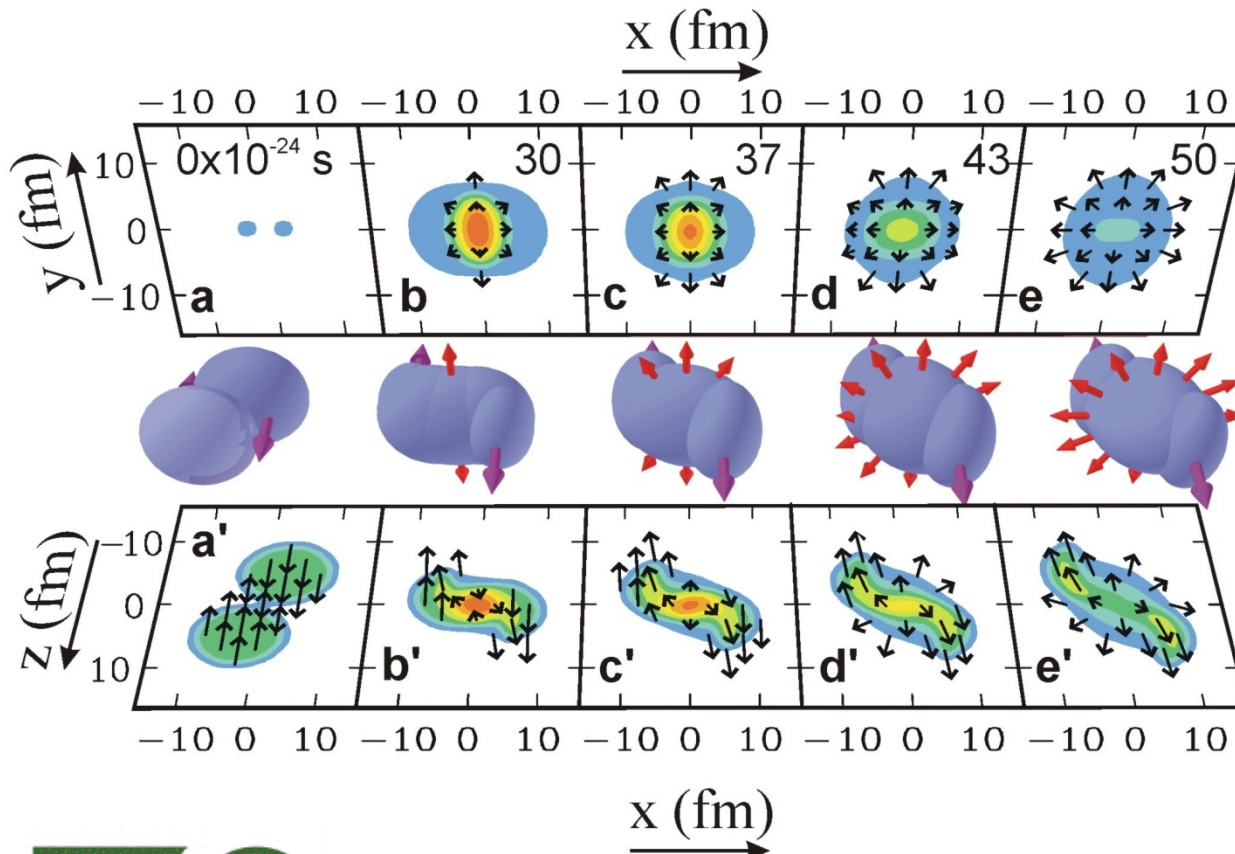


Experimental Observables to study the nuclear symmetry energy with Heavy Ion Collision



Heavy Ion Meeting

April 13, 2012

Pohang, Korea



Betty Tsang
The National Superconducting
Cyclotron Laboratory
Michigan State University





The National Superconducting Cyclotron Laboratory

Michigan State University

U.S. flagship user facility for rare isotope research and education in nuclear science, astro-nuclear physics, accelerator physics, and societal applications



USA

State and Capital



San Francisco

Los Angeles

Chicago

New York City

C A N A D A

MEXICO

CANADA

Pacific Ocean

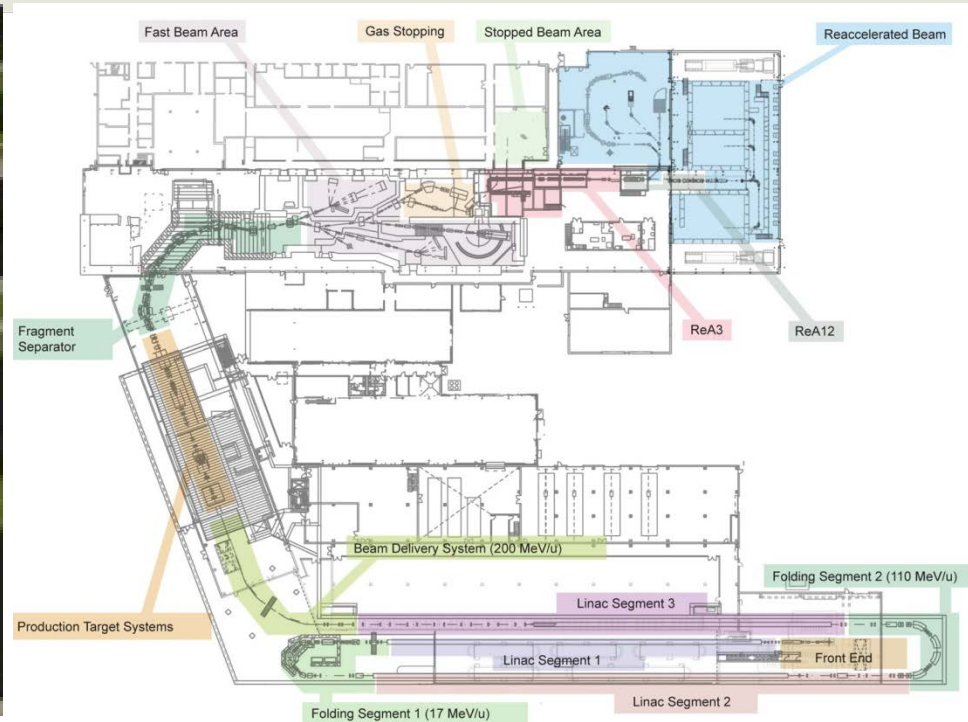
Pacific Ocean

0 100 200 400 600 800



Michigan State University

Facility for Rare Isotope Beams (FRIB)



FRIB will provide intense beams of rare isotopes (that is, short-lived nuclei not normally found on Earth). FRIB will enable scientists to make discoveries about the properties of these rare isotopes in order to better understand the physics of nuclei, nuclear astrophysics, fundamental interactions, and applications for society.





282 employees, including 24 faculty, 46 graduate, and 51 undergraduate students.
(as of March 05)

489 employees, including 40 faculty, 64 graduate and 70 undergraduate students
as of August 16, 2011



Facility for Rare Isotope Beams (FRIB)



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Nuclear Equation of State

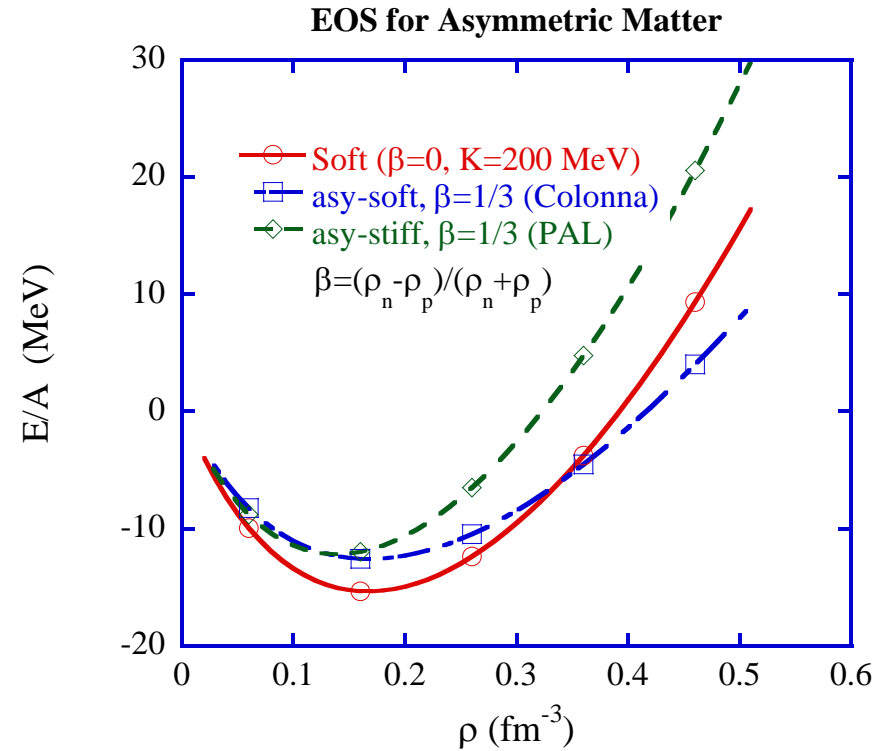
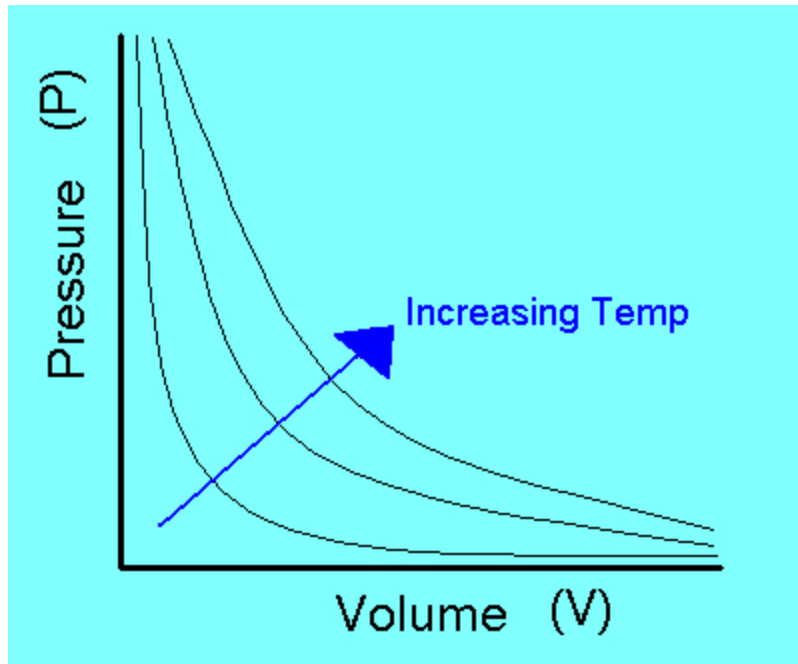
$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho)$$
$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N - Z) / A$$

Research with rare isotope beams

- ✓ *Nuclear Structure – What is the nature of the nuclear force that binds protons and neutrons into stable nuclei and rare isotopes?*
- ✓ *Nuclear Astrophysics – What is the nature of neutron stars and dense nuclear matter? What is the origin of elements heavier than iron in the cosmos? What are the nuclear reactions that drive stars and stellar explosions?*
- ✓ *Tests of Fundamental Symmetries – Why is there now more matter than antimatter in the universe?*

Equation of State (EoS)

Ideal gas: $PV=nRT$

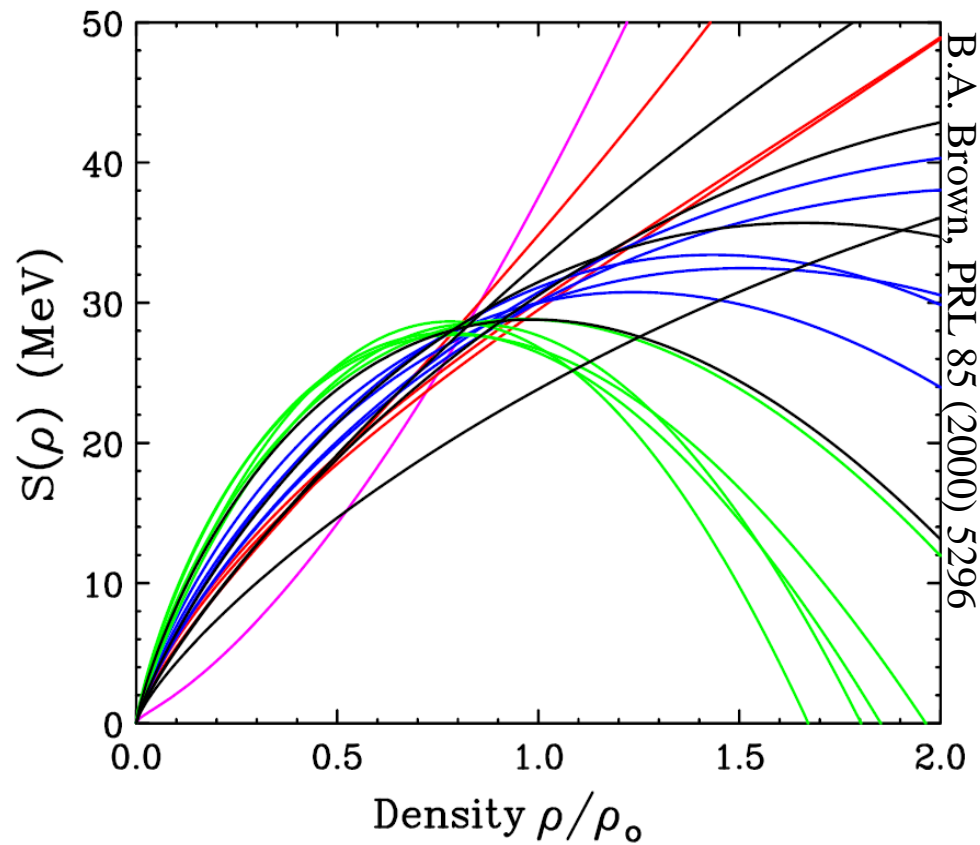
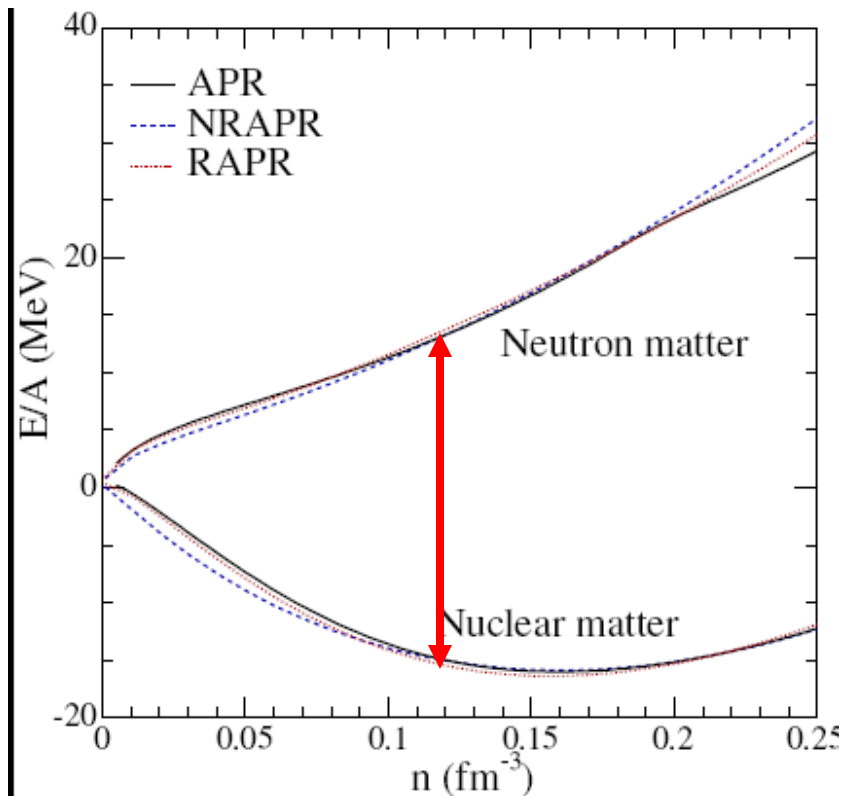


Definition of Symmetry Energy

$$B = a_v A - a_s A^{2/3} + \delta \left[-a_c \frac{Z(Z-1)}{A^{1/3}} - a_{sym} \frac{(A-2Z)^2}{A} \right]$$

$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho);$$

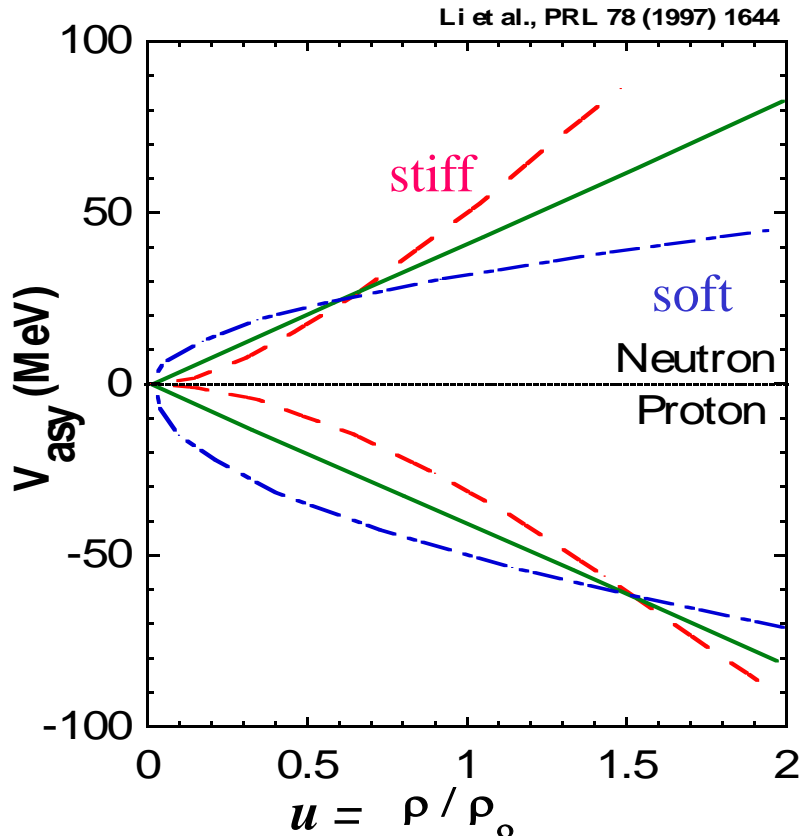
$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N-Z)/A$$



