

Theoretical developments on initial state and fluctuation (QM2014 Review)

Heavy Ion Meeting 2014-06

June 20 2012

Korea University

Sungtae Cho



Institute of Physics and Applied Physics
Yonsei University

Outline

- New universal parametrization of initial –state fluctuations and its application to event-by-event anisotropy ... by L. Yan
- Multi-particle production and ridge structure in A+A, p+A, and p+p collisions ... by B .Schenke
- Is perfect fluidity of the sQGP necessary in light of recent BES & D+Au & p+Au data from RHIC and LHC? ... by M. Gyulassy

New universal parametrization of initial-state fluctuations and its application to event-by-event anisotropy

Li Yan¹, Jean-Yves Ollitrault¹ and Art Poskanzer²

¹CNRS, Institut de Physique Théorique, Saclay

²Lawrence Berkeley National Laboratory

Quark Matter 2014, Darmstadt

Outline

- ▶ Introduce **Elliptic Power** and **Power** parameterizations of ε_n fluctuations.
- ▶ Apply **Elliptic Power** and **Power** to v_n data.

– Elliptic power distribution

L. Yan, J-Y. Ollitrault, and A. M. Poskanizer, arXiv:1405:6595

Eccentricity distributions in nucleus-nucleus collisions

Li Yan,¹ Jean-Yves Ollitrault,¹ and Arthur M. Poskanzer²

¹*CNRS, URA2306, IPhT, Institut de physique théorique de Saclay, F-91191 Gif-sur-Yvette, France*

²*Lawrence Berkeley National Laboratory, Berkeley, California, 94720*

(Dated: May 27, 2014)

- 1) A parametrization of the distribution of the initial eccentricity in a nucleus-nucleus collisions at a fixed centrality
- 2) A two parameter distribution, where one of them corresponds to the intrinsic eccentricity, while the other controls the magnitude of eccentricity fluctuations.

– Eccentricity ε_2

- 1) v_2 is, to a good approximation, a linear response to the initial eccentricity ε_2 , which quantifies the spatial azimuthal anisotropy of the fireball

- 2) The initial eccentricity comes from two effects
 - i. The overlap area between the colliding nuclei has the shape of an almond in non-central collisions.
 - ii. There is a sizable eccentricity, even in central collisions, due to quantum fluctuations in wave functions of incoming nuclei

- 3) It is defined in every event from the initial energy density profile and thus carries information about how energy is deposited in the early stage of heavy ion collisions

– Models of the initial energy density profile and its fluctuation

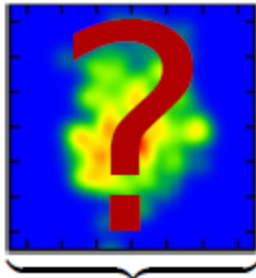
- 1) The MC Glauber model in event-by-event hydrodynamics
: the energy is localized around each wounded nucleon
- 2) The MC+ saturation physics as an initial conditions in hydro

– Simple parametrization of ε_2

- 1) The Bessel-Gaussian distribution
: works well for nucleus-nucleus collisions at moderate impact parameters, but fails for more peripheral collisions and/or small systems such as proton-nucleus collisions
- 2) A new power distribution

Motivation: fluctuations of harmonics

- Fluctuating initial state and harmonic flow v_n :

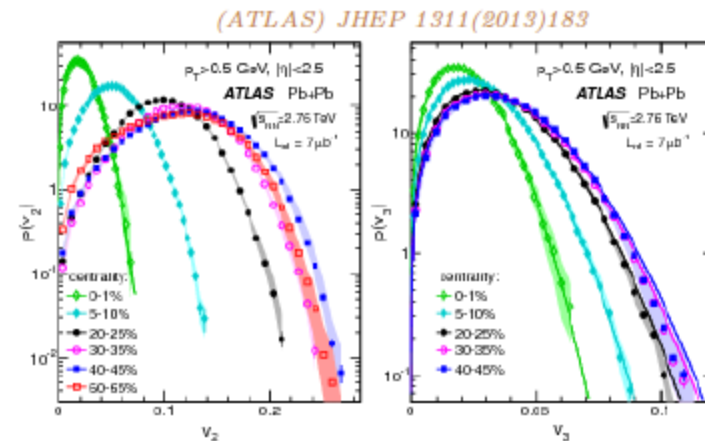
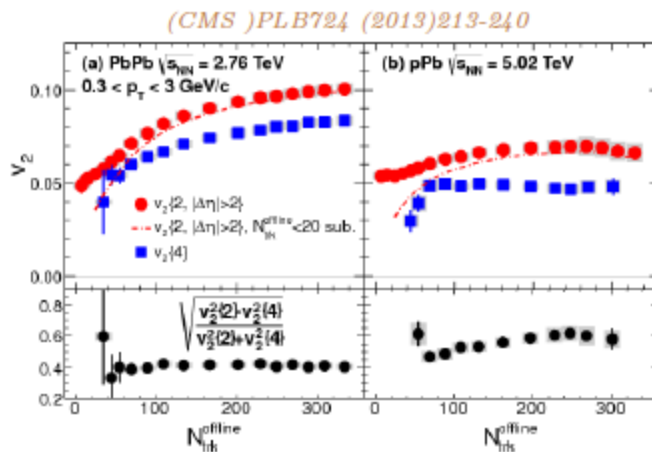


\rightleftharpoons
medium exp.

$$\frac{dN}{d\phi_p} \sim 1 + 2 \sum_n v_n e^{in(\phi_p - \Psi_n)}$$

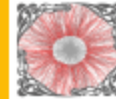
Glauber, KLN, IP-Glasma

- Fluctuations of v_n in experiments:



- 1 Significant $v_2\{4\}$ observed in p-Pb? Do we see collective expansion in p-Pb?
- 2 What can we learn from EbyE v_n distribution? In particular, η/s ?

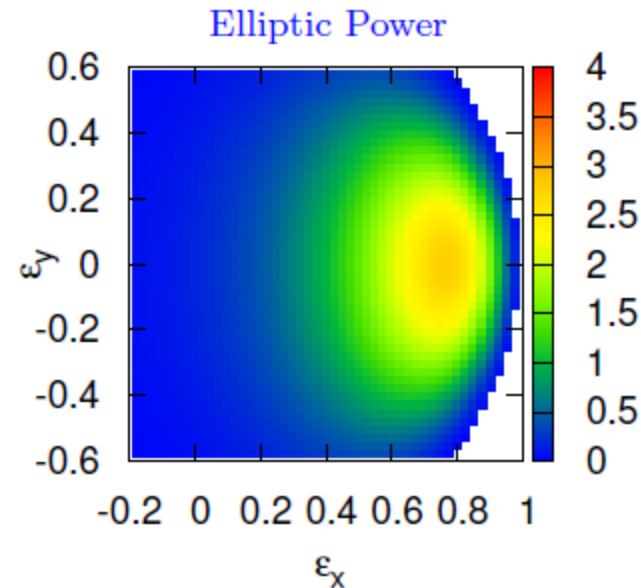
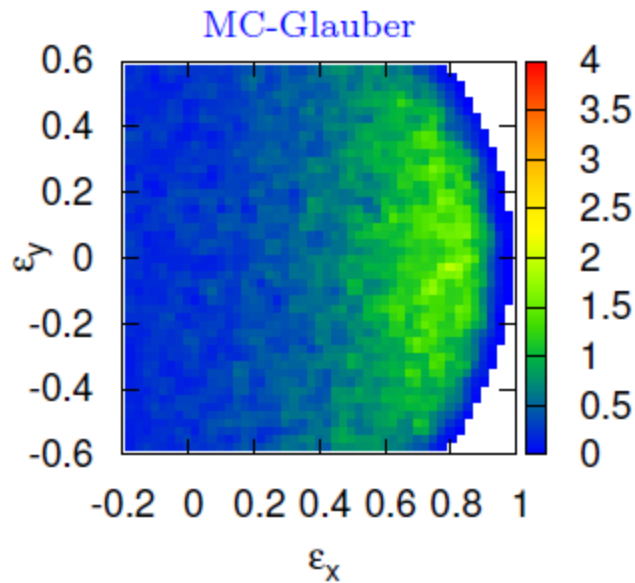
Elliptic Power distribution and Power distribution



