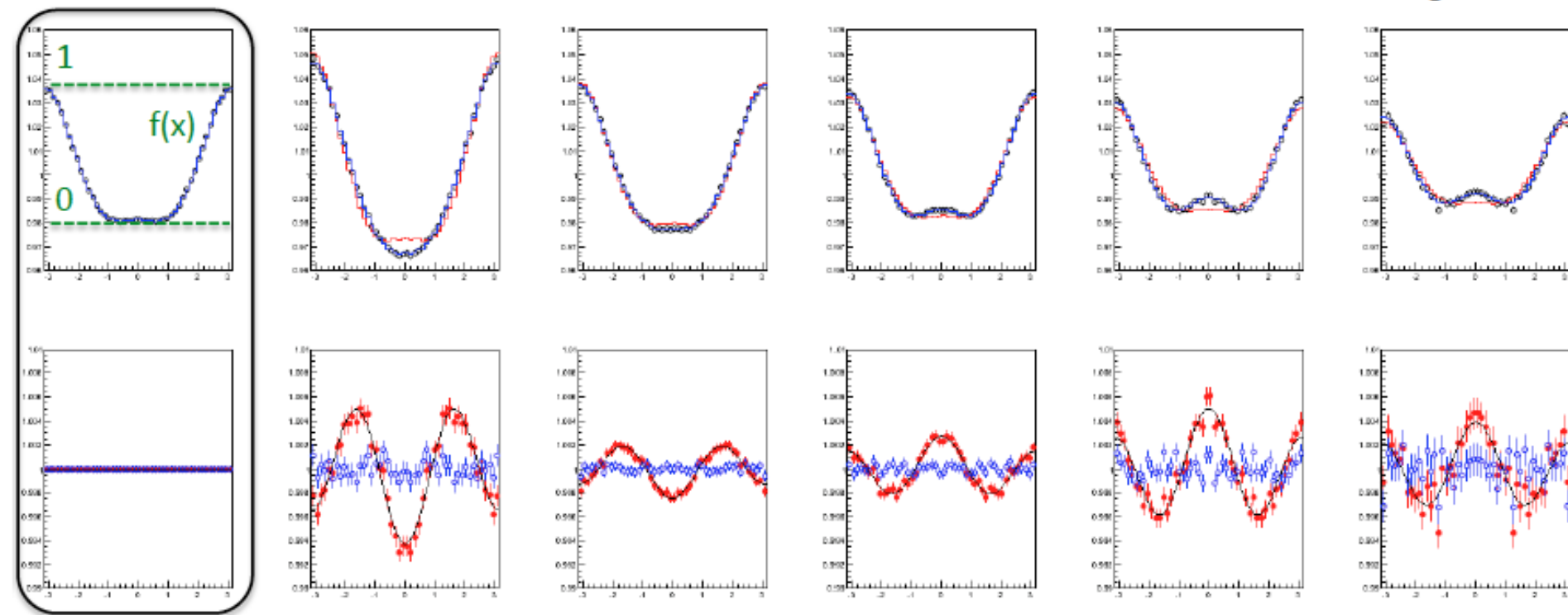
AMPT pp test with reference fitting method

- AMPT data
- Reference fitting : $F(x) = a + b f(x)$
- Reference fitting + v_2 term : $F(x) = a + b f(x) + 2 c \cos(2x)$

M.B.