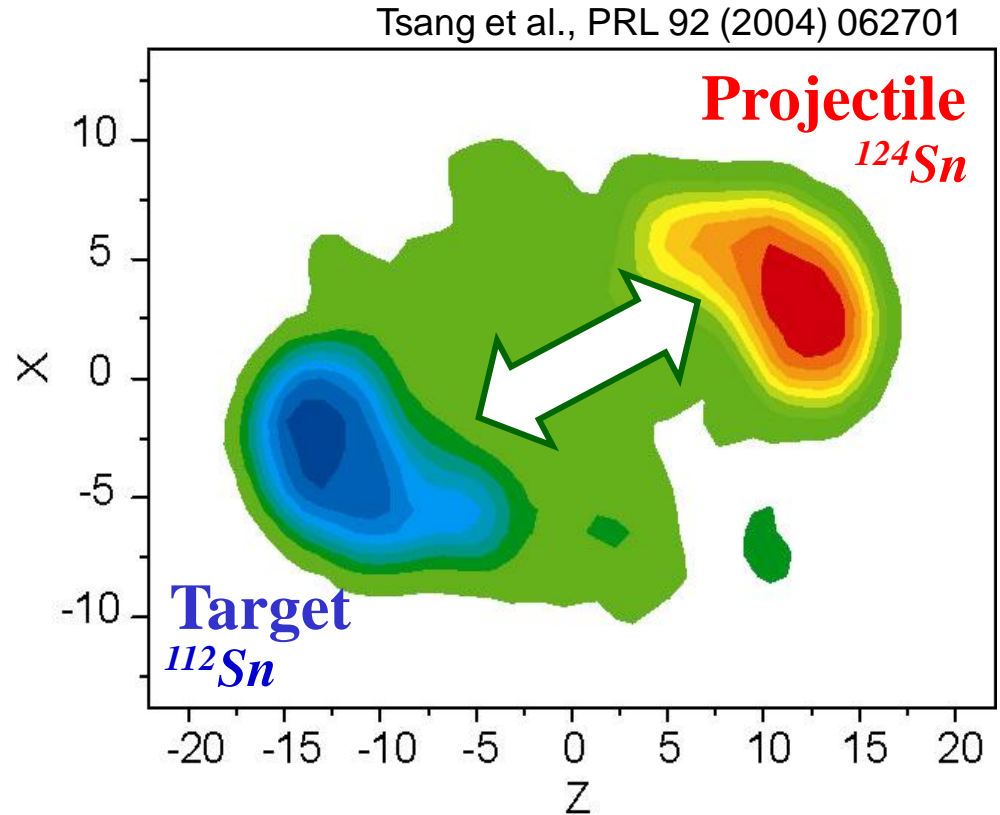
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Two observables: n/p ratios and isospin diffusion



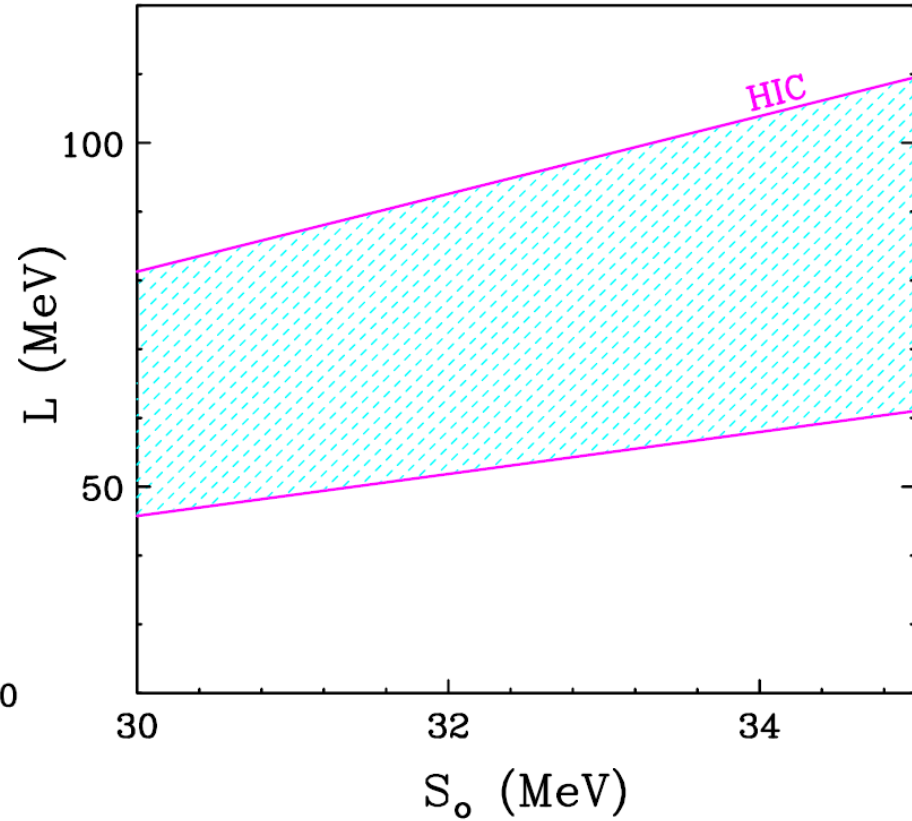
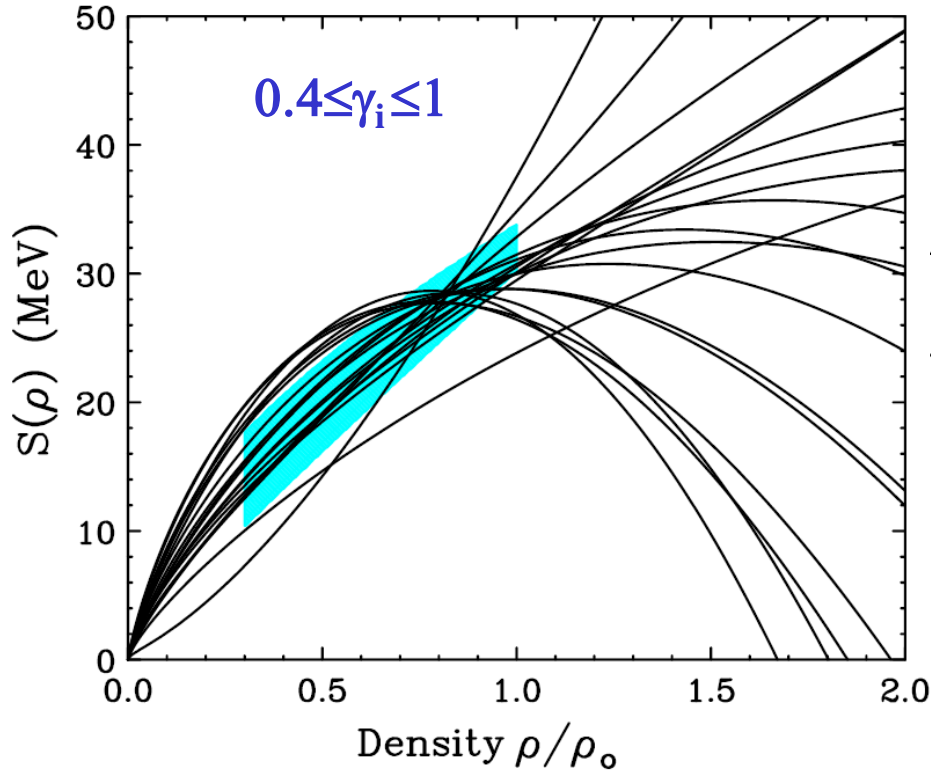
$Y(n)/Y(p)$; $t/{}^3\text{He}$, π^+/π^-



Isospin Diffusion; low ρ , E_{beam}

Symmetry energy constraints from HIC

arXiv:1204.0466

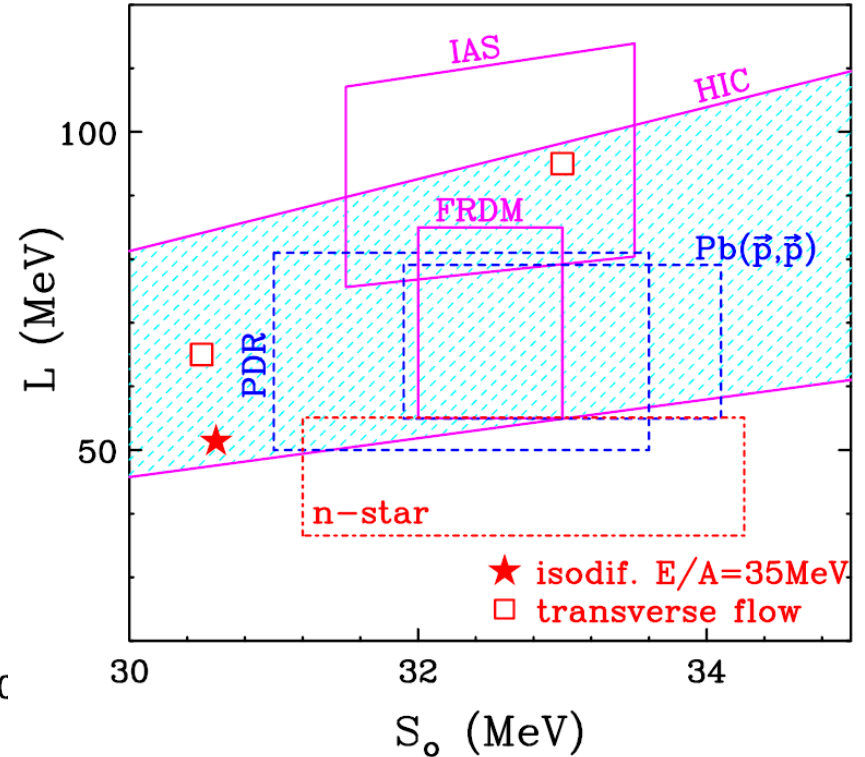
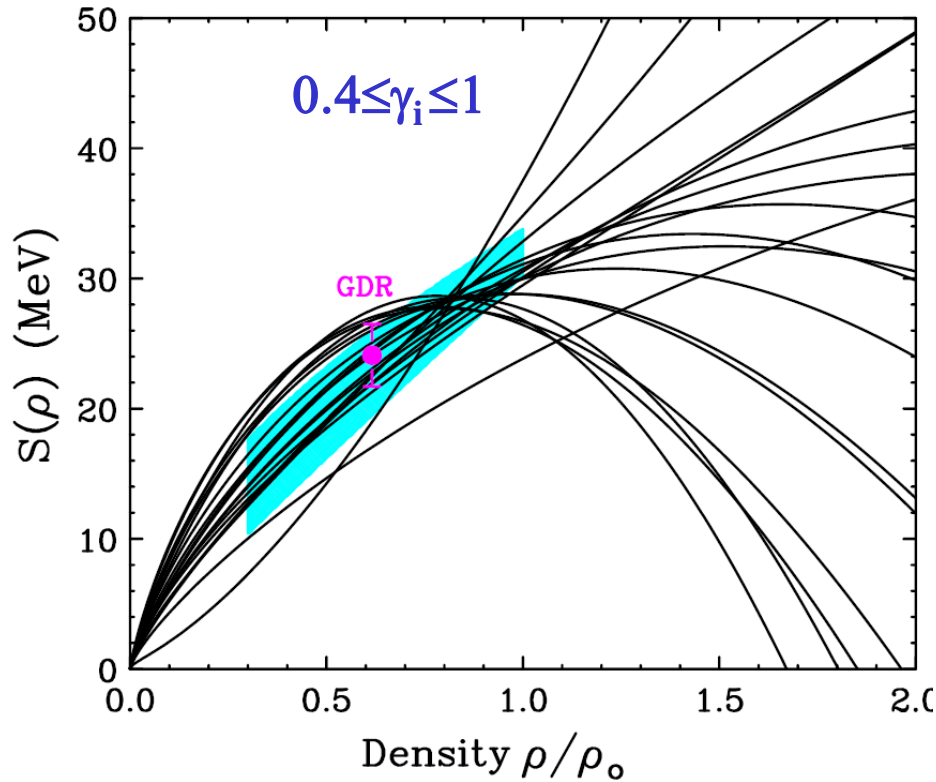


$$E_{sym} = S_o + \frac{L}{3} \left(\frac{\rho_B - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

$$L = 3\rho_0 \left. \frac{\partial E_{sym}}{\partial \rho_B} \right|_{\rho_B = \rho_0} = \frac{3}{\rho_0} P_{sym}$$

Symmetry energy constraints from HIC

arXiv:1204.0466

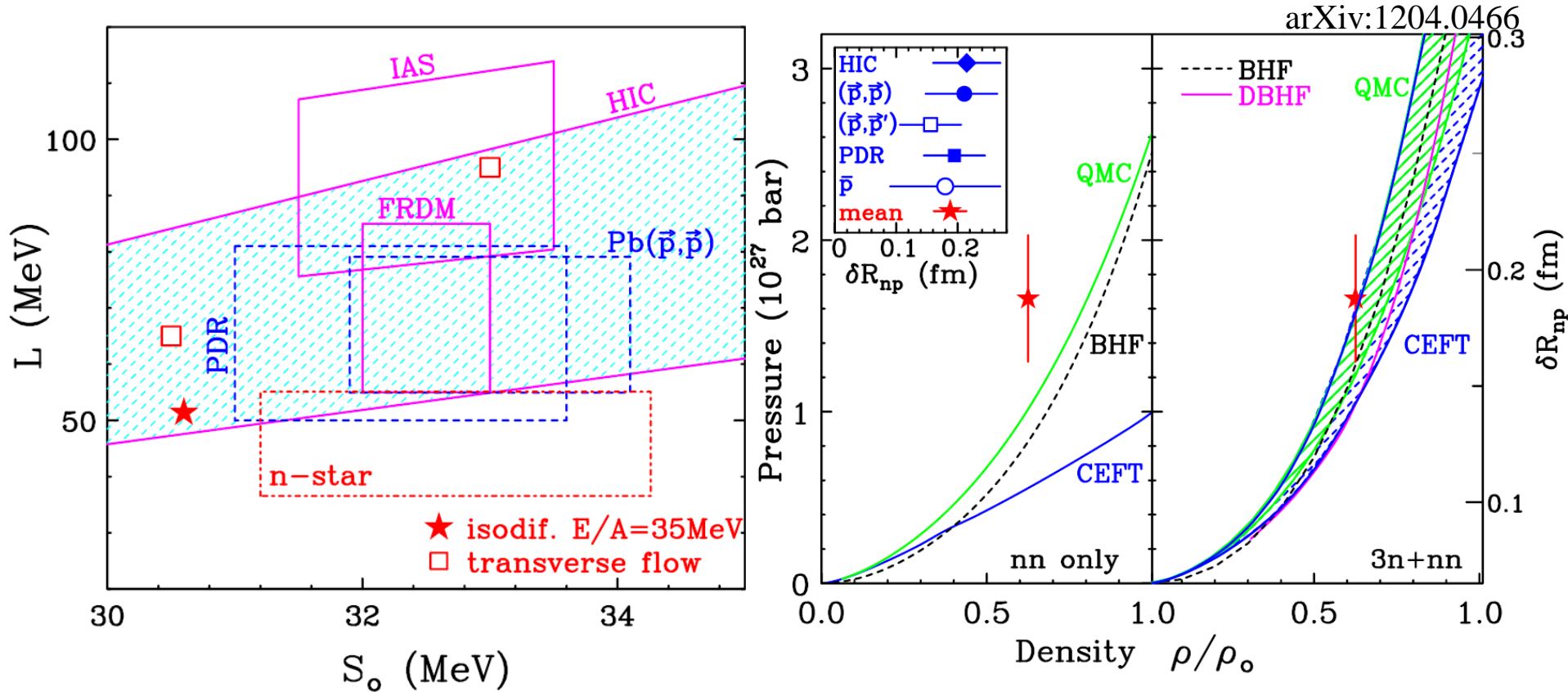


$$E_{sym} = S_o + \frac{L}{3} \left(\frac{\rho_B - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

$$L = 3\rho_0 \left. \frac{\partial E_{sym}}{\partial \rho_B} \right|_{\rho_B = \rho_0} = \frac{3}{\rho_0} P_{sym}$$

HIC has been successful in obtaining constraints on the symmetry energy at $0.3 < \rho/\rho_0 < 1$

Summary

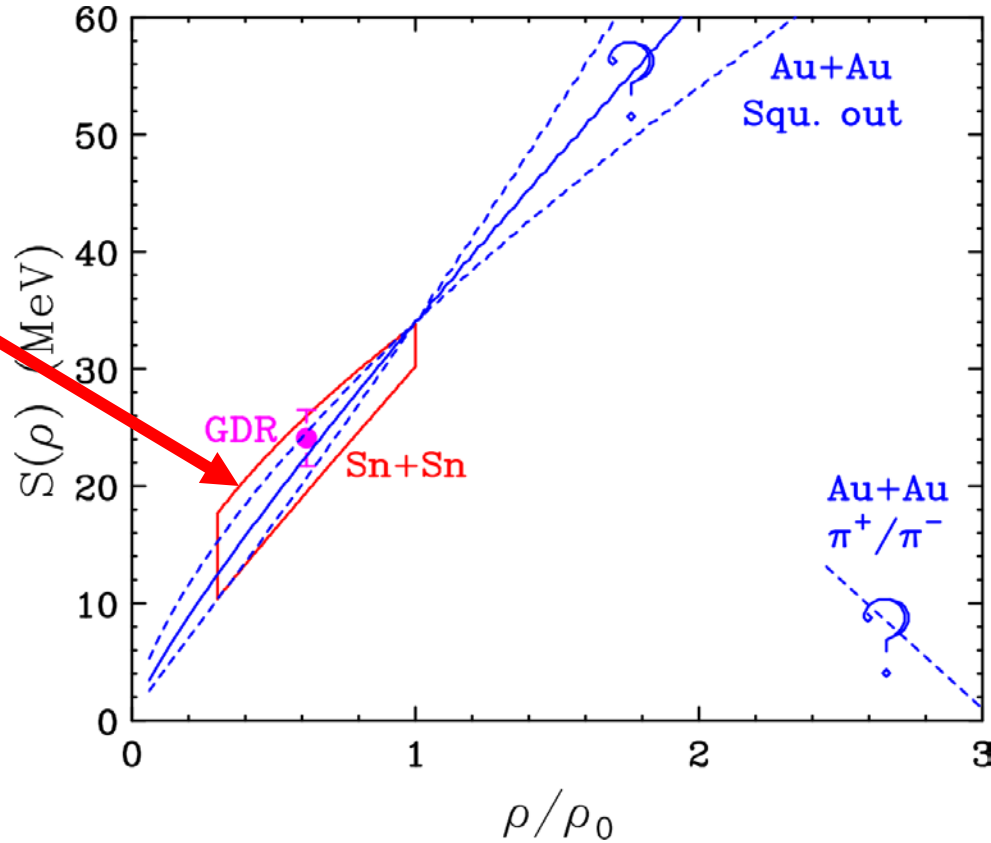
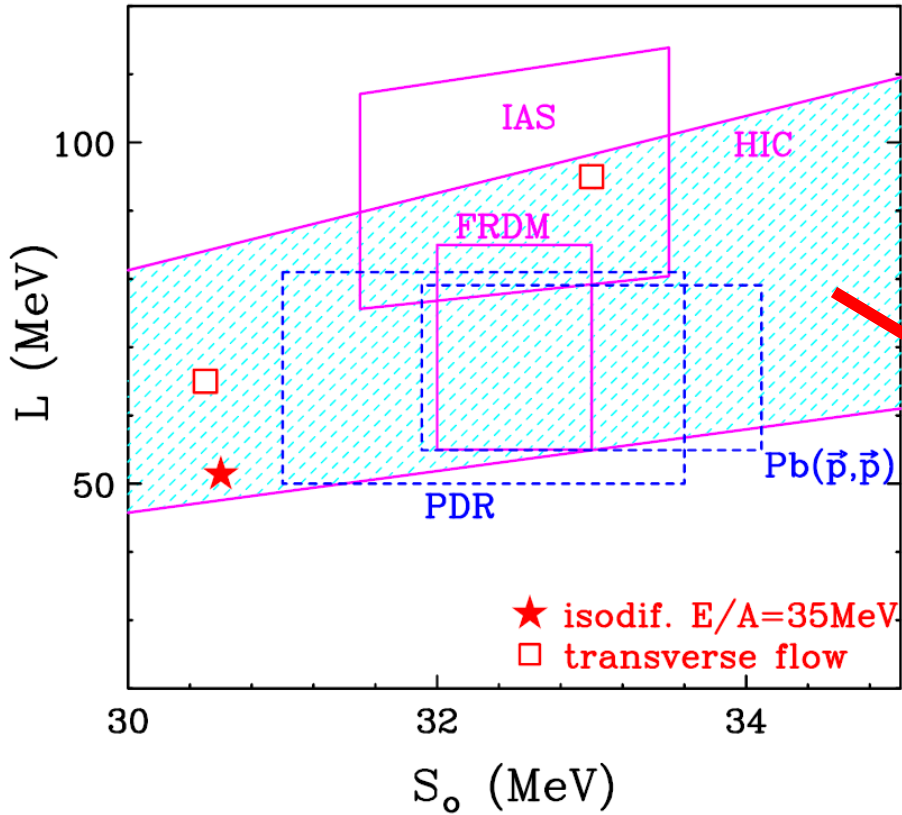


Symmetry Energy constraints for $0.3 < \rho/\rho_0 < 1$ are consistent even though different experimental techniques and theories are involved.