- **Elliptic Power distribution** : (e.g. assuming N independent point-like sources)

$$P_{\text{EP}}(\varepsilon_x, \varepsilon_y) = \frac{\alpha}{\pi} (1 - \varepsilon_0^2)^{\alpha + \frac{1}{2}} \frac{(1 - \varepsilon_x^2 - \varepsilon_y^2)^{\alpha - 1}}{(1 - \varepsilon_0 \varepsilon_x)^{2\alpha + 1}}, \quad \text{with } \varepsilon_x^2 + \varepsilon_y^2 < 1$$

$\alpha \sim N \Rightarrow$ fluctuations, $\varepsilon_0 \Rightarrow$ average reaction plane(RP) eccentricity



- **Power distribution** (e.g. ε_3 in AA, ε_n in p-Pb) : fluctuation-driven with $\varepsilon_0 = 0$

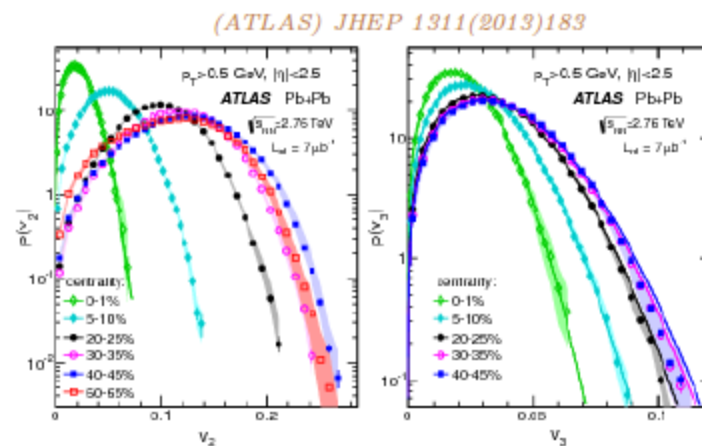
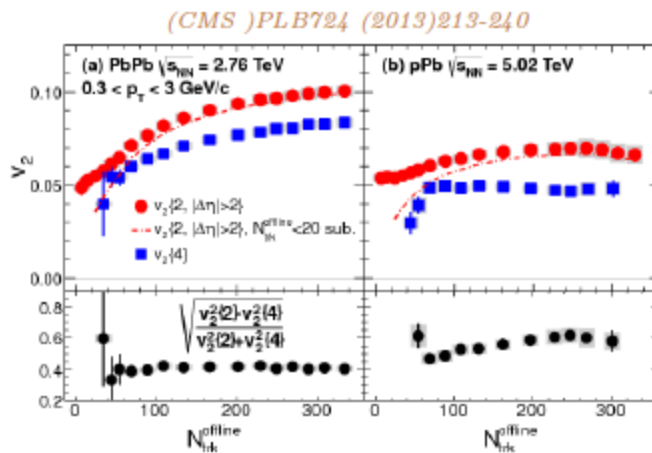
$$P_{\text{Power}}(\varepsilon_x, \varepsilon_y) = \frac{\alpha}{\pi} (1 - \varepsilon_x^2 - \varepsilon_y^2)^{\alpha - 1} \quad \Leftrightarrow \quad P_{\text{EP}}(\varepsilon_0 \rightarrow 0)$$

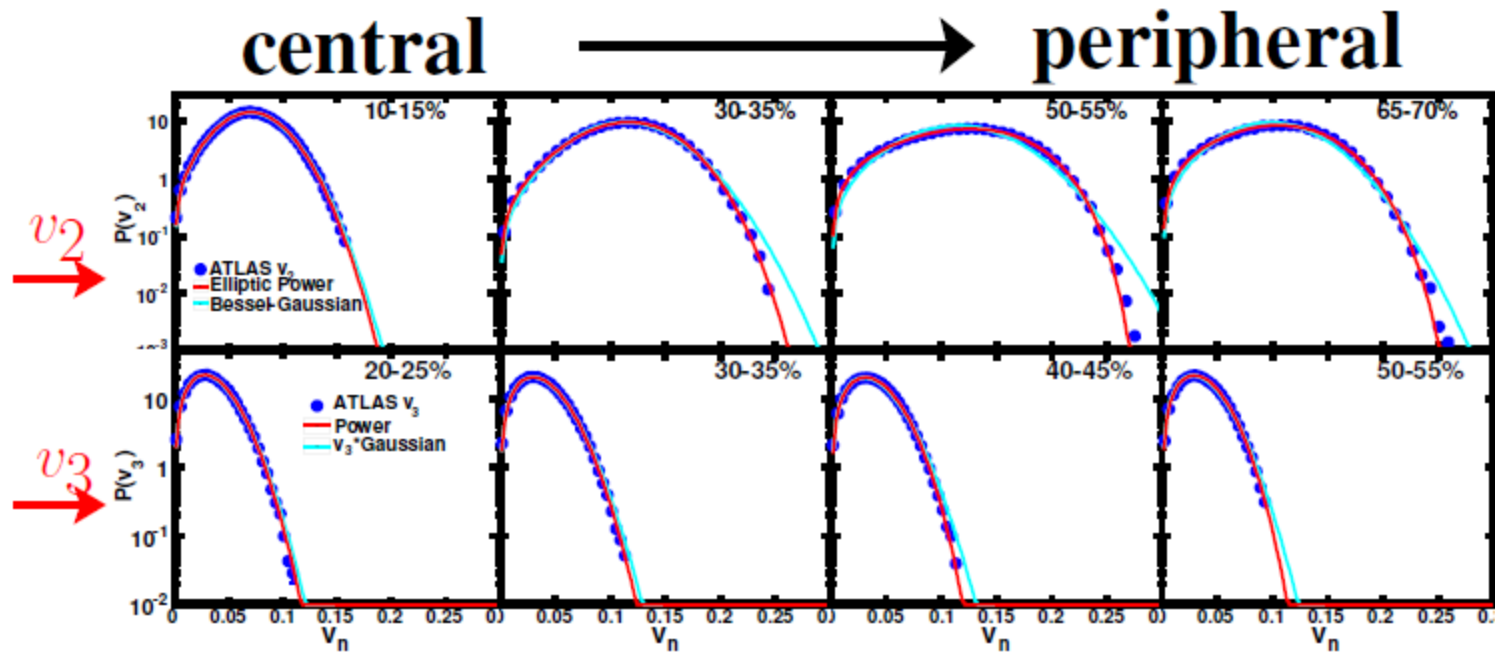
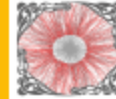
Applications to data

- With Elliptic Power and Power characterizing initial state fluctuations,
- Linear eccentricity scaling: ($n = 2$ and 3) *H.Niemi et al., Phys.Rev. C87 (2013) 054901*

$$v_n = \underbrace{\kappa_n}_{\text{medium resp.: } \eta/s} \times \underbrace{\varepsilon_n}_{\text{Elliptic Power or Power}}$$

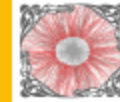
- Ignore fluctuations in medium response, i.e., κ_n does not fluctuate.
- Then distribution of v_n is rescaled Elliptic Power or Power distribution.