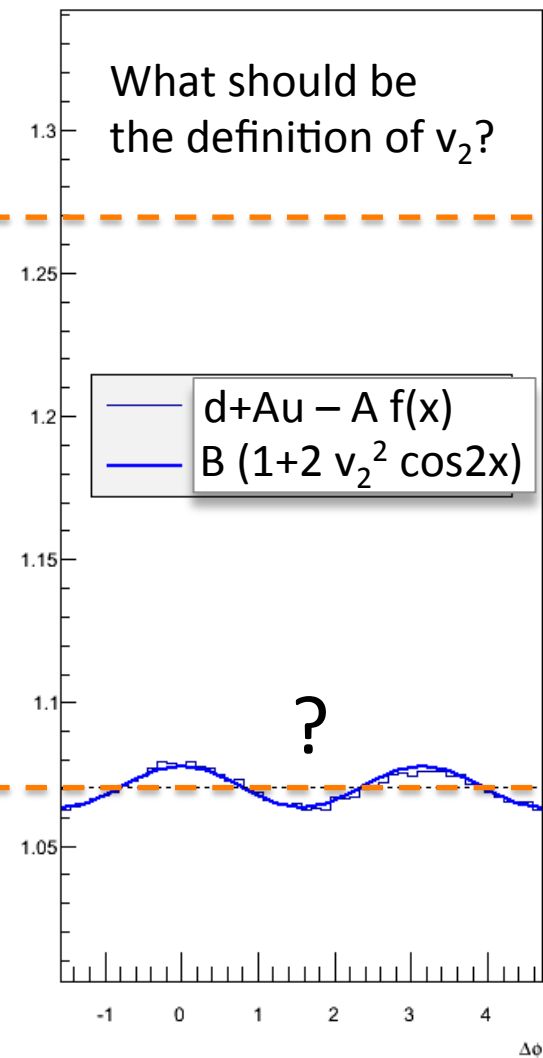
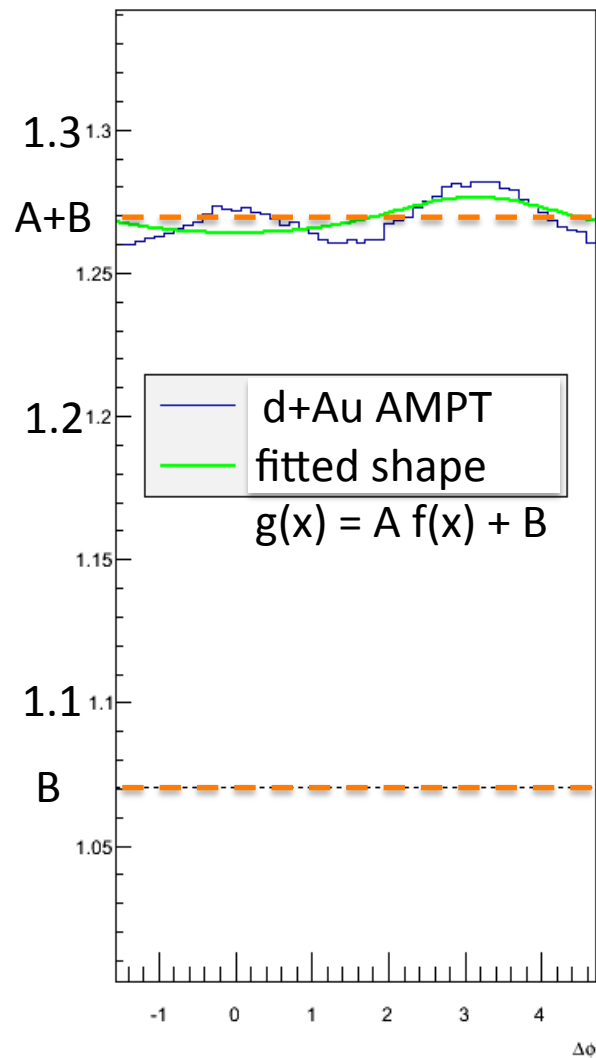
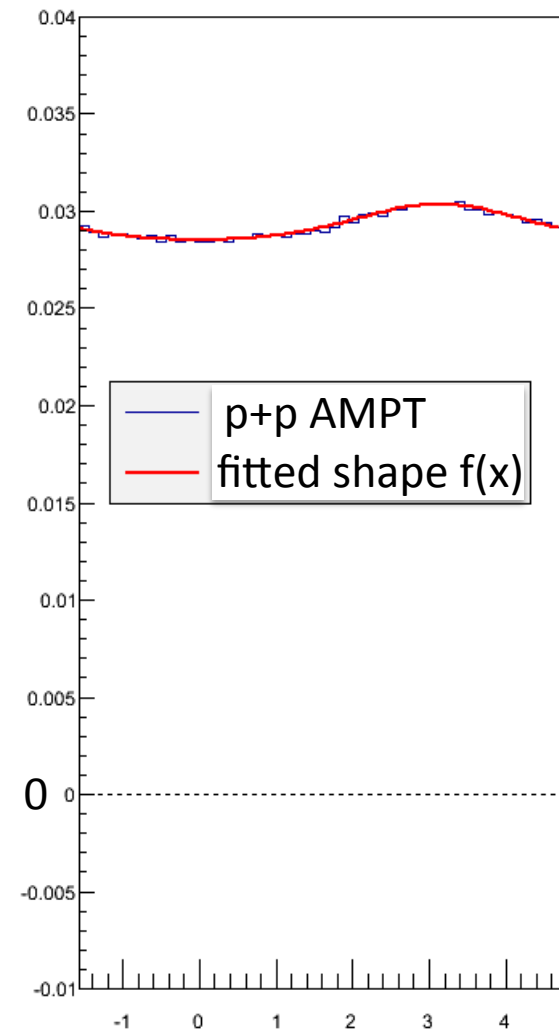
Low Mult. ←