3n force is needed in the description of EoS of pure n-matter.

Challenges: Constraints on the density dependence of symmetry energy at supra normal density

arXiv:1204.0466



Xiao et al., PRL102, 062502 (2009)
 Russotto et al., PL B697 (2011) 471

HIC has been successful in obtaining constraints on the symmetry energy at $0.3 < \rho/\rho_0 < 1$

Lessons learned from LE measurements:

1. HI collision dynamics are complex but prove to be sensitive to density dependence of symmetry energy.
2. Need multiple observables to verify results and to add credibility to the constraints
3. Problems still remain, e.g.
 - How to extract results to $T=0$;
 - Control of input parameters in transport models.
4. Provide guidance to the experiments at high energy

Talk Outline

1. Review of LE experimental observables
2. Discussions of HE experimental observables and experiments at RIKEN, KoRIA & FRIB

How to obtain the information about EoS?

Both astrophysical and laboratory observables can constrain the EoS, $\varepsilon(\rho, T, \delta)$ or $P(\rho, T, \delta)$ indirectly.

Experiments:

Accelerator: Projectile, target, energy

*Detectors: Information of emitted particles – identity, spatial info, energy, yields
→ construct observables*

Models

Input: Projectile, target, energy.

Simulate the collisions with the appropriate physics

Success depends on the comparisons of observables.

What are the experimental challenges?

What are the theory challenges?

Density Dependence of Symmetry Energy

Density region sampled depends on reaction mechanisms (impact parameter) & beam energy

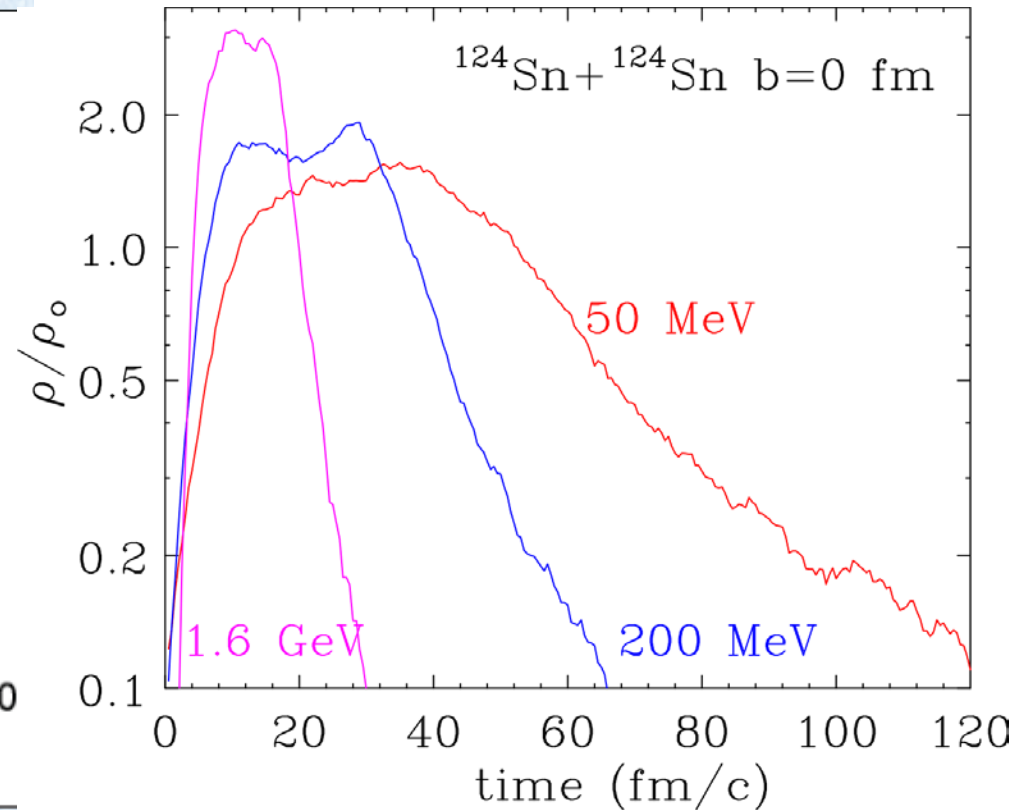
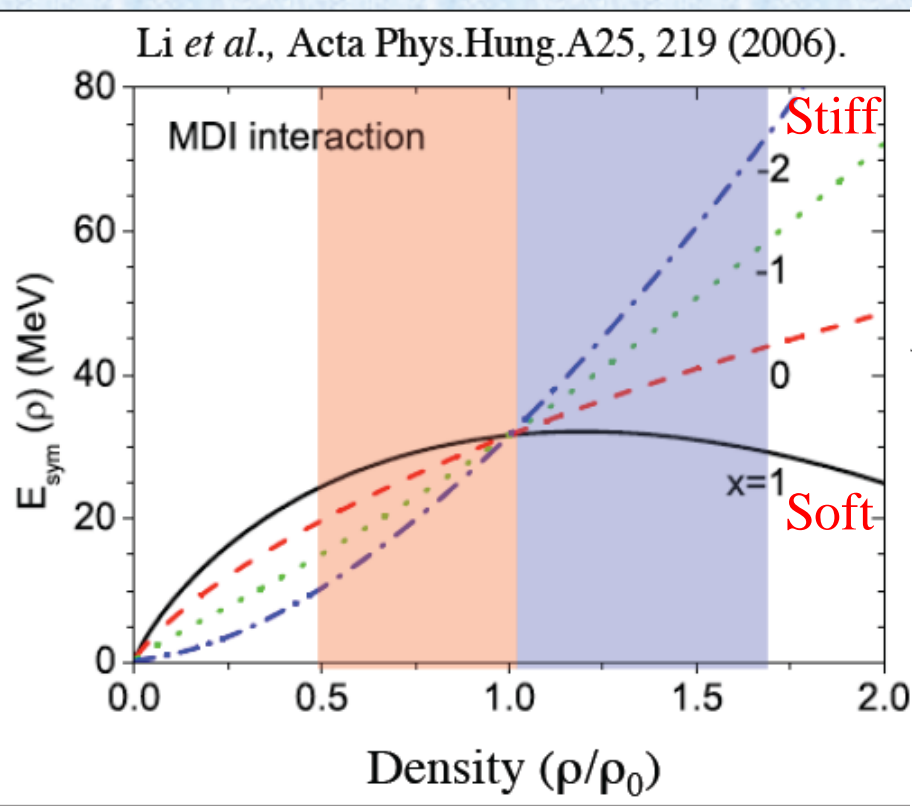
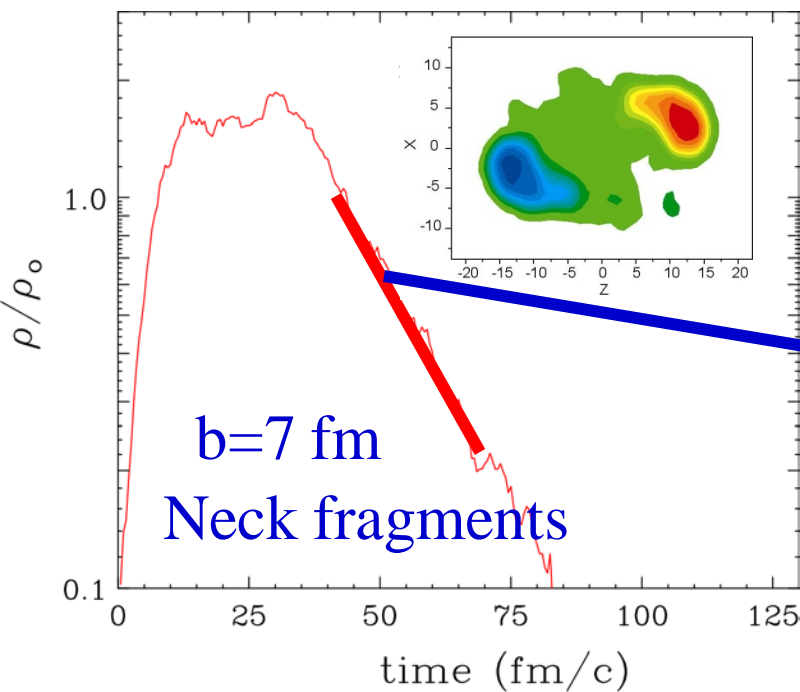
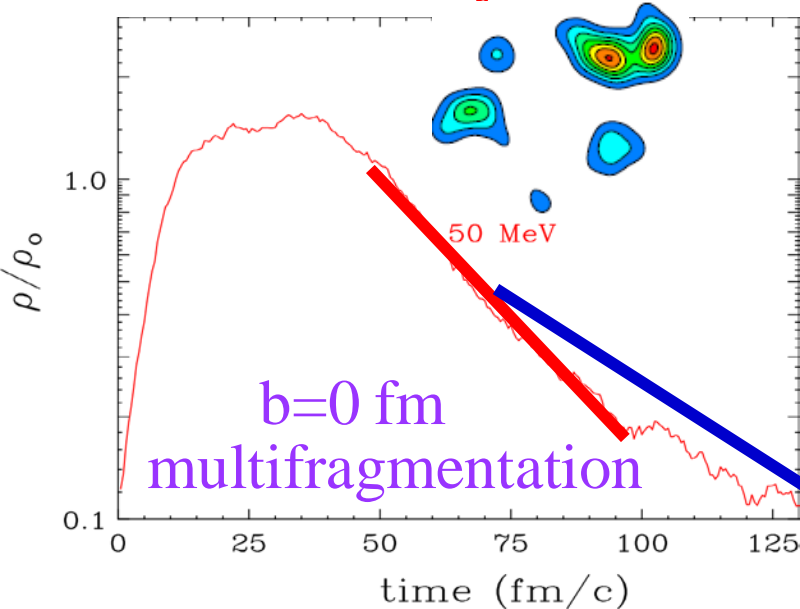


Figure credit : A. Bickley

Observables:

- $\rho < \rho_0$: Isospin diffusion, n/p ratios. flow and observables from NS.
- $\rho > \rho_0$: HIC the only game in town: n/p , $t/{}^3\text{He}$, flow, p^+/p^- ratio

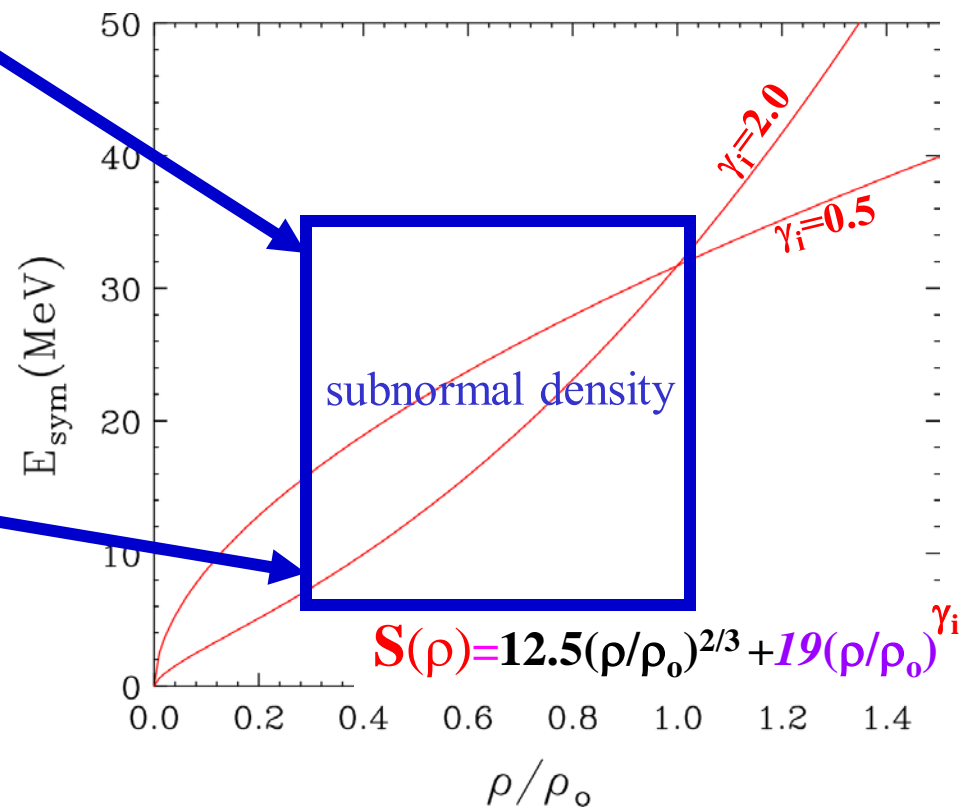
Heavy Ion collision: $^{124}\text{Sn}+^{124}\text{Sn}$, $E/A=50$ MeV



Reaction mechanism of fragment productions depends on impact parameters

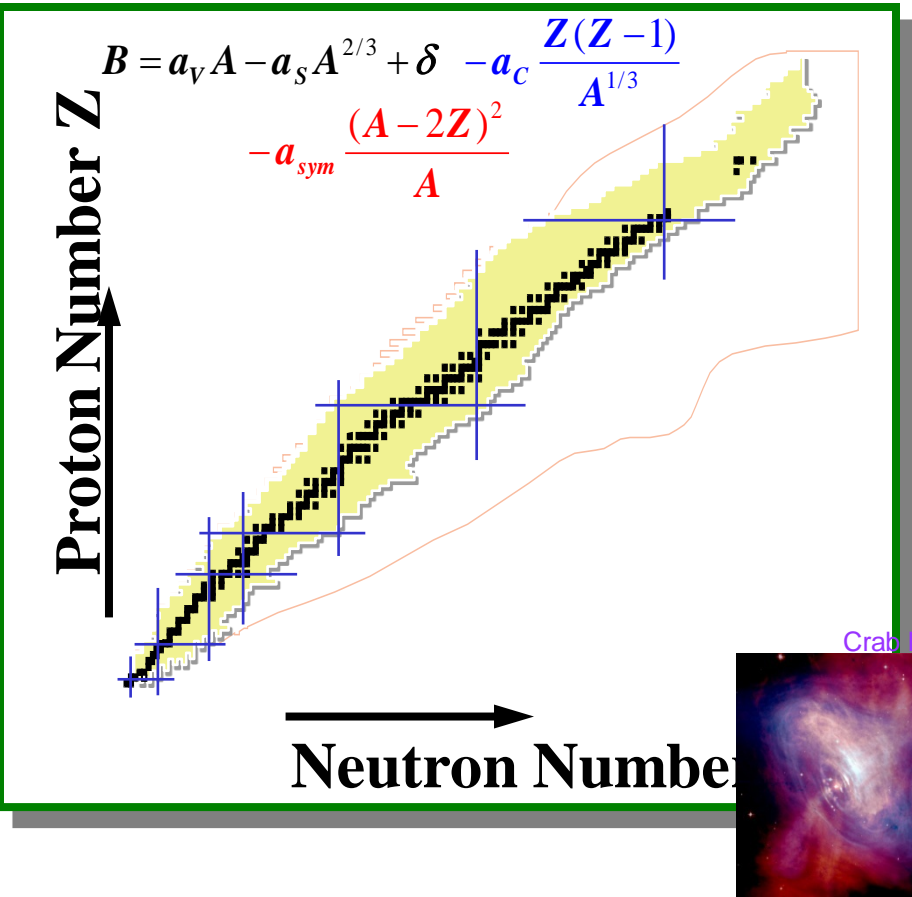
Charged fragments ($Z=3-20$) are formed at subnormal density

Impact parameter selection is a must!