- Significant improvement with Elliptic Power and Power parameterization.
- Error of v_2 fit is dominated by systematic errors on $\sigma_v / \langle v \rangle$ from ATLAS results.
- Error of v_3 fit is from statistical error of v_3 only. Systematic errors are too large.

Summary and conclusions



- New parameterizations of eccentricity fluctuations: Elliptic Power and Power
 1. Implement the condition $|\varepsilon_n| < 1$: large anisotropies are correctly modeled
 2. Fit all models of the initial state (Glauber, KLN, IP-Glasma, etc.)
 3. Reveals physical information of initial state: fluctuations (α) and average shape (ε_0).
- Applications
 1. Naturally explains large $v_2\{4\}$ in p-Pb of LHC \Rightarrow collective expansion of p-Pb system.
 2. Fits of ATLAS EbyE v_2 and v_3 distributions: we are able to disentangle for the first time the initial eccentricity from the hydrodynamic response **without assuming a particular model of initial conditions.**
 - Info. of initial state \Rightarrow Fluctuations and average eccentricity of initial state.
 - Info. of the medium \Rightarrow Extraction of $\eta/s \sim 0.18$.
 3. And more



MULTI-PARTICLE PRODUCTION
AND RIDGE STRUCTURE
IN A+A, p+A, AND p+p COLLISIONS
BJÖRN SCHENKE, BROOKHAVEN NATIONAL LABORATORY

QUARK MATTER 2014
DARMSTADT
MAY 21 2014



– IP-Glasma + MUSIC

B. Schenke and R. Venugopalan, arXiv:1405:3605

Eccentric protons? Sensitivity of flow to system size and shape in p+p, p+Pb and Pb+Pb collisions

Björn Schenke and Raju Venugopalan

Physics Department, Brookhaven National Laboratory, Upton, NY 11973, USA

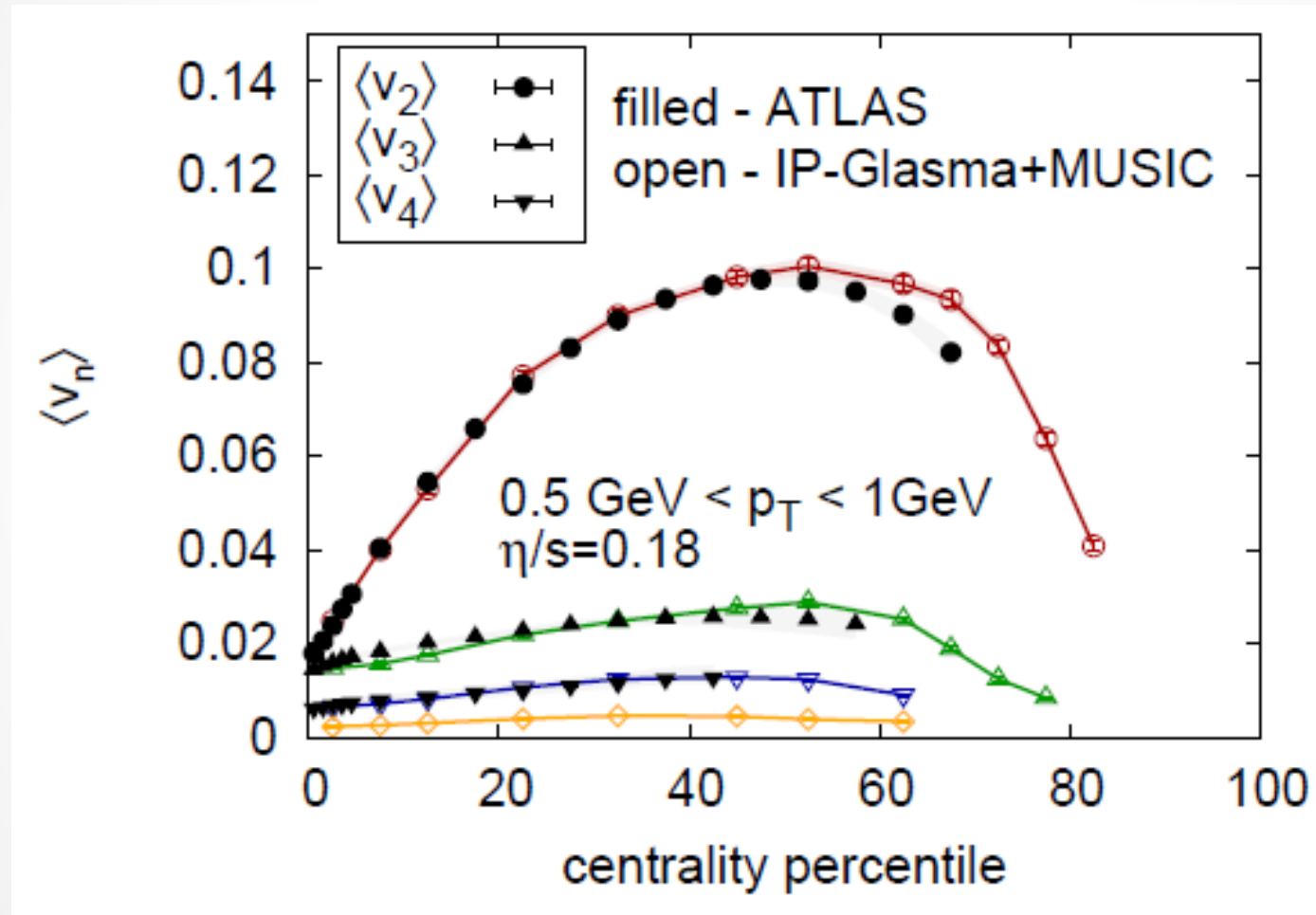
- 1) Event-by-event fluid dynamics model
 - : The color glass condensate (CGC) based IP-Glasma model in combination with the viscous fluid dynamic simulation, MUSIC

- 2) The impact parameter dependent saturation model (IP-Sat) with the classical description of initial glasma fields
 - : includes the quantum fluctuation of color charges and produces initial energy fluctuation