→ High Mult.

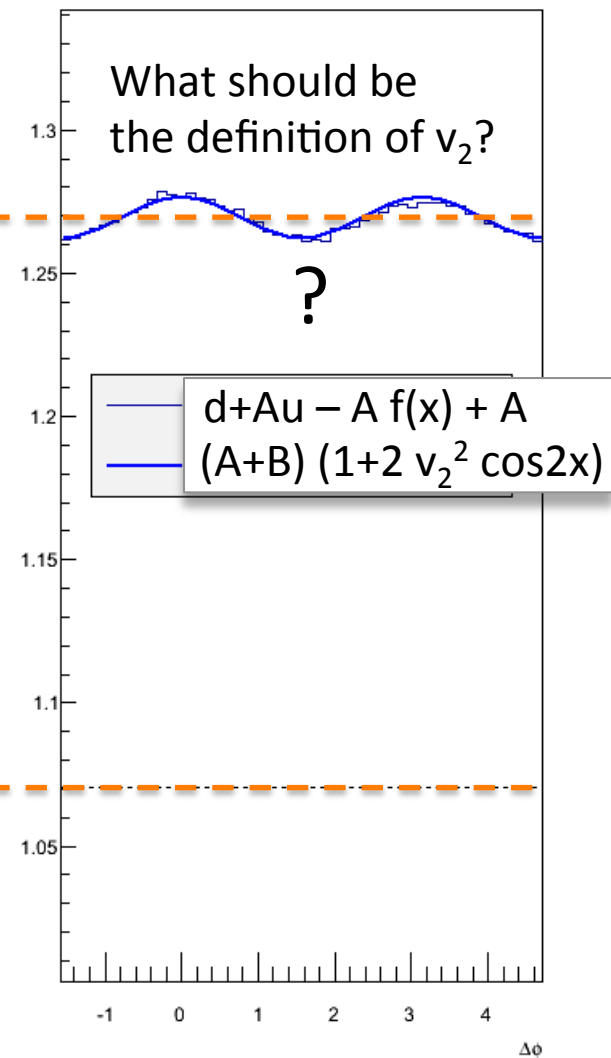
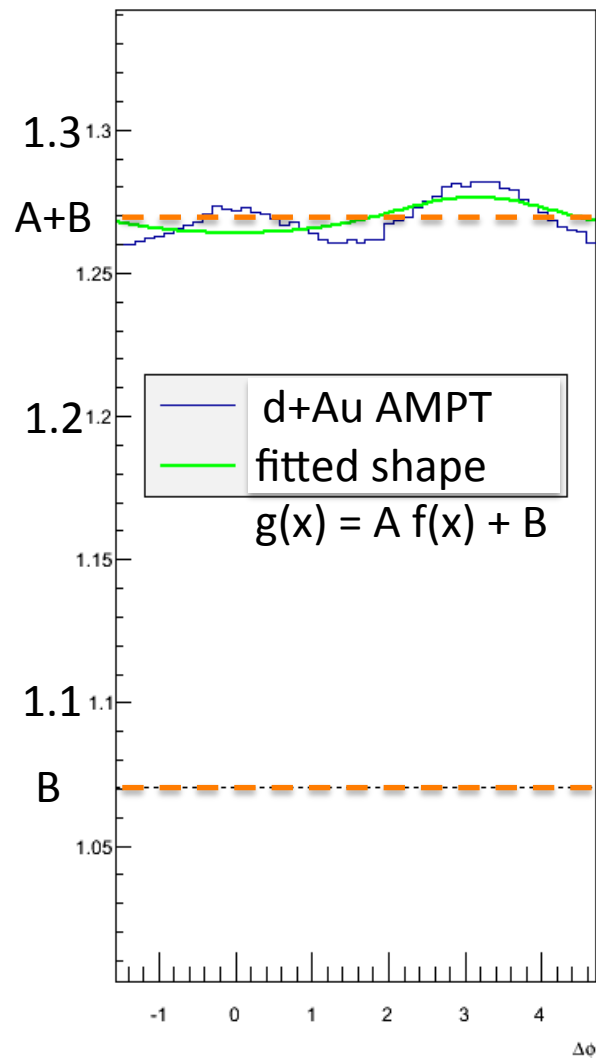
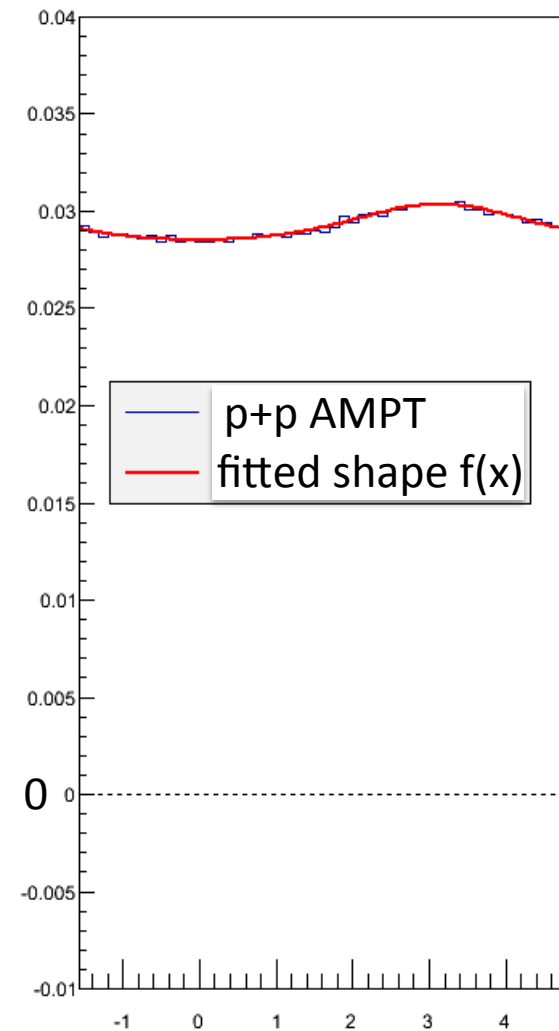


- AMPT data - Reference fitting + 1
- AMPT data - (Reference fitting + v_2 term) + 1

0.4



0.4



**Thank you very much
for our current and continuing fruitful collaboration !**