Strategies used to study the symmetry energy with Heavy Ion collisions below $E/A=100$ MeV

Isospin degree of freedom



- Vary the N/Z compositions of projectile and targets
 - $^{124}\text{Sn}+^{124}\text{Sn}$, $^{124}\text{Sn}+^{112}\text{Sn}$, $^{112}\text{Sn}+^{124}\text{Sn}$, $^{112}\text{Sn}+^{112}\text{Sn}$
- Measure N/Z compositions of emitted particles
 - n & p yields
 - isotopes yields – isospin diffusion

Strategies used to study the symmetry energy with Heavy Ion collisions below $E/A=100$ MeV

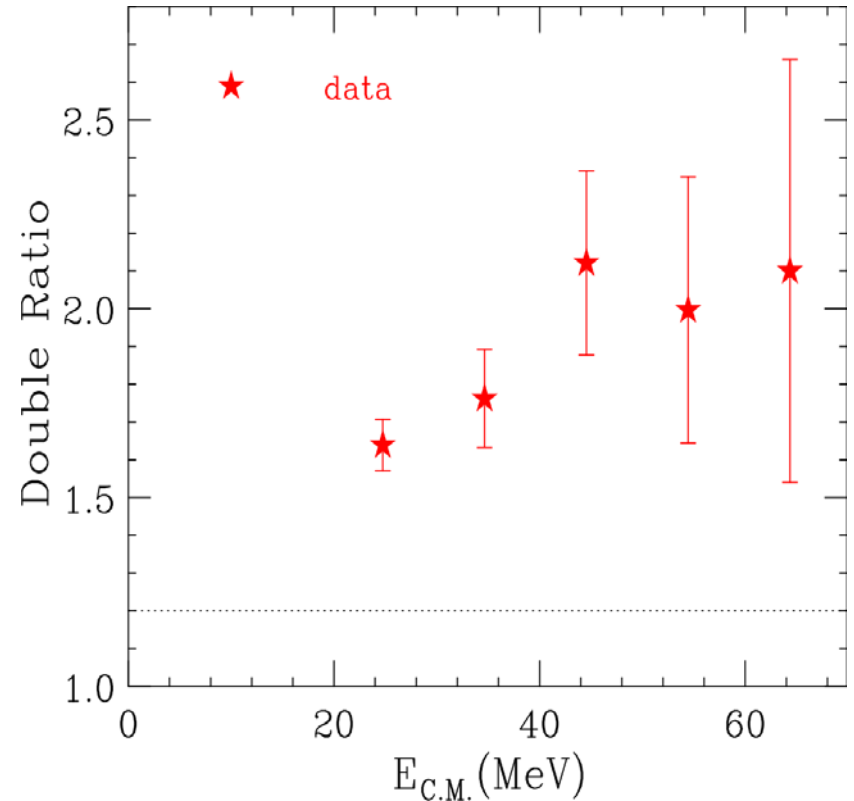
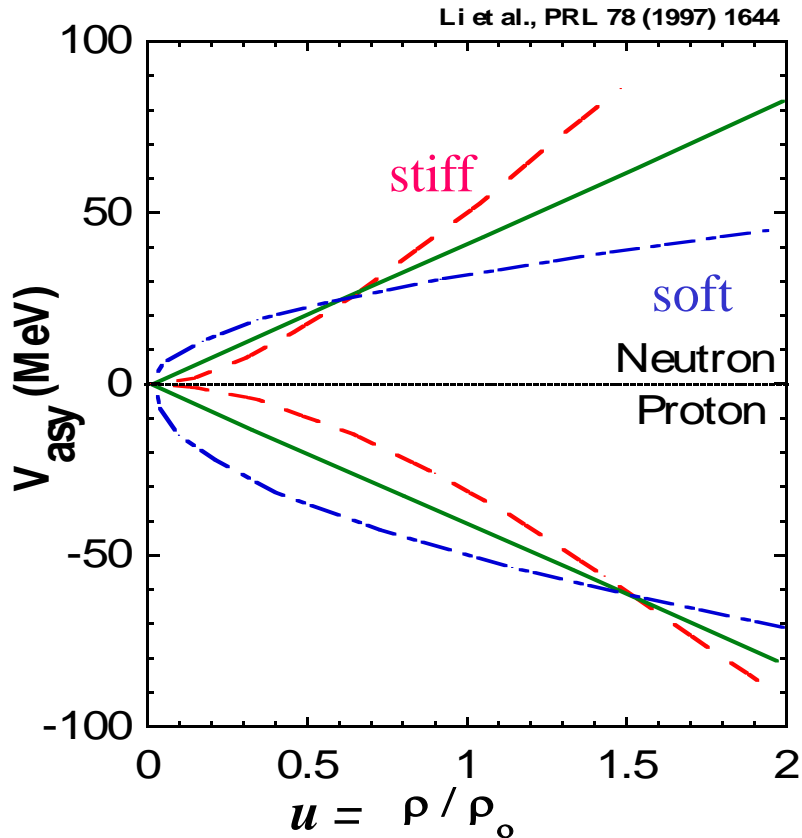
At $E/A > 100$ MeV, $\rho > \rho_0$
Strategies should be
similar but observables
maybe different

- Vary the N/Z compositions of projectile and targets
 $^{124}\text{Sn}+^{124}\text{Sn}$, $^{124}\text{Sn}+^{112}\text{Sn}$,
 $^{112}\text{Sn}+^{124}\text{Sn}$, $^{112}\text{Sn}+^{112}\text{Sn}$
- Measure N/Z compositions of emitted particles
 - n & p yields
 - isotopes yields – isospin diffusion

$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho)$$

$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N - Z) / A$$

Two observables: n/p ratios and isospin diffusion



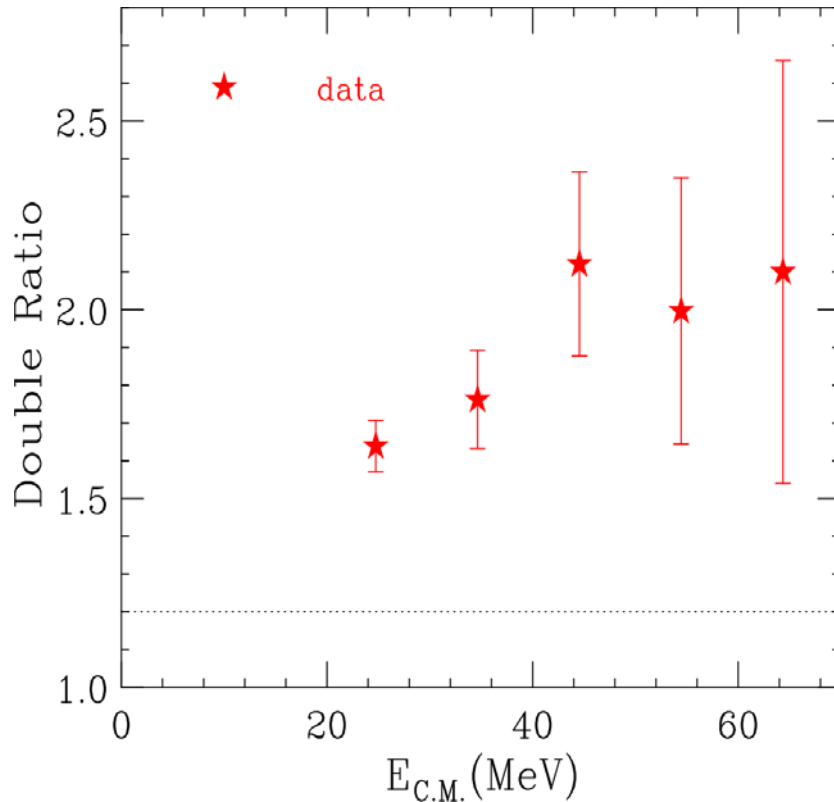
Data : Famiano et al. PRL 97 (2006) 052701

Double Ratio $\Rightarrow \frac{^{124}\text{Sn}+^{124}\text{Sn}; Y(n)/Y(p)}{^{112}\text{Sn}+^{112}\text{Sn}; Y(n)/Y(p)} \Rightarrow \text{minimize systematic errors}$

n/p double yield ratios and flow ratios

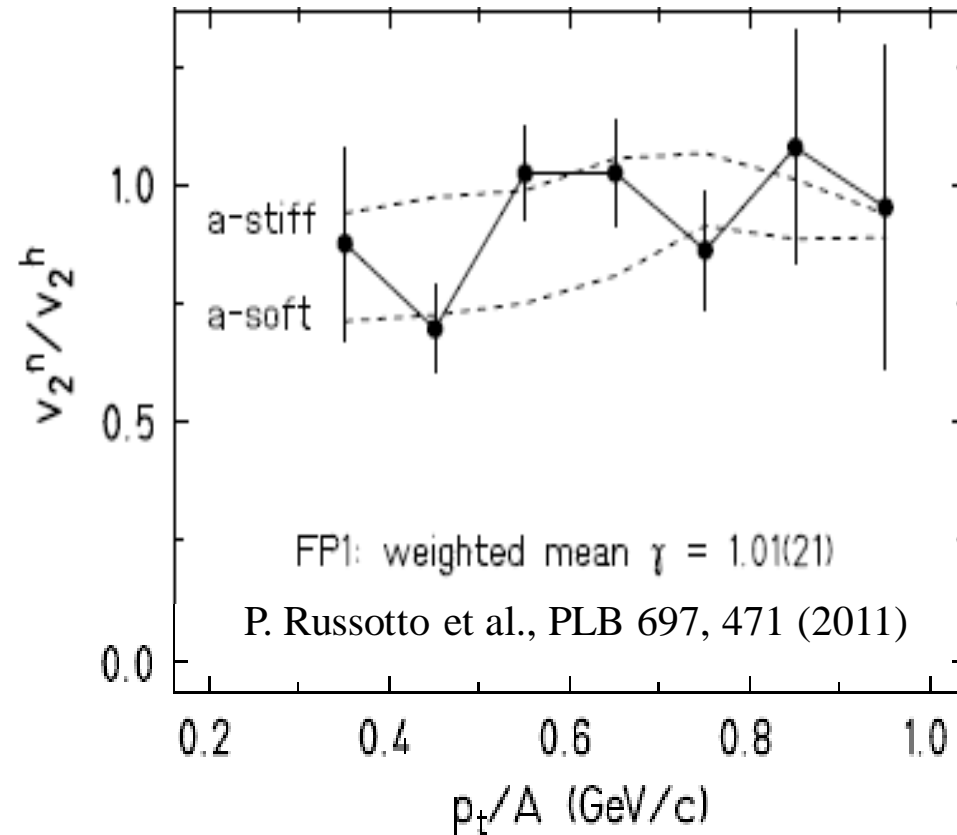
Data : Famiano et al. PRL 97 (2006) 052701

50 A.MeV Sn+Sn



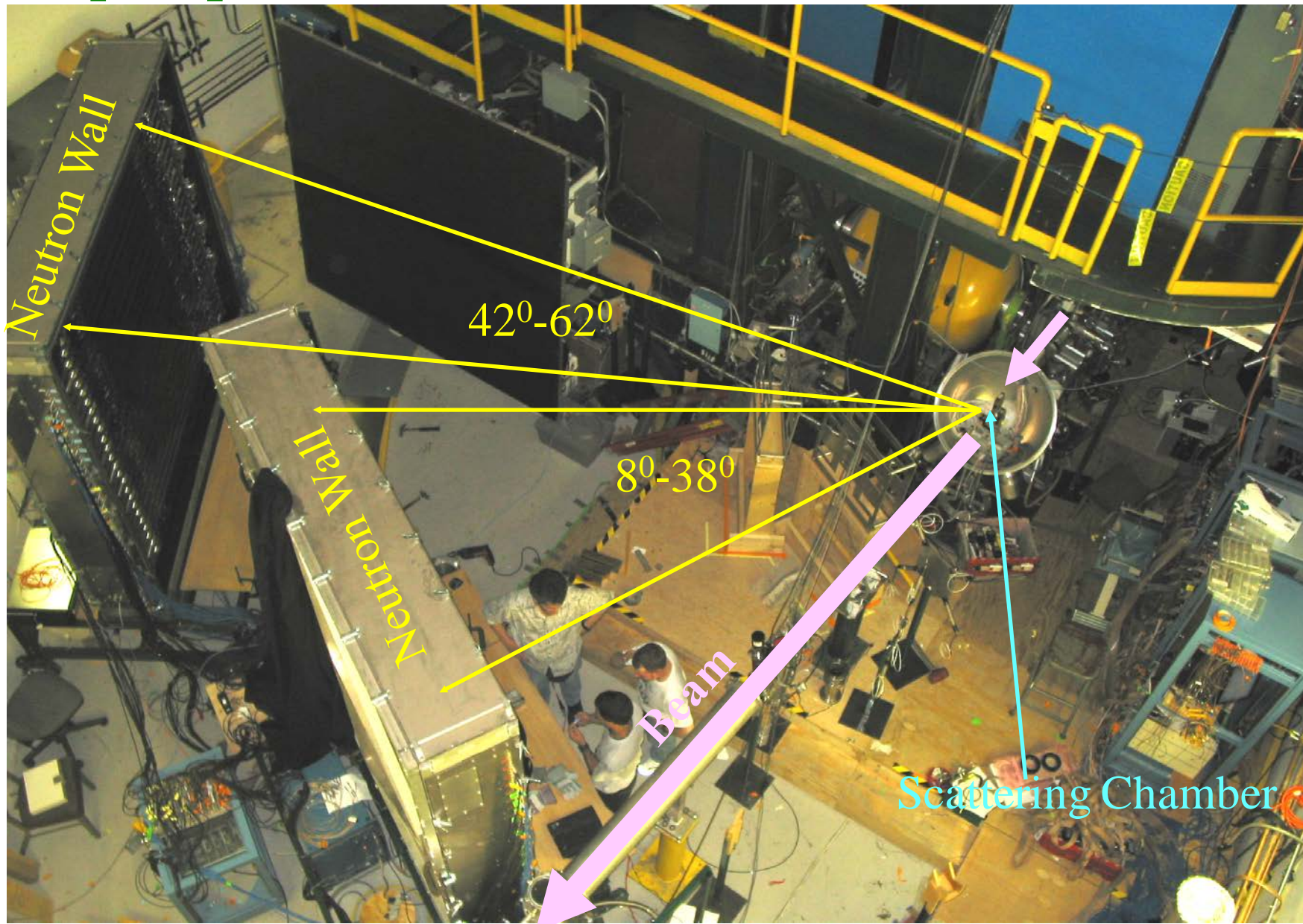
Russotto et al., PL B697 (2011) 471

400 A.MeV Au + Au

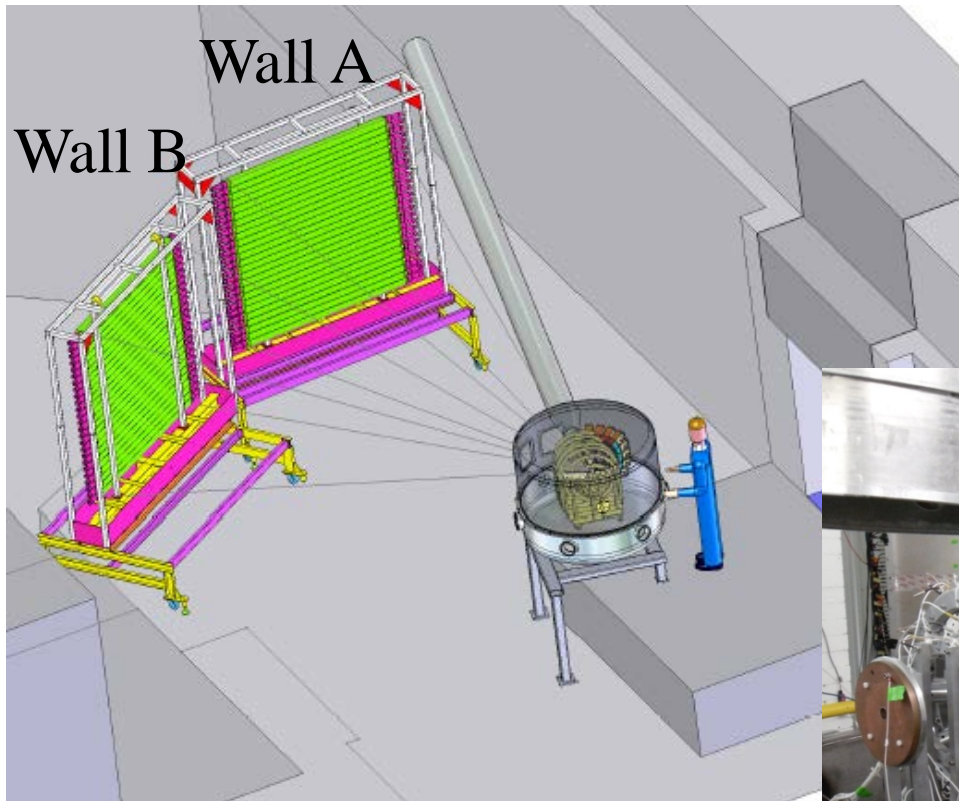


Theorists frustration: large experimental uncertainties!
Results from better designed experiments are coming!

n/p Experiment $^{124}\text{Sn}+^{124}\text{Sn}; ^{112}\text{Sn}+^{112}\text{Sn}; E/A=50 \text{ MeV}$