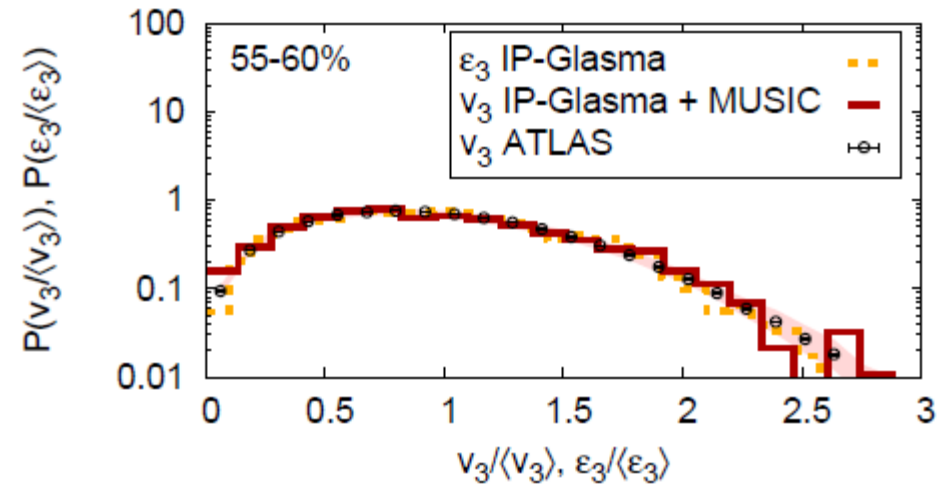
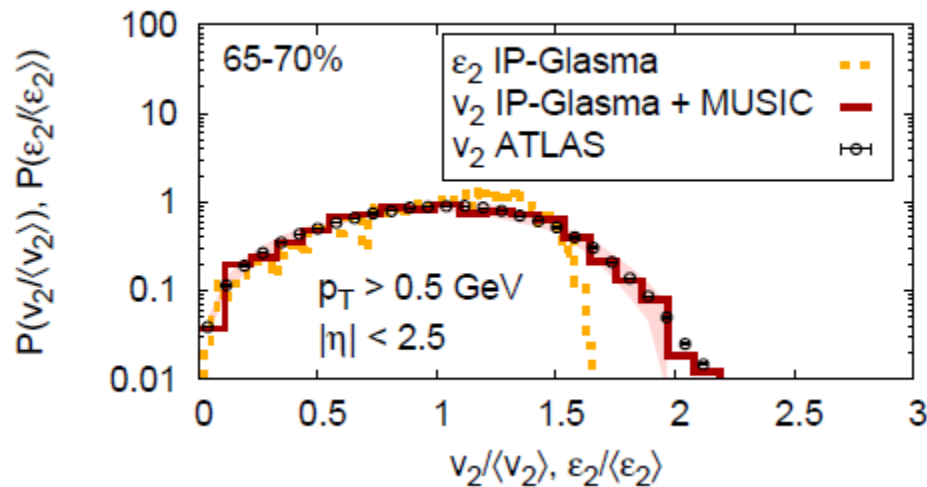
– Collective effects in pp, pA, and AA

- 1) Striking similarity in the structure of long range pseudo-rapidity correlation between high multiplicity d+Au, p+Pb collisions and peripheral heavy ion collisions with similar multiplicity
- 2) The observed mass splitting of elliptic flow has been qualitatively explained within the fluid dynamic model description
- 3) The v_n distribution are not well described by the initial state developed so far except IP-Glasma+MUSIC

- Average v_n



– Event-by-event distribution of v_n



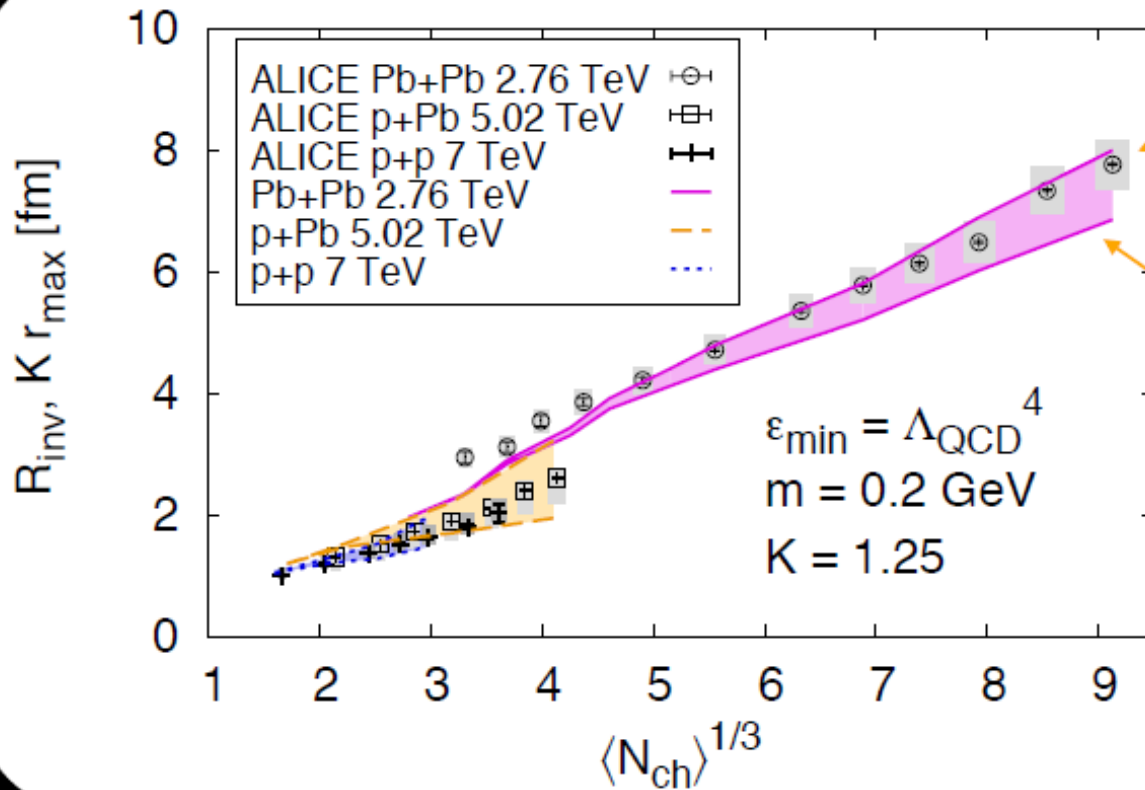
1) The initial state eccentricities ϵ_n

: quantifies the spatial azimuthal anisotropy of the fireball created right after the collisions

2) Nonlinearity effects in fluid dynamics evolution modify the shape of the distributions : the necessity of fluid dynamics

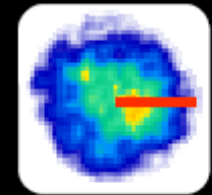
SYSTEM SIZE

A. BZDAK, B. SCHENKE, P. TRIBEDY, R. VENUGOPALAN, PRC87, 064906 (2013)
 AND B. SCHENKE, R. VENUGOPALAN, ARXIV:1405.3605 (2014)
 HBT DATA: ALICE COLLABORATION, ARXIV:1404.1194