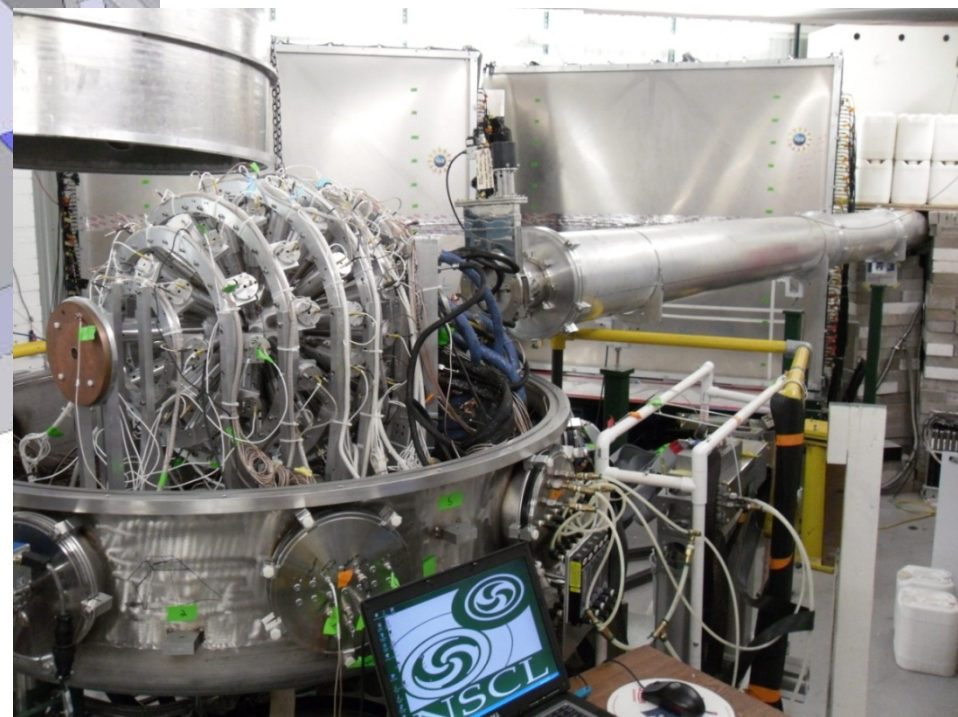
Complicated Experimental Layout



LASSA – charged particles
Miniball – impact parameter

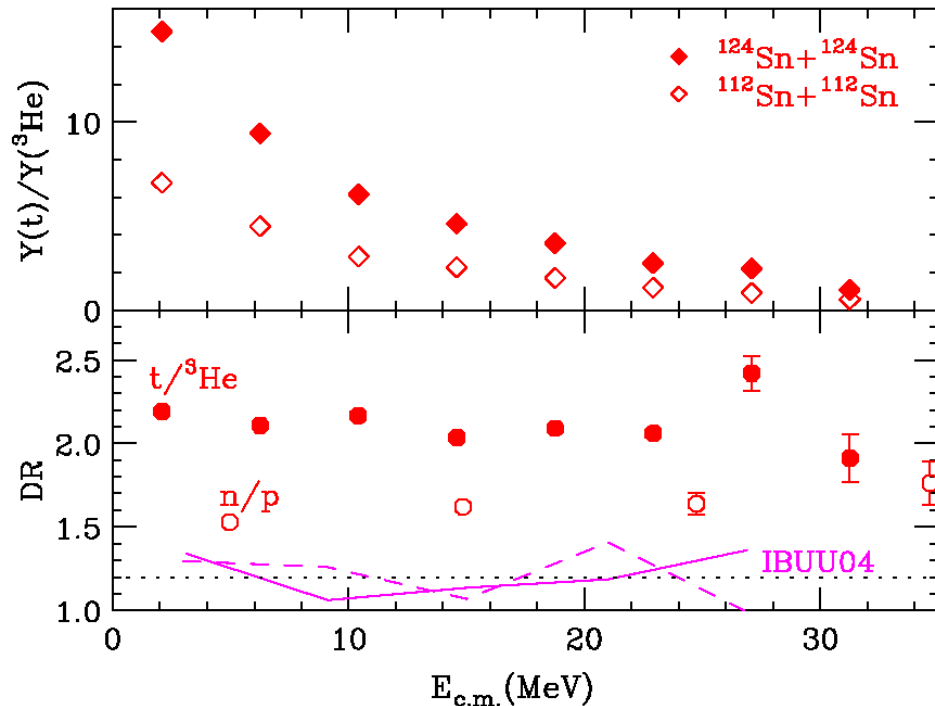
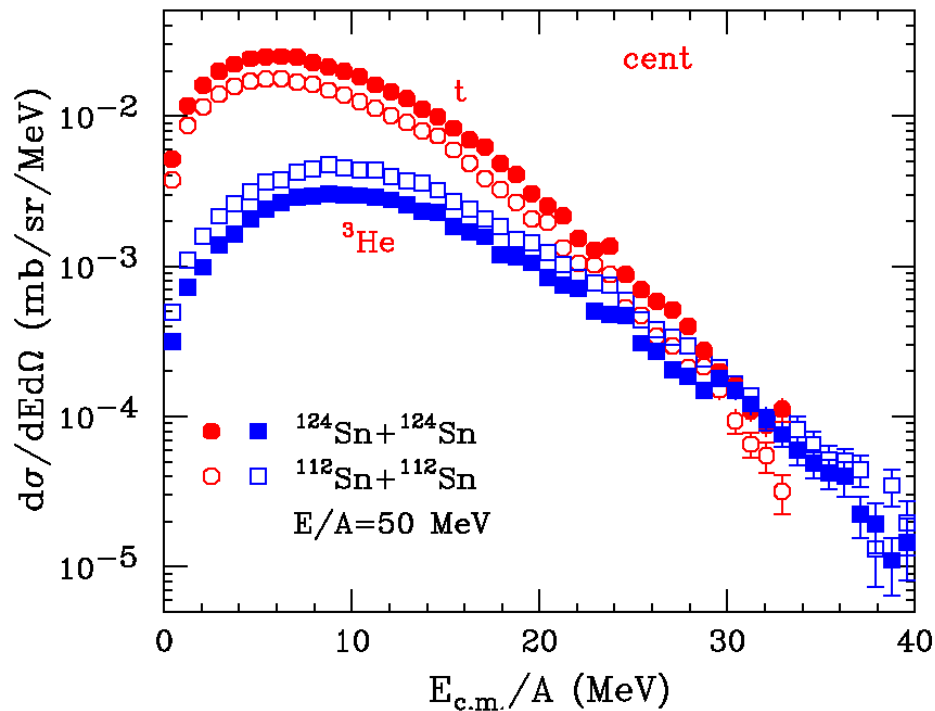
Courtesy Mike Famiano

Neutron walls – neutrons
Forward Array – time start
Proton Veto scintillators



Dan Coupland, PhD thesis (2013)

$t/{}^3\text{He}$ Double Ratios (central collisions)



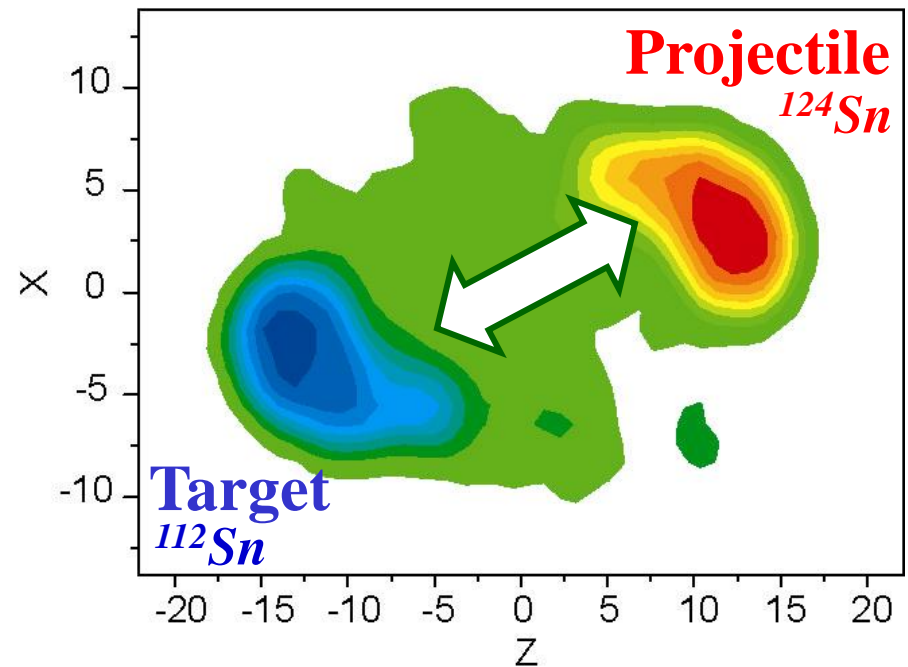
Detection of $t/{}^3\text{He}$ are better controlled but still have cut off problems at high energy due to statistics and detector limitations.

More suitable for experiments at higher beam energy

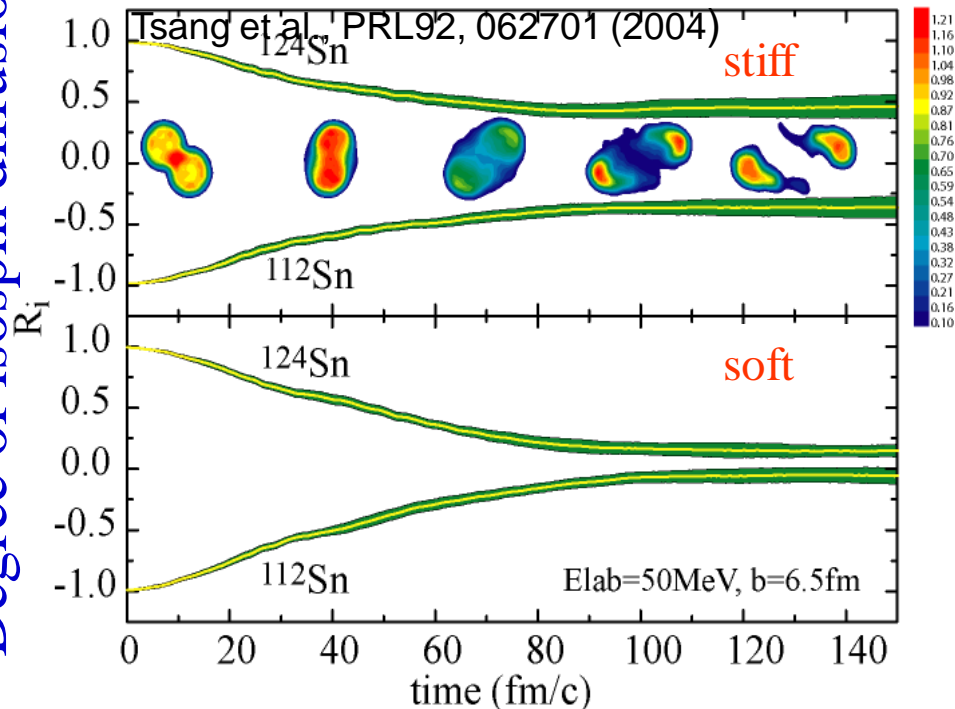
Experimental Observable : Isospin Diffusion

- *Isospin “diffuse” through low-density neck region*
- *Symmetry energy drives system towards equilibrium.*
 - *stiff EOS → small diffusion; $|R_i| \gg 0$*
 - *soft EOS → fast equilibrium; $R_i \rightarrow 0$*
- **Advantages**
 - *Sequential decays and non diffusion effects normalized by the symmetric systems*

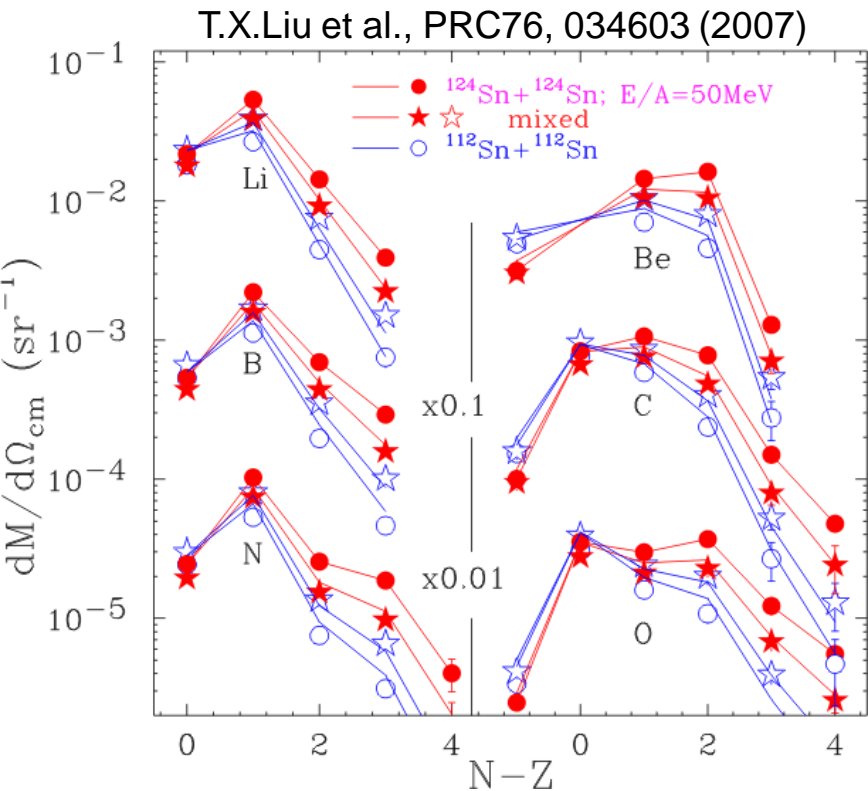
$$R_i = 2 \frac{x_{AB} - (x_{AA} + x_{BB}) / 2}{x_{AA} - x_{BB}}$$



Degree of isospin diffusion



Isotope distributions and isospin diffusions



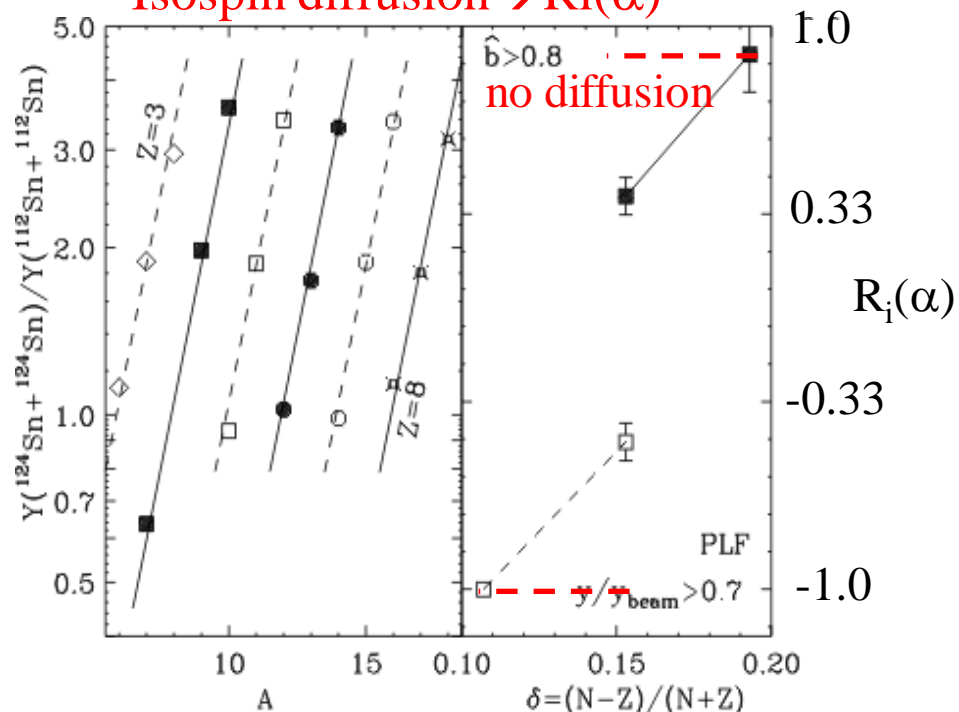
The main effect of changing the asymmetry of the projectile spectator remnant is to shift the isotopic distributions of the products of its decay

This can be described by the isoscaling parameters α and β :

$$\frac{Y_2(N, Z)}{Y_1(N, Z)} = C \exp(\alpha N + \beta Z)$$

α and β are related to the nucleon chemical potentials

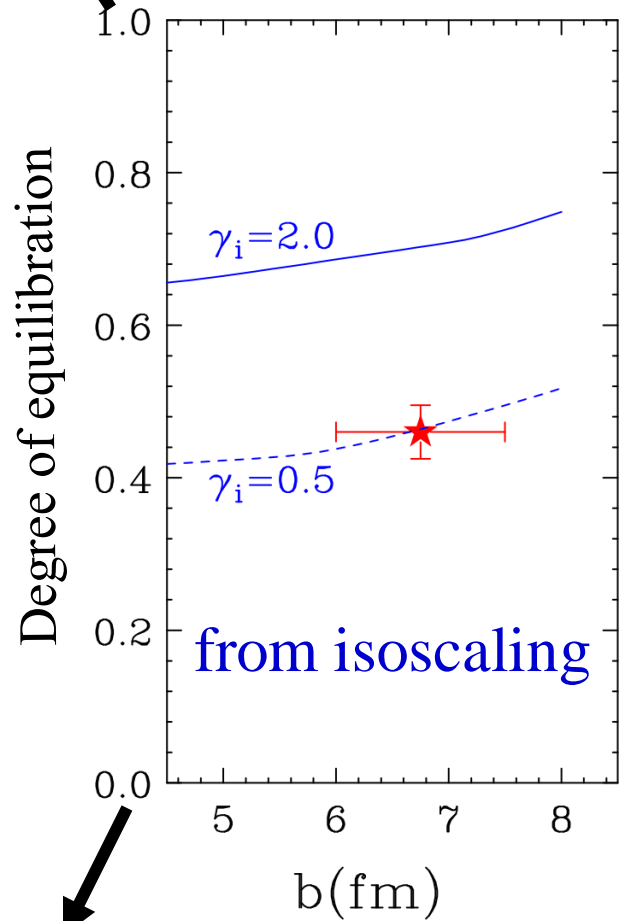
Isospin diffusion $\rightarrow R_i(\alpha)$



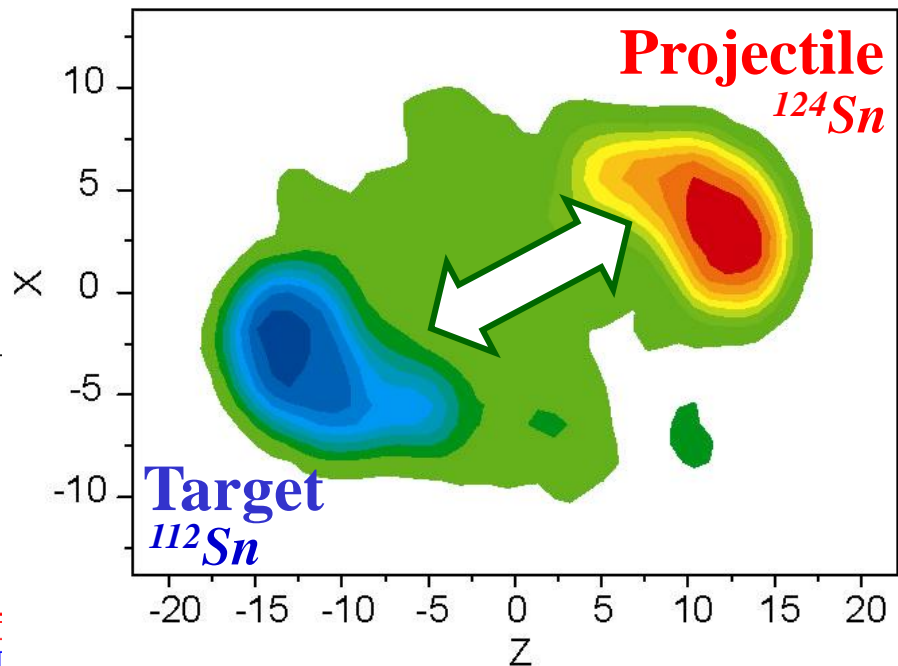
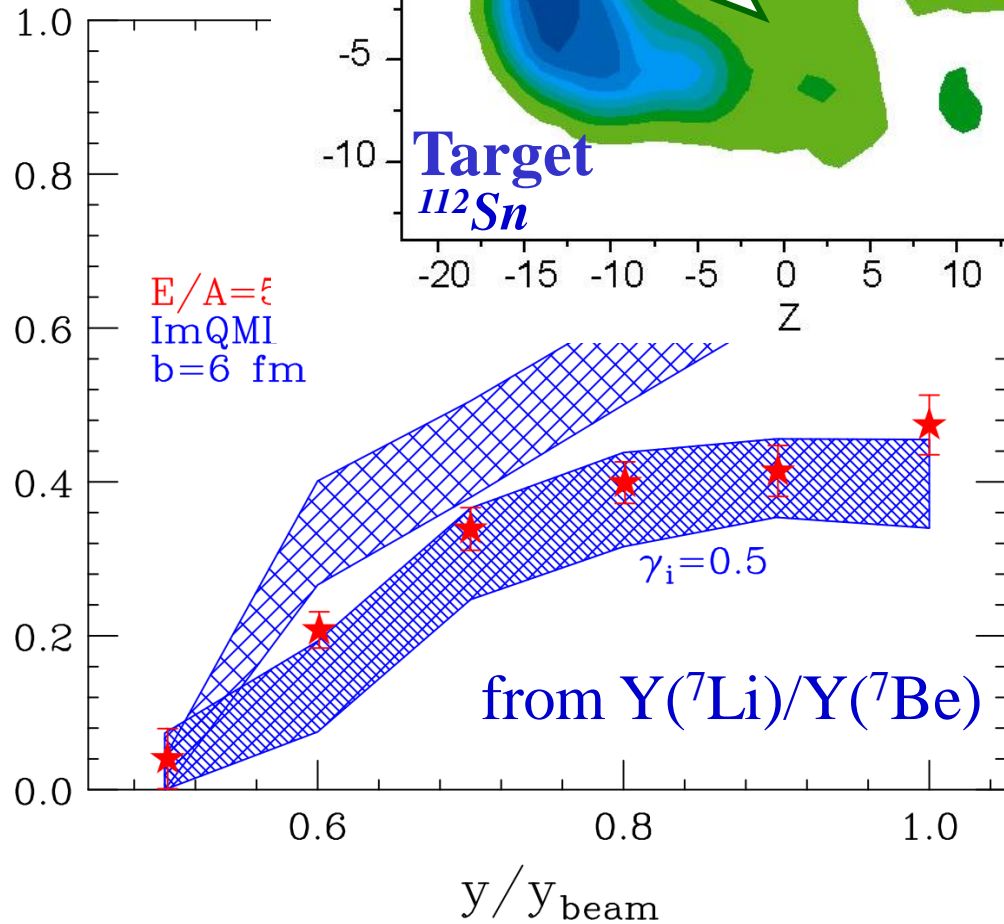
Tsang et al., PRL92, 062701 (2004)

Isospin Diffusion

No diffusion



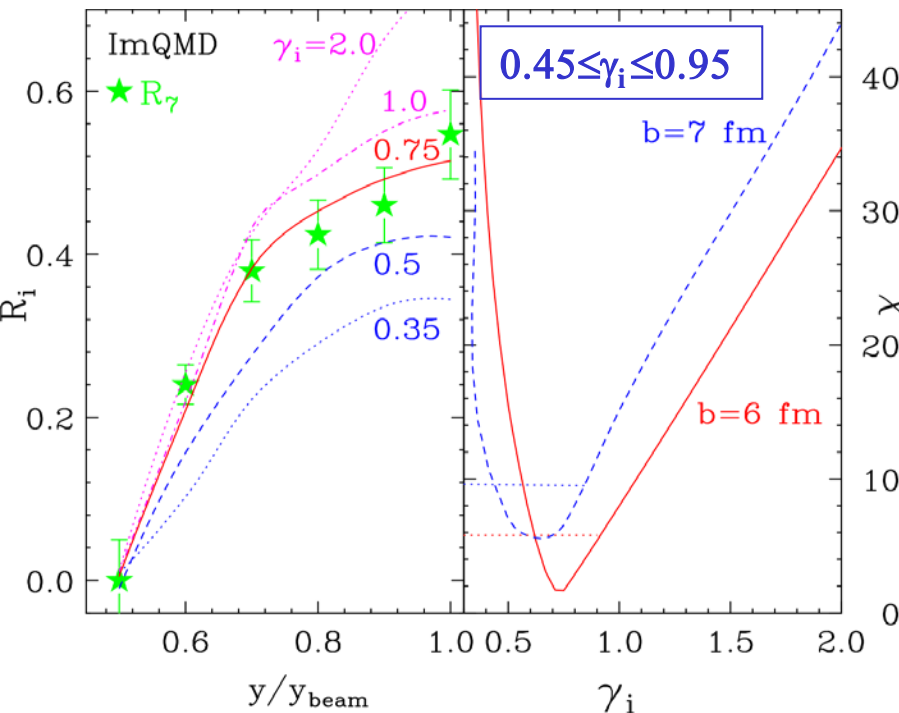
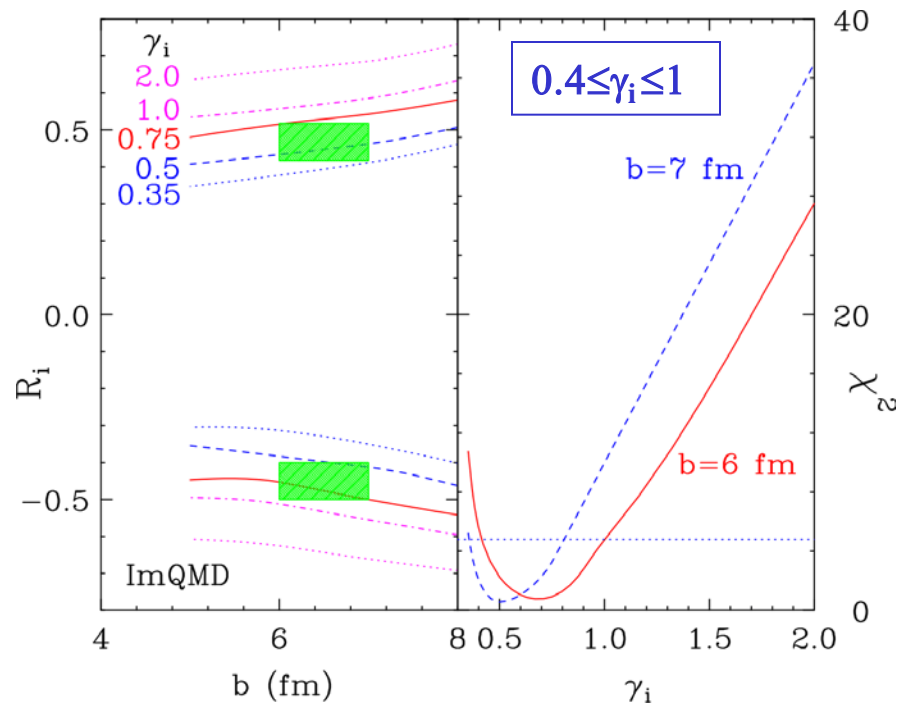
Complete mixing



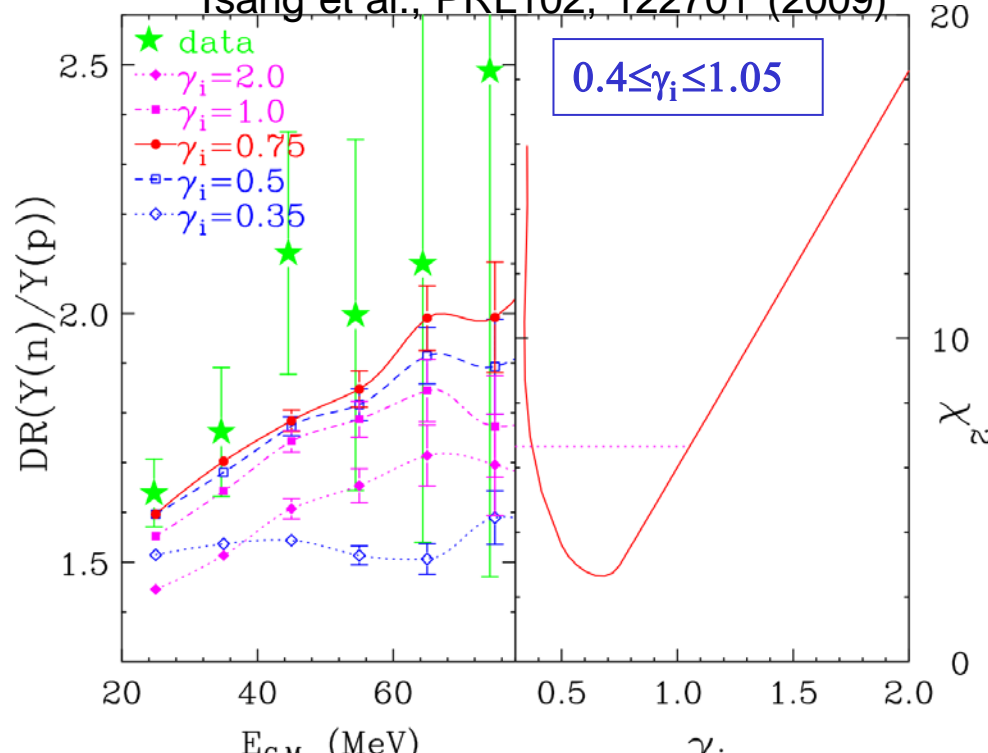
ImQMD model describes np ratios and two isospin diffusion measurements:

$$S(\rho) = 12.5(\rho/\rho_0)^{2/3} + 17.6(\rho/\rho_0)^{\gamma_i}$$

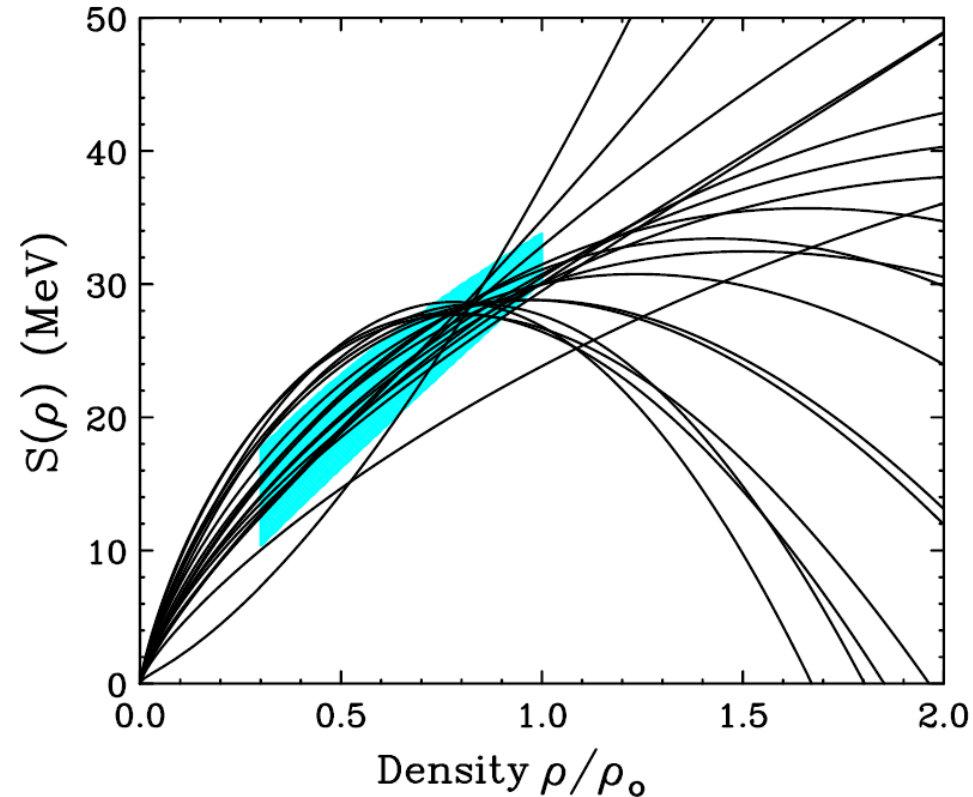
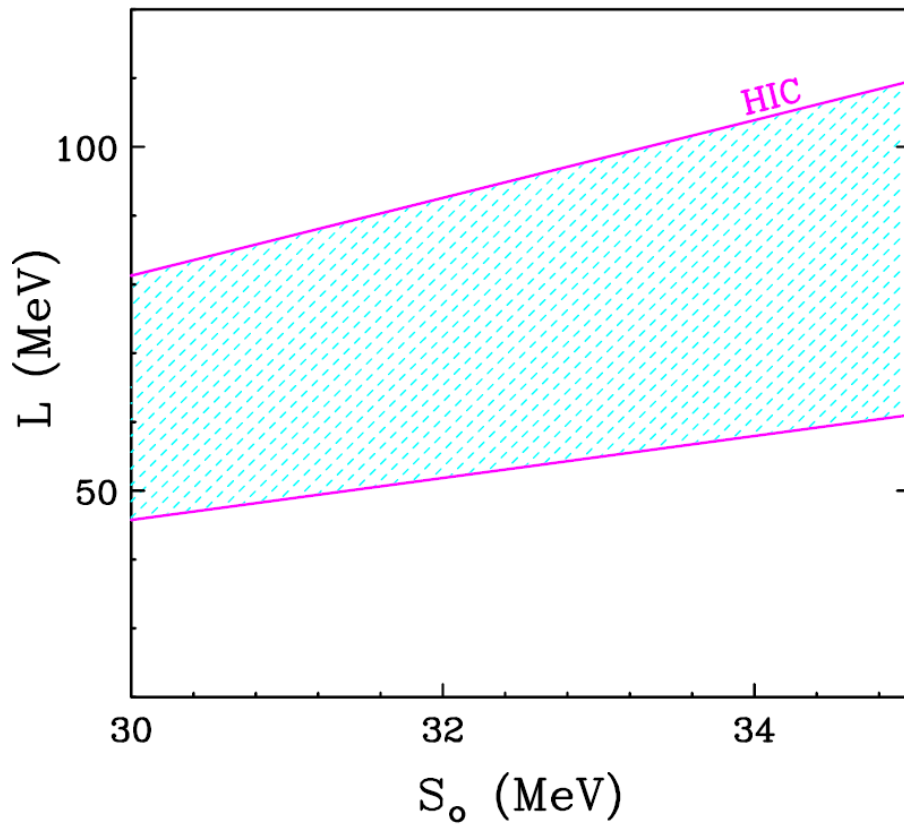
Consistent constraints from the χ^2 analysis of three observables $0.4 \leq \gamma_i \leq 1$



Tsang et al., PRL102, 122701 (2009)



HIC constraints at sub-saturation densities



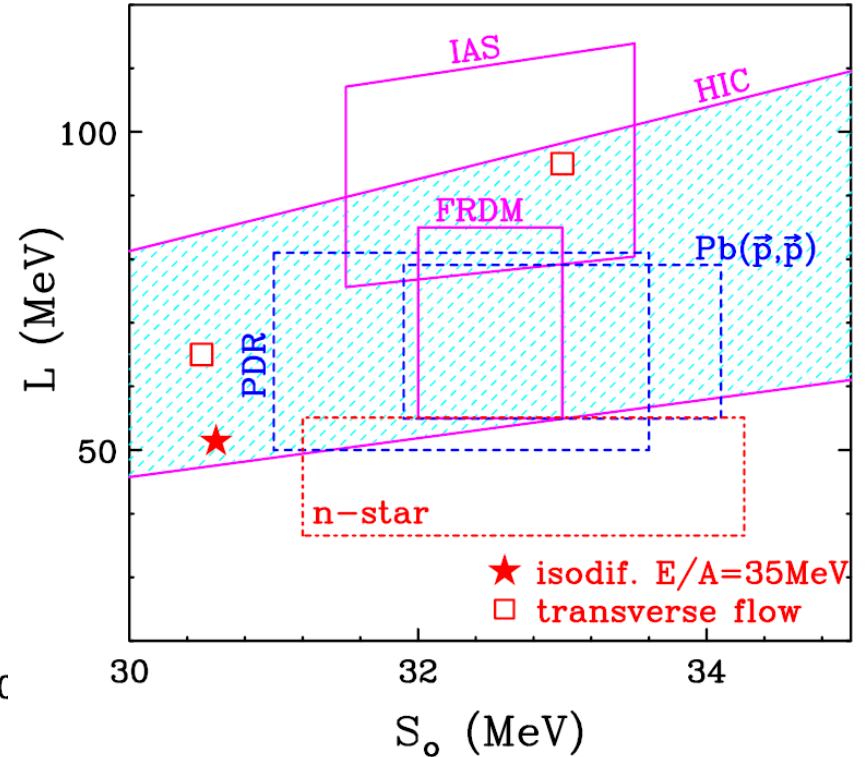
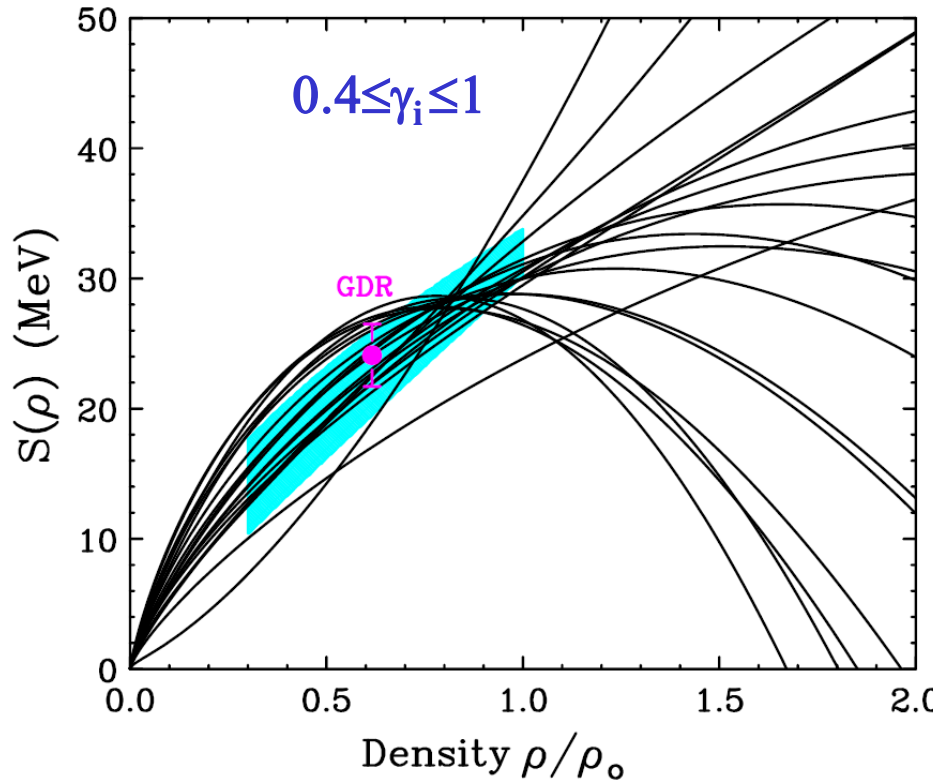
$$E_{sym} = S_o + \frac{L}{3} \left(\frac{\rho_B - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