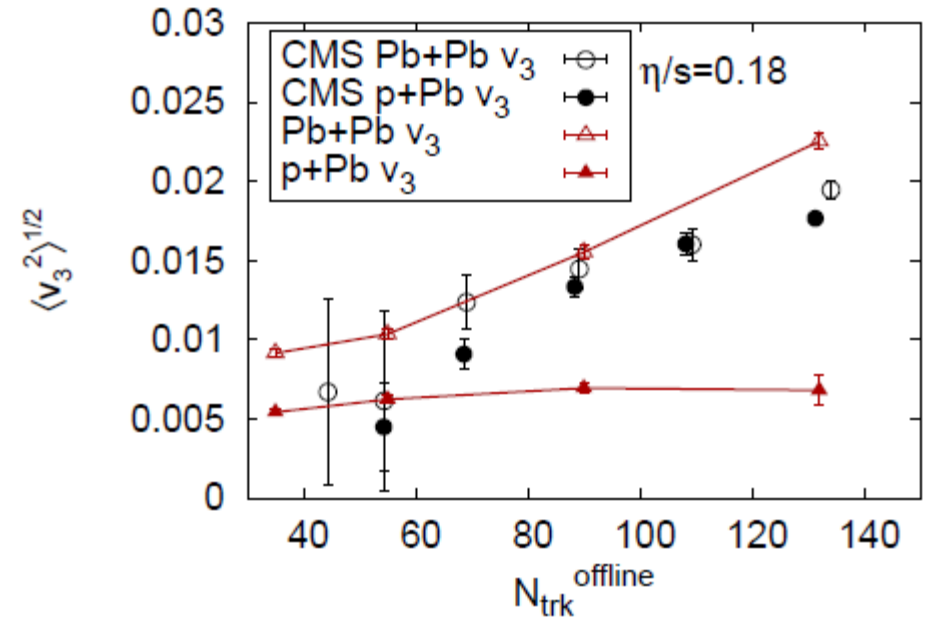
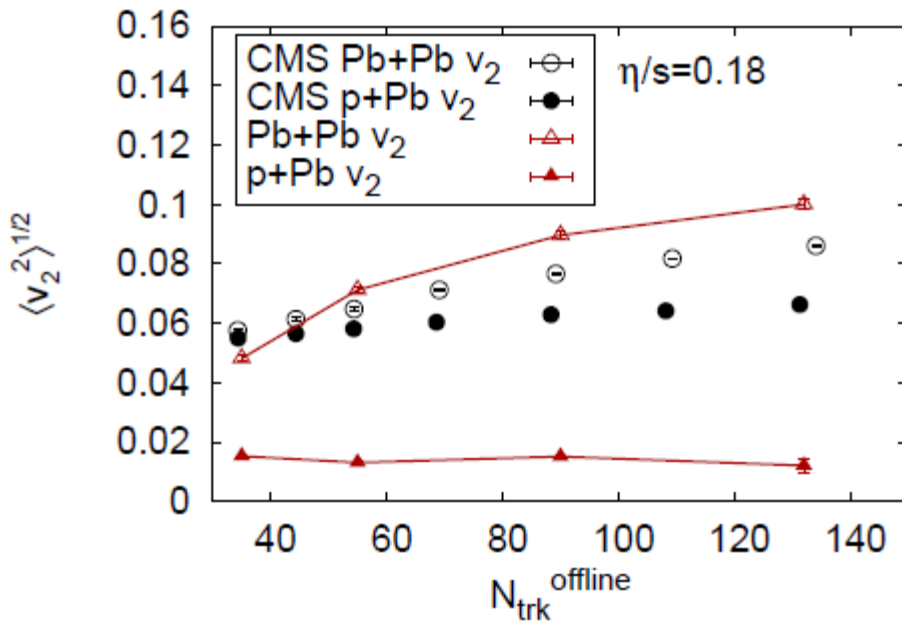
MAXIMAL
SIZE DURING
EVOLUTION

INITIAL SIZE



r_{max}

- Anisotropic flows in p+Pb collisions



1) $N_{\text{trk}}^{\text{offline}} = 132$ corresponds to 65-70% central Pb+Pb events

2) Pb+Pb data are well described while p+Pb data are not.

: No choice of parameters could achieve better agreement

FOURIER HARMONICS IN $p+Pb$

B. SCHENKE, R. VENUGOPALAN, ARXIV:1405.3605 (2014)

Why does it not work? Two possibilities:

a) We neglected correlations from the initial state

K. DUSLING, R. VENUGOPALAN, PHYS.REV. D87 054014 (2013)

They are there in IP-Glasma - just need to keep them

b) The proton is not spherical and its shape fluctuates

Other models:

MC-Glauber: similar fluctuations in $p+Pb$ and $Pb+Pb$

P. BOZEK, G. TORRIERI, W. BRONIEWSKI, PHYS.REV.LETT. 111, 172303 (2013)

I. KOZLOV, M. LUZUM, G. DENICOL, S. JEON, C. GALE, ARXIV:1405.3976 (2014)

One challenge for MC-Glauber are the similar $p+p$ and $p+Pb$ HBT radii

EPOS: Fluctuations of "cut pomerons" - larger eccentricities

K. WERNER, M. BLEICHER, B. GUIOT, I. KARPENKO, T. PIEROG, ARXIV:1307.4379

SUMMARY

- IP-Glasma model + fluid dynamics does very good job in describing experimental data in A+A collisions out to very peripheral events
- Similar size in p+p and p+Pb agrees with ALICE HBT
- Within IP-Glasma+MUSIC model and ignoring initial state correlations, v_n in p+Pb are not well described
- If fluid dynamic picture holds we have access to shape fluctuations of the proton's gluon distribution



Is Perfect Fluidity of the sQGP ***necessary*** in light of recent BES & D+Au & p+Au data from RHIC and LHC ?

Gyulassy Miklós
Wigner Research Center KFKI
(Columbia University)

Collaborators: Levai P, Vitev I, Biro T

Abstract:

Recent low $p_T < 2$ GeV azimuthal correlation data from the beam energy scan (BES) and D+Au at RHIC/BNL and the especially the surprising low p_T azimuthal $v_n(p_T)$ in p+Pb at LHC challenge long held assumptions about the necessity of perfect fluidity (minimal viscosity to entropy $\sim 1/4\pi$) to account for azimuthal asymmetric "flow" patterns in A+A.

Perfect fluidity is certainly sufficient to fit all A+A and even p+A, data,
but is it really necessary, i.e., is it a unique property of sQGP?

I discuss **basic** pQCD interference phenomena from beam jet color antenna arrays that may help unravel current BES+DA+pA vs AA puzzles without requiring perfect fluid hydrodynamic or CGC Glasma diagrams, but only LO Feynmann diagrams.

– The color scintillation antenna (CSA)

M. Gyulassy, P. Levai, I. Vitev, and T. Biro, arXiv:1405:7825

Non-Abelian Bremsstrahlung and Azimuthal Asymmetries in High Energy p+A Reactions

M. Gyulassy,^{1,2,*} P. Levai,¹ I. Vitev,³ and T. Biro¹

¹*MTA WIGNER Research Centre for Physics, RMI, Budapest, Hungary*

²*Department of Physics, Columbia University, New York, NY 10027, USA*

³*Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA*

(Dated: May 30, 2014)

- 1) Multiple resolved clusters of recoiling target beam jets together with the projectile beam produces color scintillation antenna (CSA) array
- 2) The scaling of intrinsically azimuthally and long range in η nature of the non-abelian bremsstrahlung leads to v_n moments, entirely due to non-abelian wave interference phenomena sourced by CSA

– Vitev-Gunion-Bertch multiple interaction pQCD bremsstrahlung

- 1) The dynamical source that could partially account for the azimuthal moment systematics may be traced to a basic perturbative QCD feature
- 2) The pQCD based model, the opacity 1 Gunion-Bertch pQCD bremsstrahlung, has been extended to all orders in opacity
- 3) Vitev-Gunion-Bertch bremsstrahlung naturally leads on an event-by-event basis to a hierarchy of non-trivial azimuthal asymmetry moments similar to those observed in p+A and peripheral A+A at fixed $dN/d\eta$

Higher harmonic flow **Fourier starts at n=1**

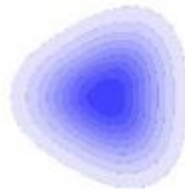


$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left(1 + \sum_{n=2} (2v_n \cos[n(\phi - \psi_n)]) \right)$$

When including fluctuations, all moments appear:



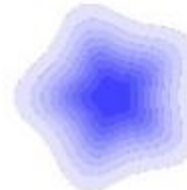
$n = 2$



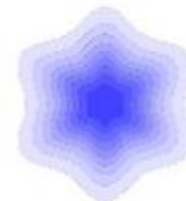
$n = 3$



$n = 4$



$n = 5$



$n = 6$

also v_1 and $n > 6$

Compute $v_n = \langle \cos[n(\phi - \psi_n)] \rangle$

with the event-plane angle $\psi_n = \frac{1}{n} \arctan \frac{\langle \sin(n\phi) \rangle}{\langle \cos(n\phi) \rangle}$

Part 1: case for perfect fluidity with CGC IS

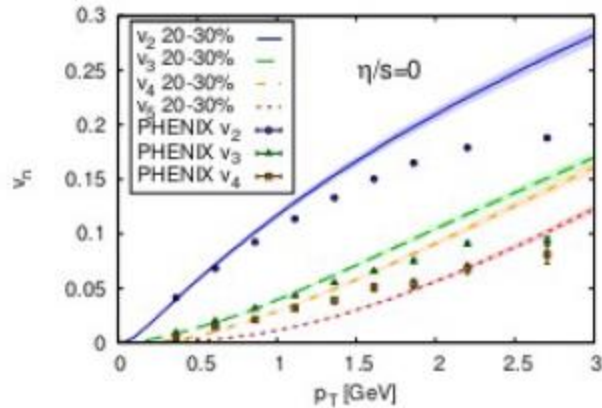
Using higher harmonics to determine η/s

Viscosity/entropy
Of perfect fluid QGP

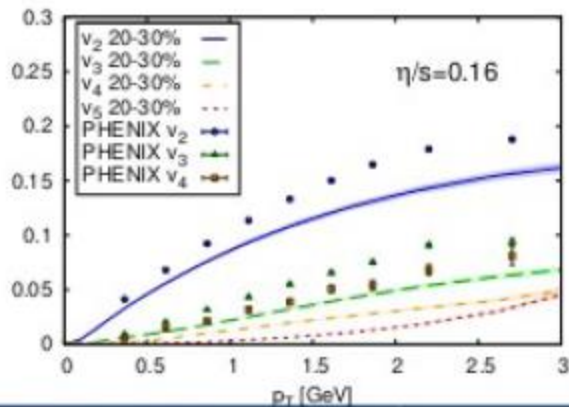
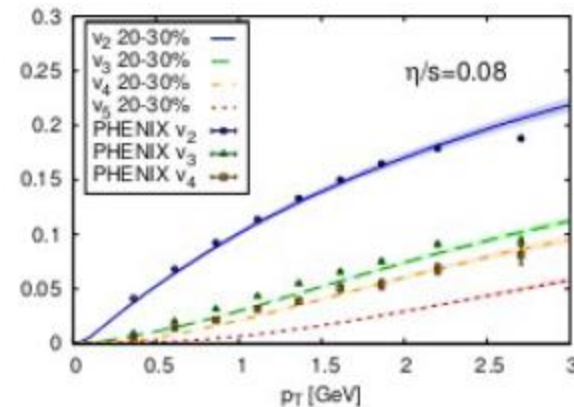


B. Schenke, S. Jeon, C. Gale, arXiv:1109.6289

Data is from event-plane method. Calculations are $\sqrt{\langle v_n^2 \rangle}$.



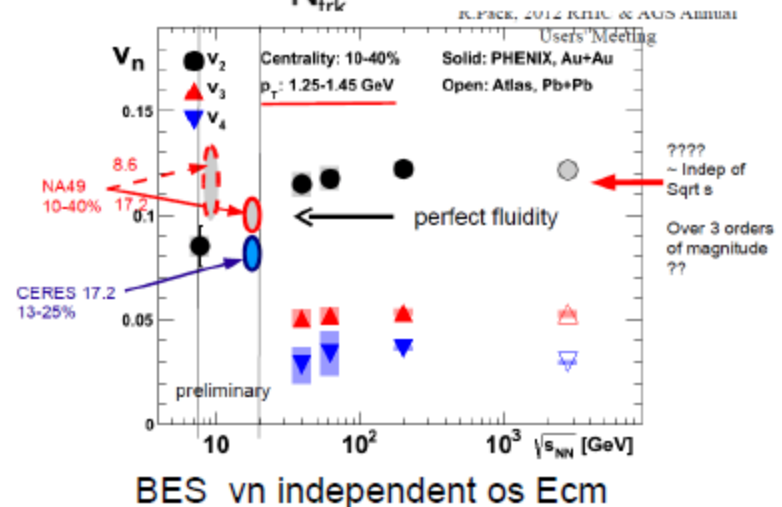
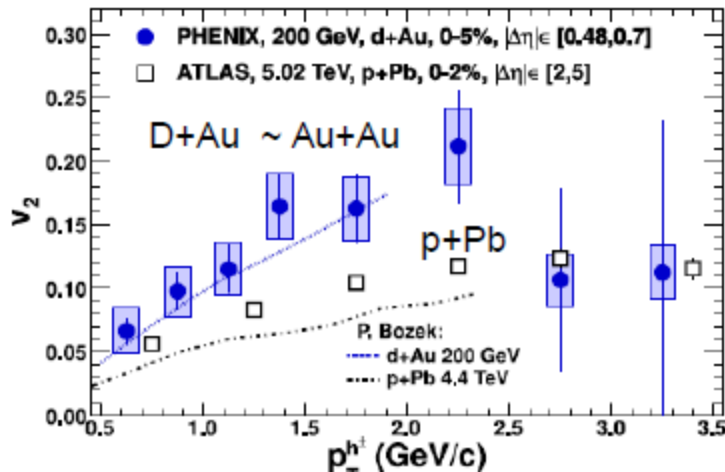
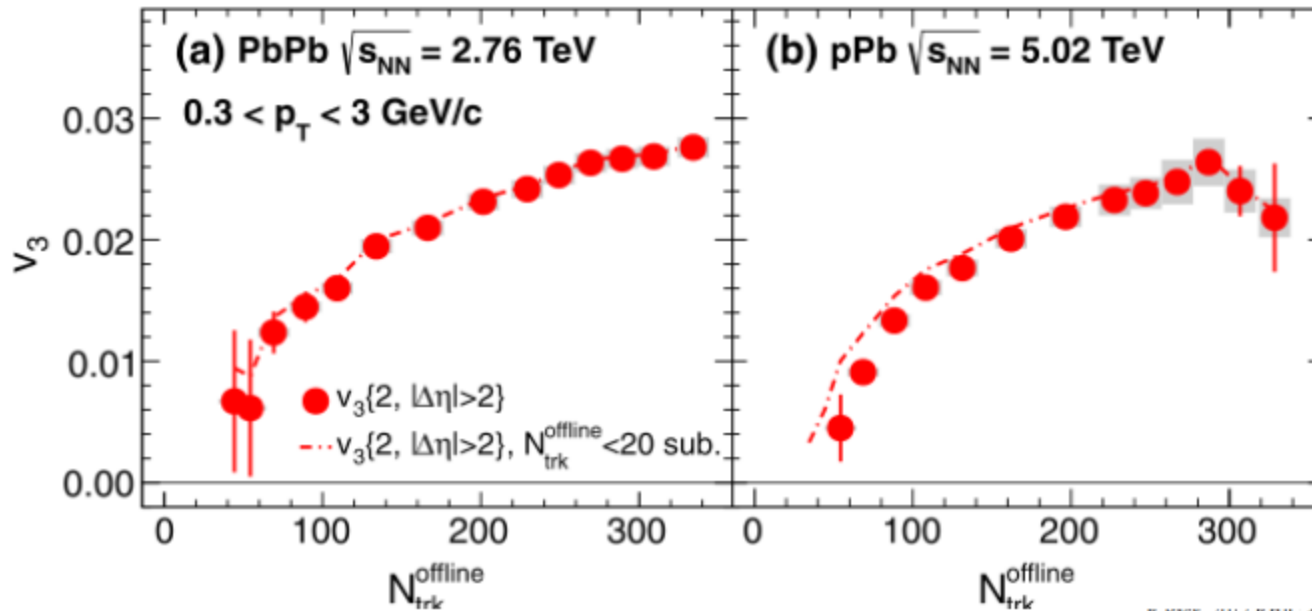
MC-Glauber initial conditions



This is promising.
Need systematic study of all v_n as
function of initial conditions,
granularity, η/s , ...