$$S(\rho) = 12.5(\rho/\rho_o)^{2/3} + 17.6(\rho/\rho_o)^{\gamma_i}$$

$$0.4 \leq \gamma_i \leq 1$$

Symmetry energy constraints from HIC

arXiv:1204.0466

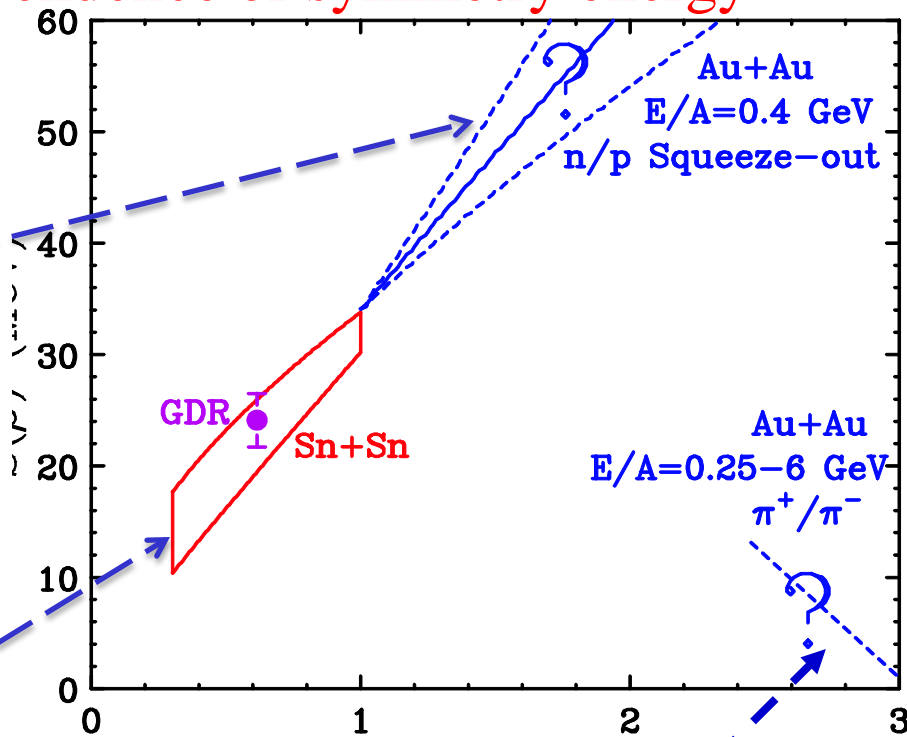
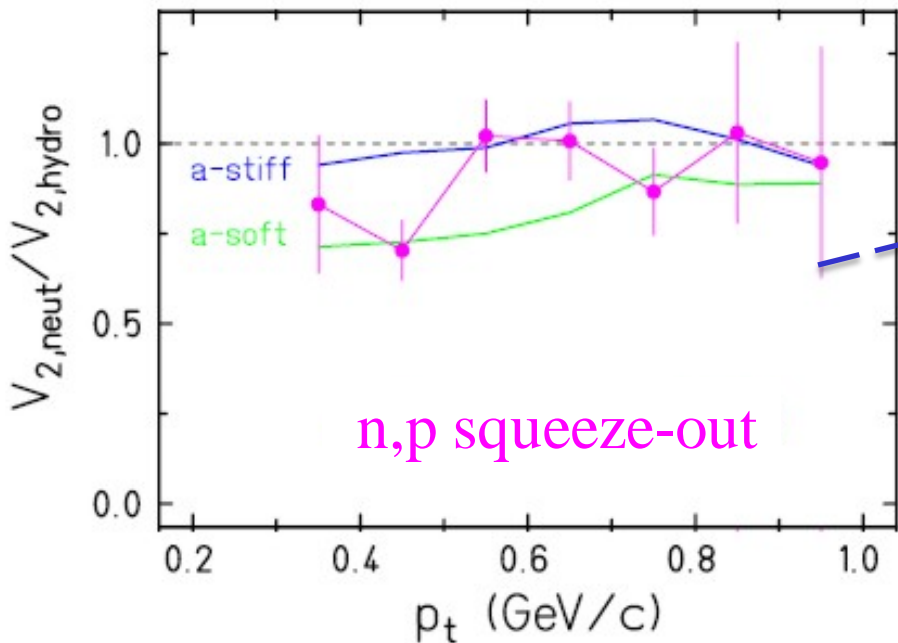


$$E_{sym} = S_o + \frac{L}{3} \left(\frac{\rho_B - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho_B - \rho_0}{\rho_0} \right)^2 + \dots$$

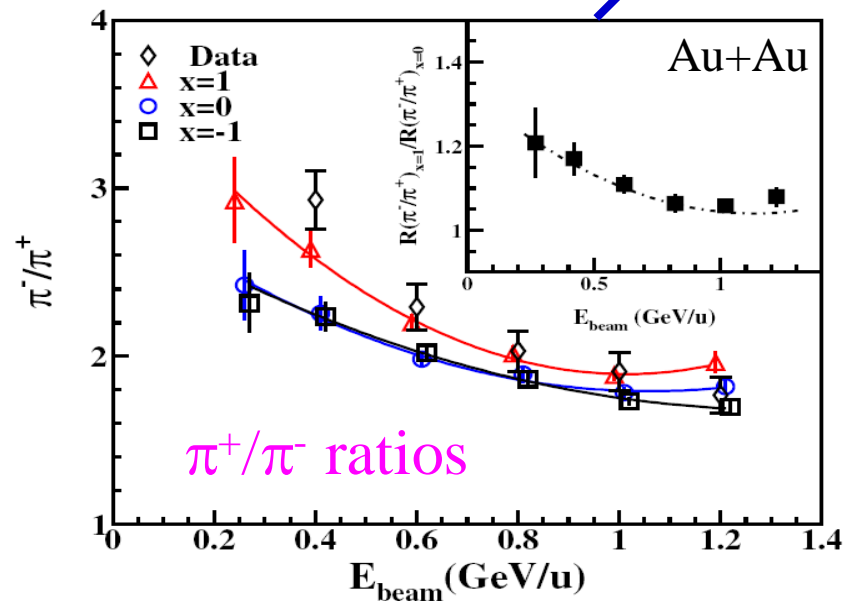
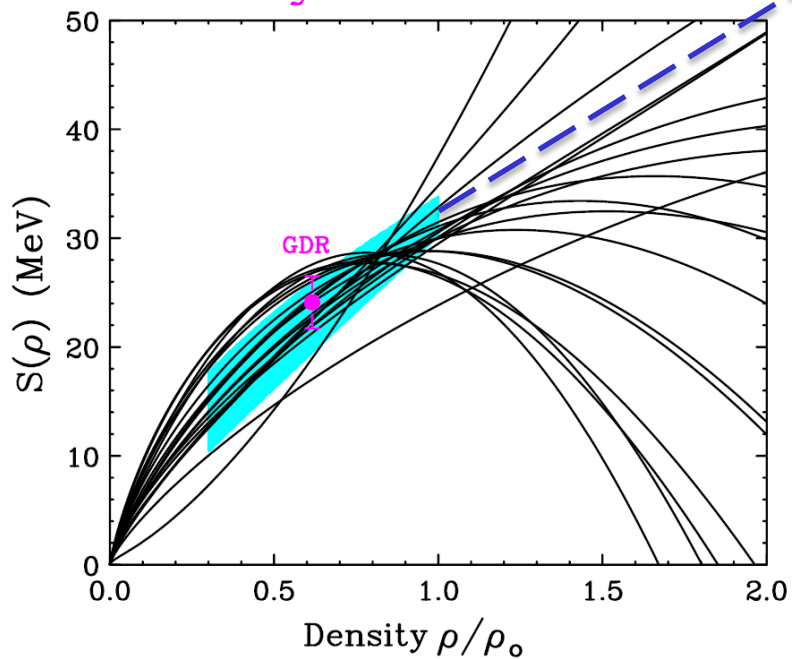
$$L = 3\rho_0 \left. \frac{\partial E_{sym}}{\partial \rho_B} \right|_{\rho_B=\rho_0} = \frac{3}{\rho_0} P_{sym}$$

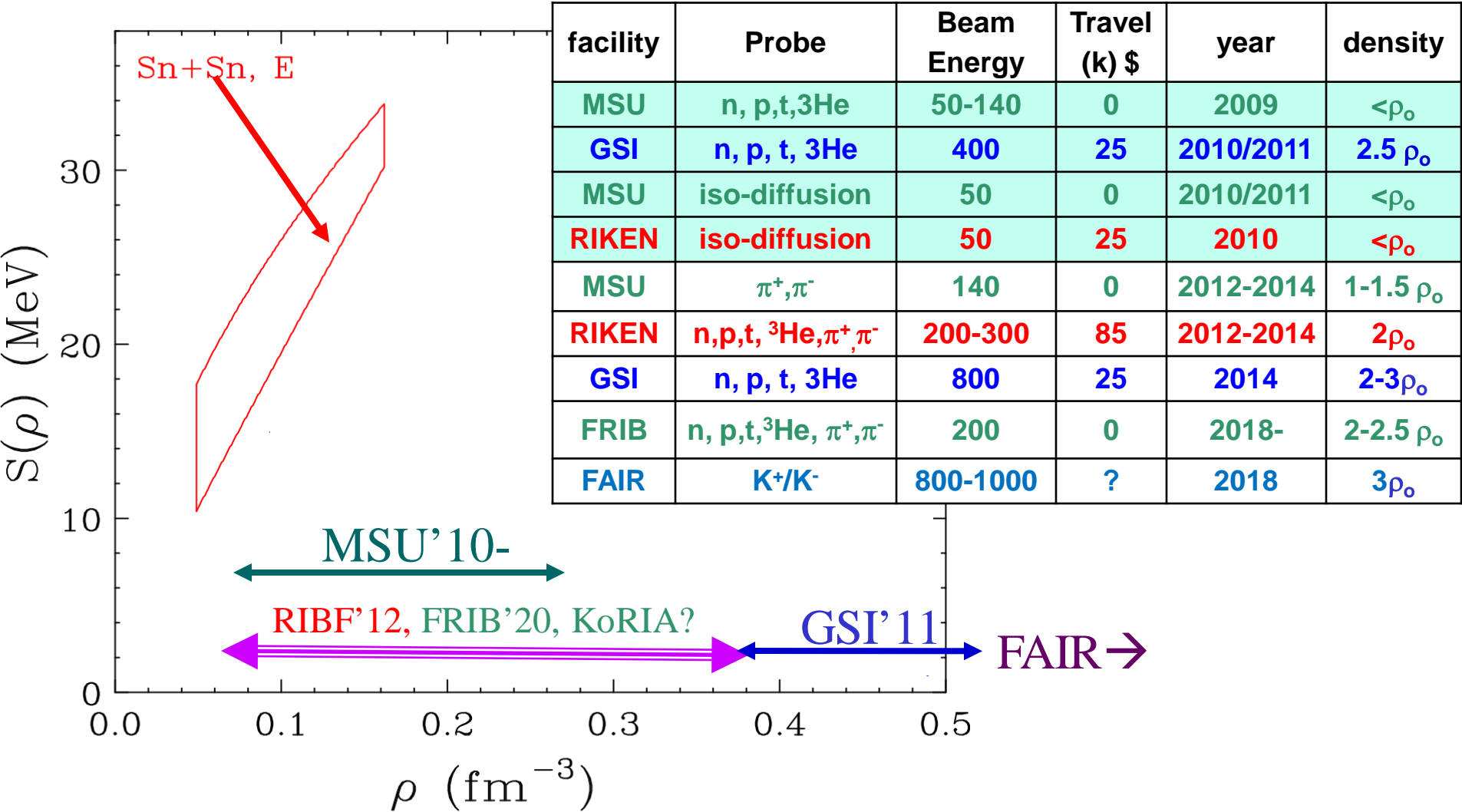
HIC has been successful in obtaining constraints on the symmetry energy at $0.3 < \rho/\rho_0 < 1$

Constraints on the density dependence of symmetry energy



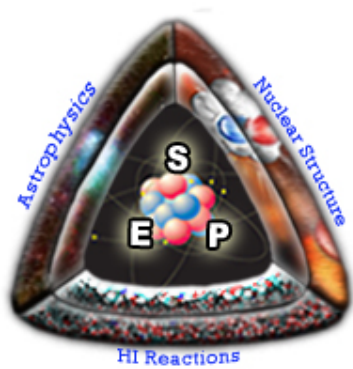
Heavy Ion Collisions





Symmetry Energy Project → International collaboration to determine the symmetry energy over a range of density

Require: New Detectors (TPC), & theory support



Nuclear Symmetry Energy (NuSym) collaboration

<http://groups.nslc.msu.edu/hira/sep.htm>

Determination of the Equation of State of Asymmetric Nuclear Matter

MSU: B. Tsang & W. Lynch, G. Westfall, P. Danielewicz, E. Brown, A. Steiner

Texas A&M University : Sherry Yennello, Alan McIntosh

Western Michigan University : Michael Famiano

RIKEN, JP: TadaAki Isobe, Atsushi Taketani, Hiroshi Sakurai

Kyoto University: Tetsuya Murakami

Tohoku University: Akira Ono

GSI, Germany: Wolfgang Trautmann , Yvonne Leifels

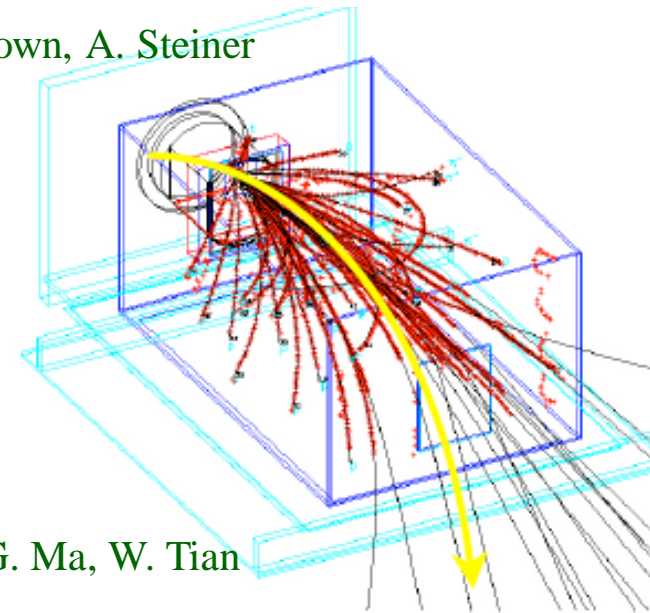
Daresbury Laboratory, UK: Roy Lemmon

INFN LNS, Italy: Giuseppe Verde, Paulo Russotto

GANIL, France: Abdou Chbihi

CIAE, PU, CAS, China: Yingxun Zhang, Zhuxia Li, Fei Lu, Y.G. Ma, W. Tian

Korea University, Korea: Byungsik Hong



The Time projection chamber is being built in the US to measure π^+/π^- & light charge particles in RIKEN

Isospin Observables in HIC at supra-normal densities

$E/A=50-100$ MeV

Neutron/proton and $t/{}^3\text{He}$ and light isotopes energy spectra & flow

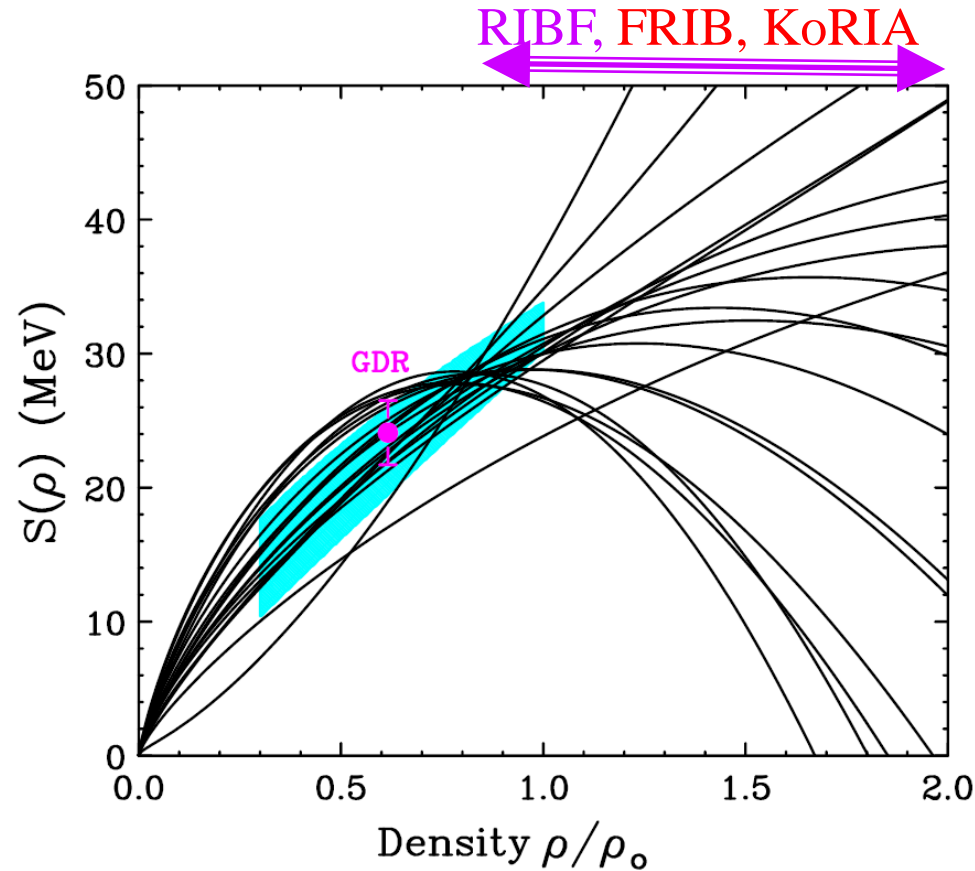
$E/A > 150$ MeV

- π^+/π^- spectra
- π^+/π^- flow

$$\frac{\pi^-}{\pi^+} \propto e^{(\mu_n - \mu_p)/T}$$

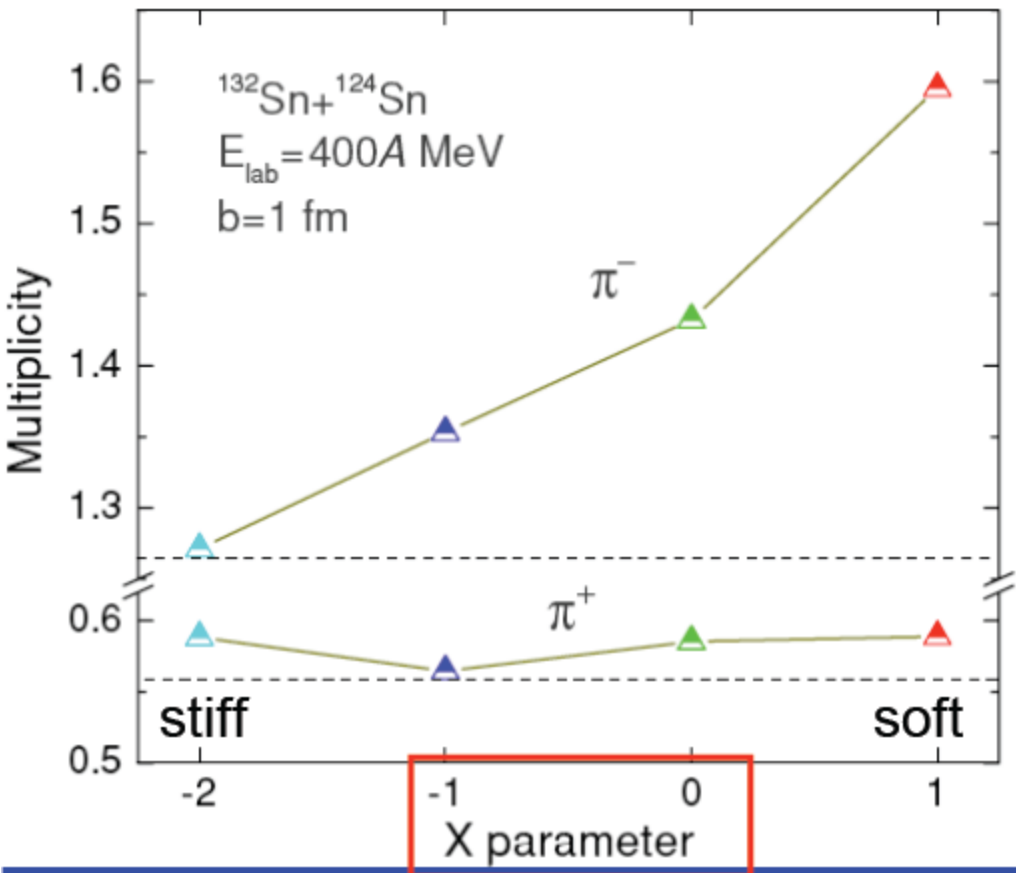
Preliminary data shows:

n/p remains robust at $E/A=120$ MeV. May be able to extend measurements to $E/A \sim 200$ MeV



A new isospin observable

Li, et al. PRC71, 014608 (2005).



$$\frac{\pi^-}{\pi^+} \propto e^{(\mu_n - \mu_p)/T}$$

- π^- generated from n+n collisions
- π^+ generated from p+p collisions
- Collisions of neutron rich nuclei: $N(\pi^-) > N(\pi^+)$
- π^- multiplicity dependent on density dependence of EOS

Slide credit : A. Bickley

Different transport codes make different predictions!

New Detector(s)

At beam energy > 100 A.MeV, fragment production decreases.

Observables are:

n/p ratios, flow, t/3He ratios, flow, π^+/π^- ratios

Properties of the Time projection chamber (TPC)

Particle identification (dE/dX–track rigidity)

Charged pions, Proton, Light ions (t, 3He)

Centrality Determination (b):

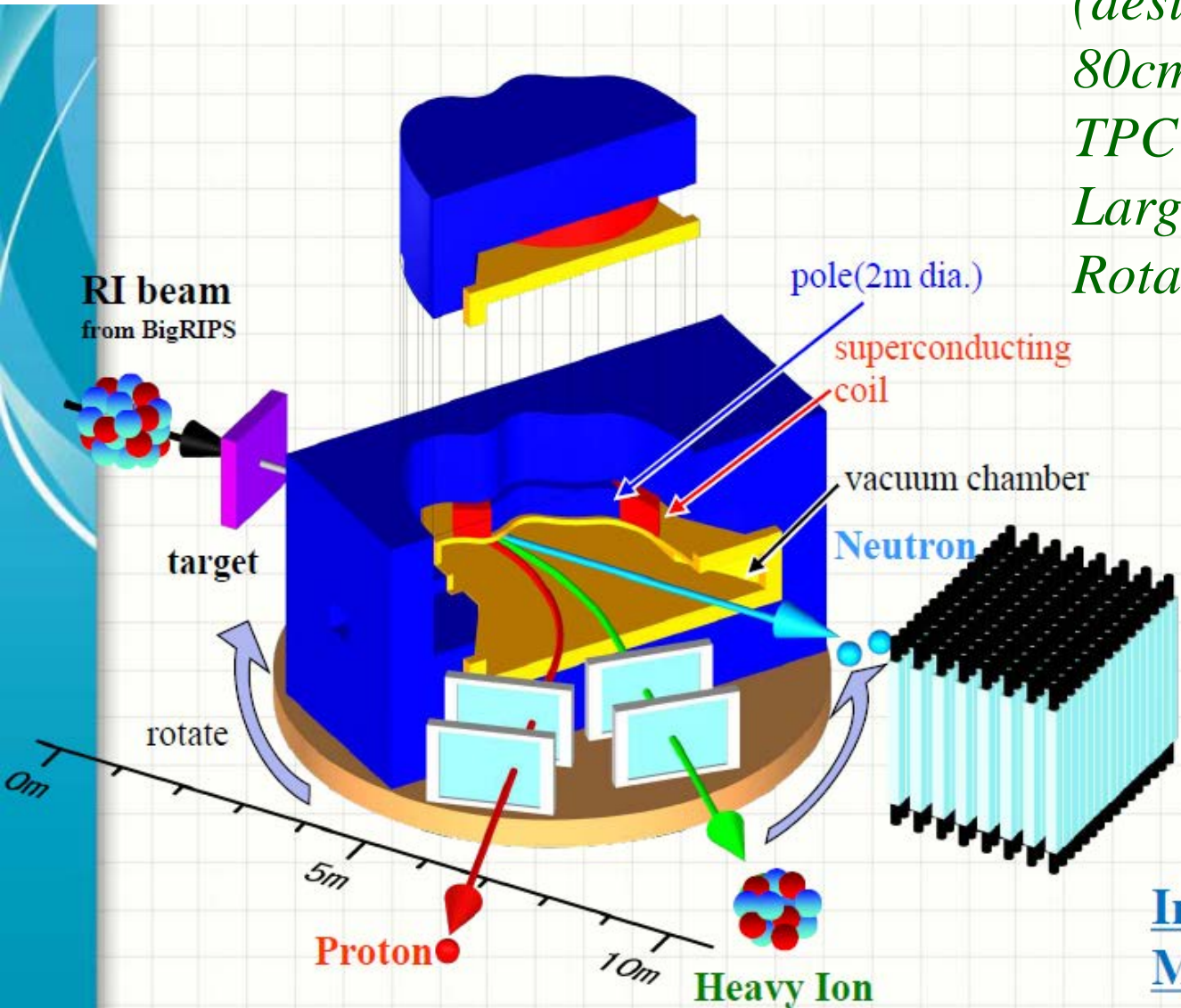
momentum measurement

Reaction plane determination

Ability to measure large number of multiple particles

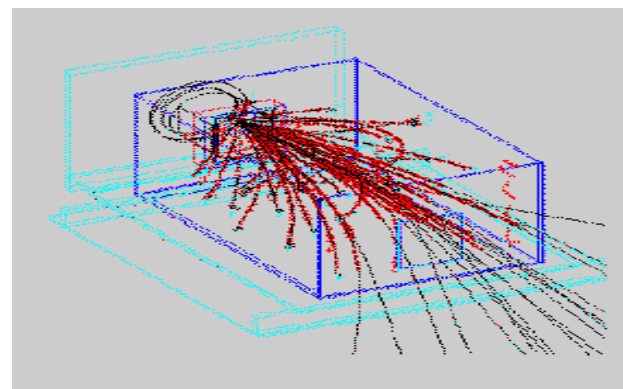
SAMURAI @ RIKEN

*Superconducting Magnet
3T with 2m dia. pole
(designed resolution 1/700)
80cm gap (vertical)
TPC
Large Vacuum Chamber
Rotational Stage*



SAMURAI-TPC

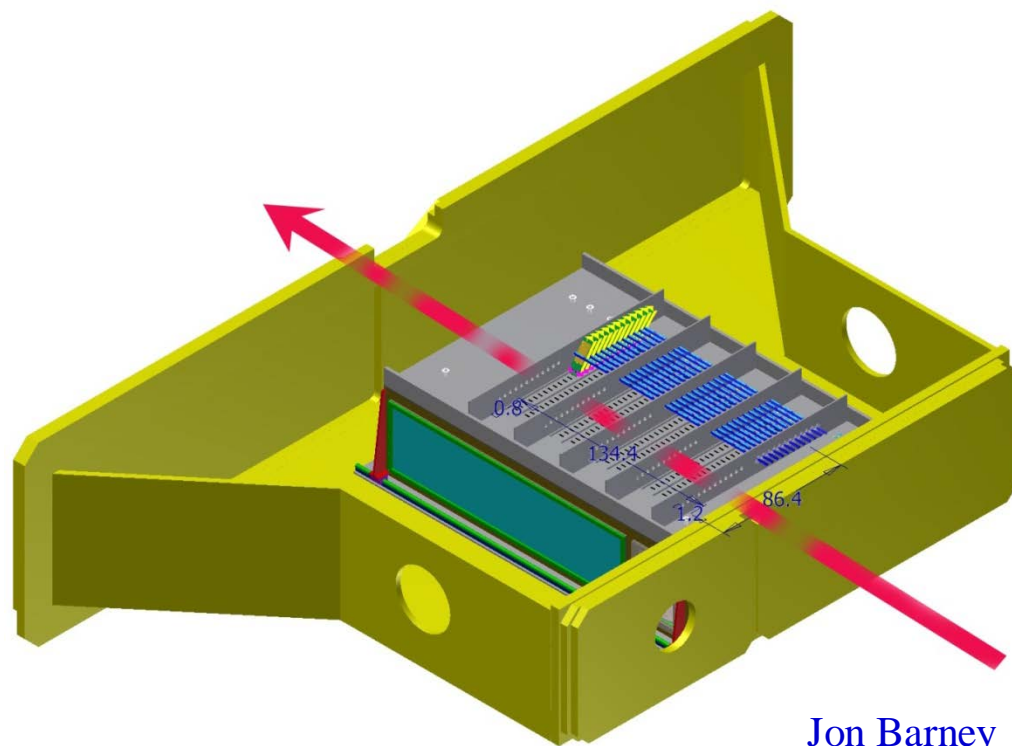
The SAMURAI Time Projection Chamber (TPC) tracks the light charged particles and pions after the heavy ion collisions.



SAMURAI Dipole Magnet



TPC in the Vacuum Chamber



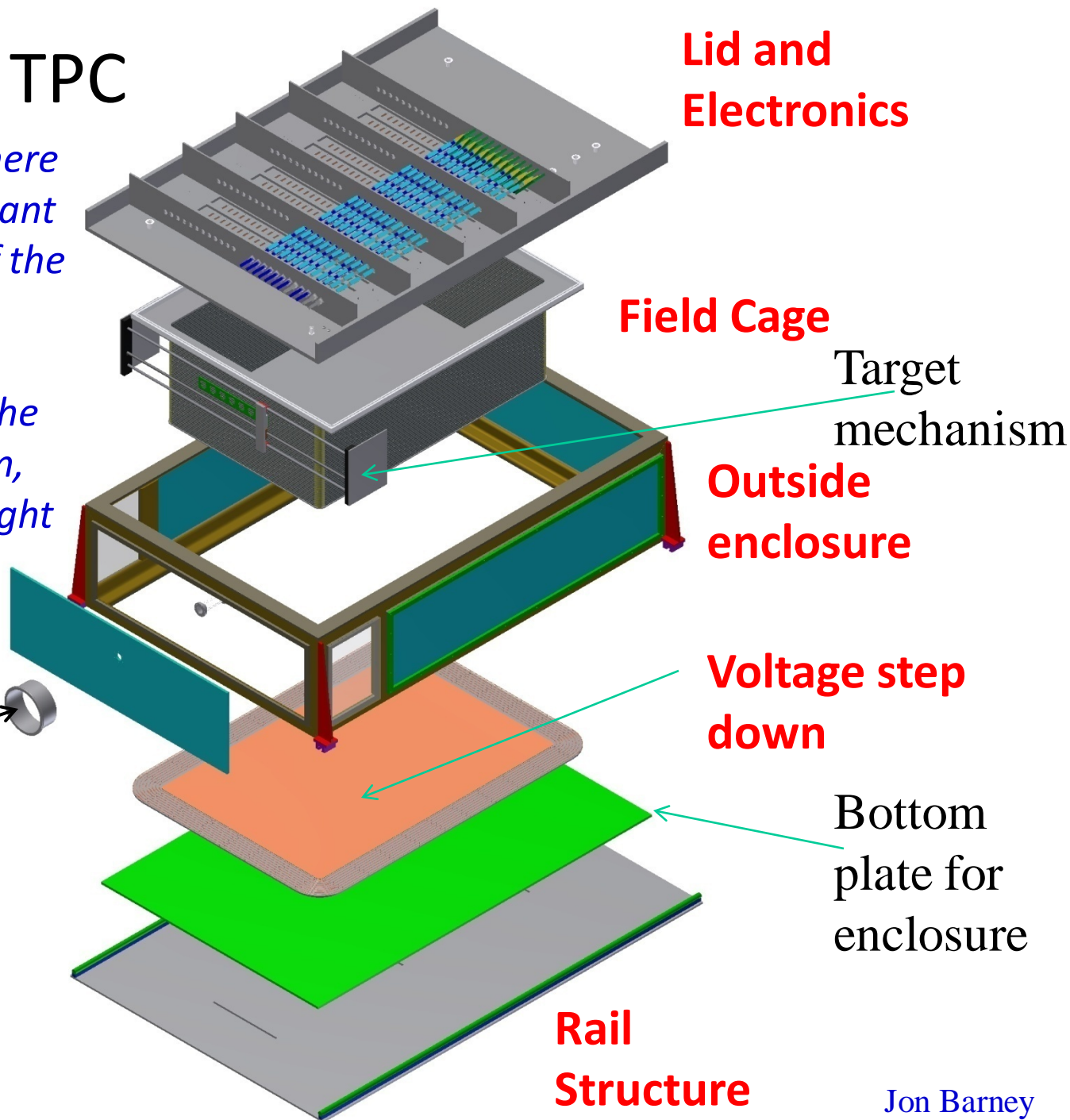
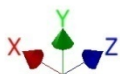
Jon Barney

The SAMURAI TPC

• Since the field cage is where the magic happens, we want to maximize the height of the field cage.

• The height is limited by the magnet chamber to 80 cm, but by minimizing the height of other parts we can maximize the field cage height

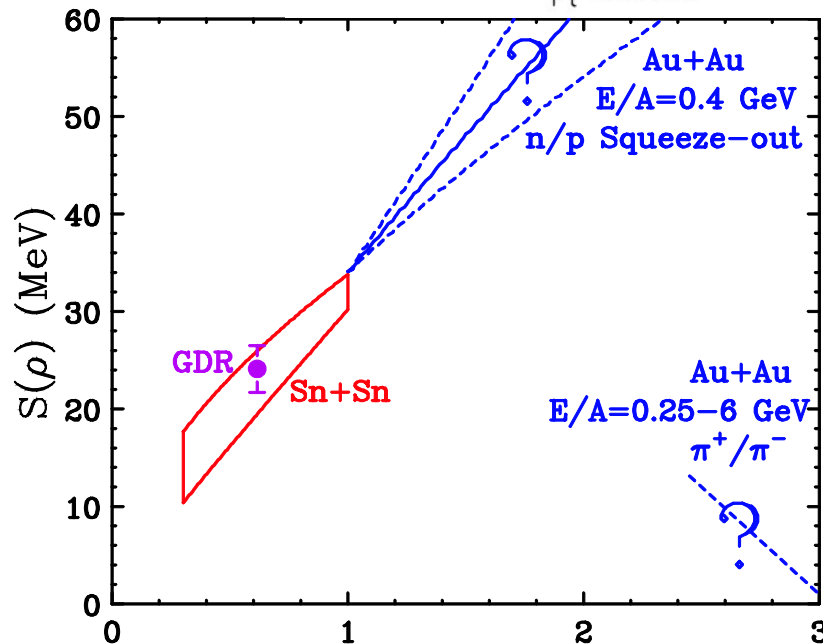
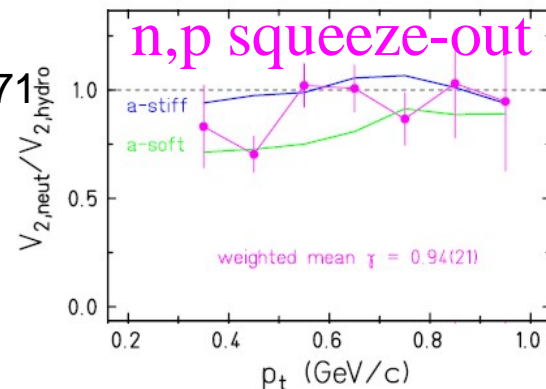
Reentrant



Summary

- Success at low energy HIC program suggests paths forward to higher energy program to determine the density dependence of symmetry energy at high density – important program in any nuclear science LR plans.
 - HIC is the only way on earth to create nuclear matter with $\rho > \rho_0$.
 - Challenges remains:
 - New detectors to measure new observables. TPC to detect p's.
 - Extension of current observables to high energy (n,/p, t/3He...)
 - HIC experiments are complicated, need advance planning and “floor place/footprint” in new facilities.
- Much work remains – exciting time to join the international effort!

Russotto et al.,
PL B697 (2011) 471



Xiao et al., PRL102, 062502 (2009)