Experimental data: PHENIX, arXiv:1105.3928

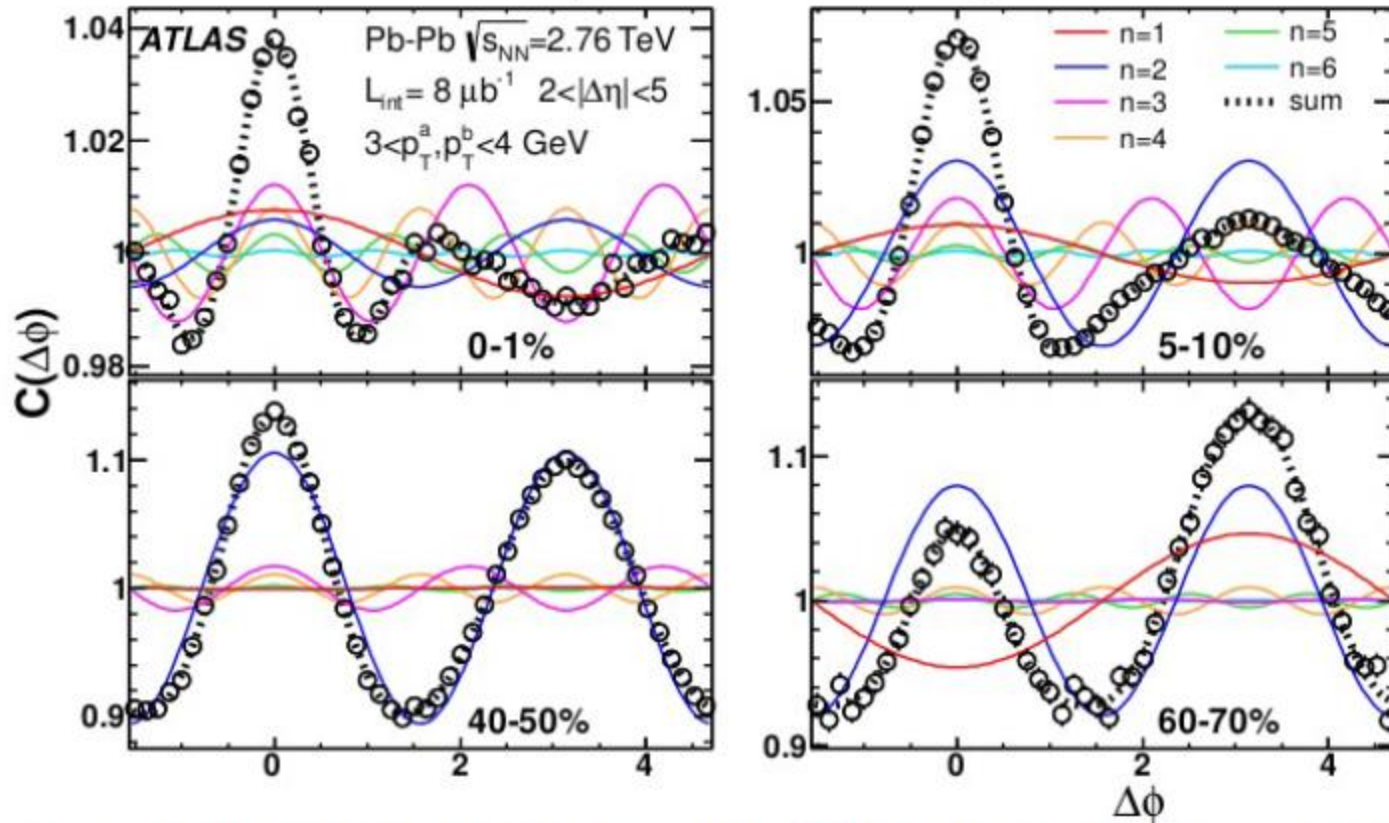
QM12 p(D) + A & BES surprises: $v_3(p+Pb) = v_3(Pb+Pb)$; $v_2(D+Au) = v_2(Au+Au)$; Ecm independent



Another surprise : v_1

[ATLAS Collaboration], PRC86, 014907 (2012)

PQCD Color Scintillations or Lumpy CGC perfect hydro response ?
or complex combo of many effects?



The magnitude of $v_1, 1 = \langle \cos[\phi_1 - \phi_2] \rangle$ **Red** is large for $p_1 \sim p_2 \sim 3-4$ GeV

After subtracting dijets and mom.consv a new rapidity even Dipole!

MGvnlascv 5/20/14 OM14

Fuctuating Dipole can also appear

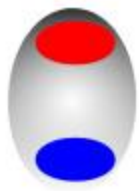


Higher harmonic flow **Fourier starts at n=1**



$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left(1 + \sum_{n=1} (2v_n \cos[n(\phi - \psi_n)]) \right)$$

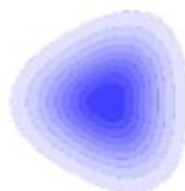
When including fluctuations, all moments appear:



n=1



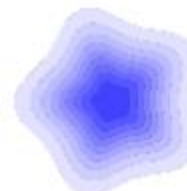
n = 2



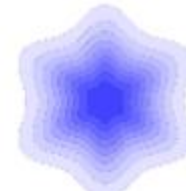
n = 3



n = 4



n = 5



n = 6

also v_1 and $n > 6$

Compute $v_n = \langle \cos[n(\phi - \psi_n)] \rangle$

with the event-plane angle $\psi_n = \frac{1}{n} \arctan \frac{\langle \sin(n\phi) \rangle}{\langle \cos(n\phi) \rangle}$

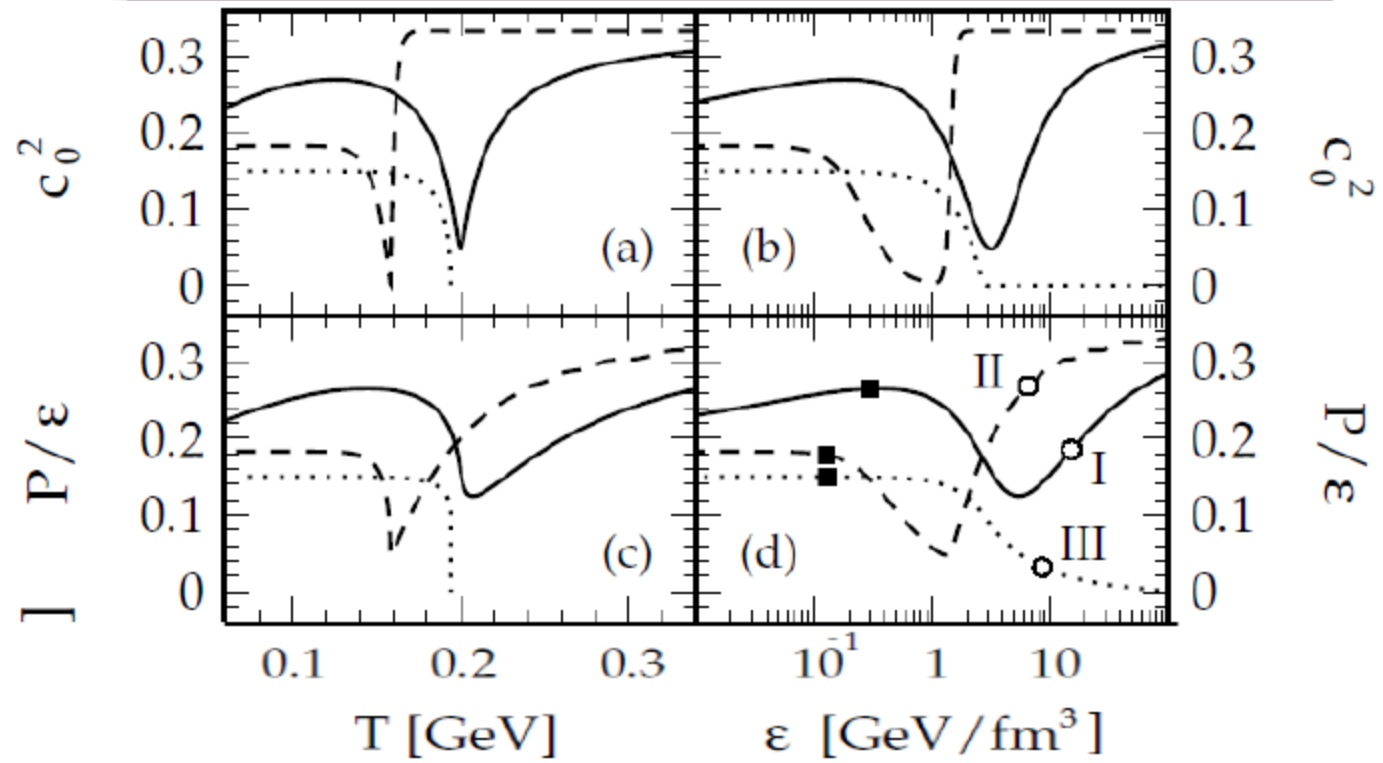
[! Danger ! Hydro can fit anything]

B.R. Schlei, D. Strottman, N. Xu

158-GeV/A Pb + Pb

[Nucl-th/9801045](#); [9710047](#), [9706037](#)

Ideal Landau 3D Hydro with different EOS I (solid), II (dashed), III(dotted)



NA44 and NA49 data could be post-dicted with Ideal relativistic hydrodynamics with **ANY Equation of State**

Given freedom to adjust **Initial** and **Freeze-out** Conditions

Mathematician's delight can be Physicist's Nightmare

K. Weierstrass (1885) Theorem:

“Über die analytische Darstellbarkeit sogenannter willkürlicher Functionen einer reellen Veränderlichen’

Sitzungsberichte der Königlich Preußischen Akademie der Wissenschaften zu Berlin, 1885 (II).

If f is a continuous real-valued function defined on the set $[a,b] \times [c,d]$ and $\varepsilon > 0$, then **there exists a polynomial function** in two variables such that

$|f(x,y) - p(x,y)| < \varepsilon$
for all x in $[a,b]$ and y in $[c,d]$.



Weierstrass

Corrolary 1: Fourier transforms exists



Corrolary 2: ideal hydro can fit anything

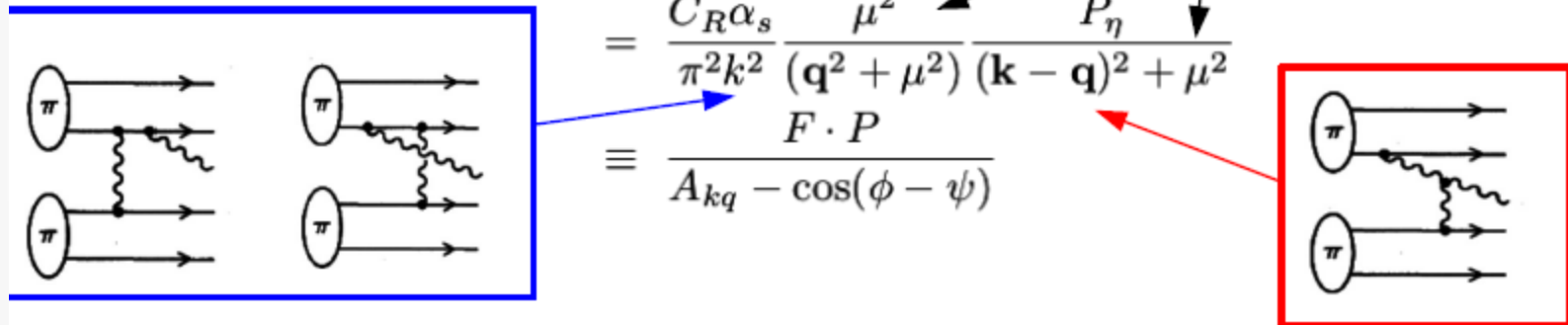


II. FIRST ORDER IN OPACITY (GB) BREMSSTRAHLUNG AND AZIMUTHAL ASYMMETRIES v_n

The above puzzles with BES and $D + Au$ at RHIC and with $p + Pb$ at LHC and models proposed so far motivate us to consider simpler more basic perturbative QCD sources of azimuthal asymmetries. The well known non-abelian bremsstrahlung Gunion-Bertsch (GB) formula[29] for the soft gluon radiation single inclusive distribution is

$$\begin{aligned}
 \frac{dN_g^{(1)}}{d\eta d^2\mathbf{k} d^2\mathbf{q}} &\equiv f(\eta, \mathbf{k}, \mathbf{q}) \\
 &= \frac{C_R \alpha_s}{\pi^2 k^2} \frac{\mu^2}{(\mathbf{q}^2 + \mu^2)} \frac{P_\eta}{(\mathbf{k} - \mathbf{q})^2 + \mu^2} \\
 &\equiv \frac{F \cdot P}{A_{kq} - \cos(\phi - \psi)}
 \end{aligned}$$

Color Dipole Form factor



Gluon Bremsstrahlung peaks in transverse direction near net momentum transfer $\vec{Q} = (Q, \Psi)$ that also defined reaction Event Plane (EP)

Basic Non-Abelian feature: uniform *rapidity-even* distributed (unlike QED)

Of course also peaks in beam direction $1/k^2$ (as in QED)

– Conclusions

M. Gyulassy, P. Levai, I. Vitev, and T. Biro, arXiv:1405:7825

- 1) The color scintillation antenna (CSA) arrays radiate gluons with characteristic boost non-invariant trapezoidal rapidity distributions in asymmetric nuclear collisions
- 2) Non-abelian beam jet CSA bremsstrahlung may provide a partial analytic solution to the beam energy scan discovery of the near energy independence of the azimuthal moments down to very low CM energy of ~ 10 AGeV, where large x valence quarks beam jet dominate inelastic dynamics
- 3) The uniqueness of the perfect fluid description of p+A cannot be taken for granted