

# Nuclear effect on charm production in $pA$ in the CGC framework

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H. Fujii (U of Tokyo, Komaba)

w/ F.Gelis, R. Venugopalan

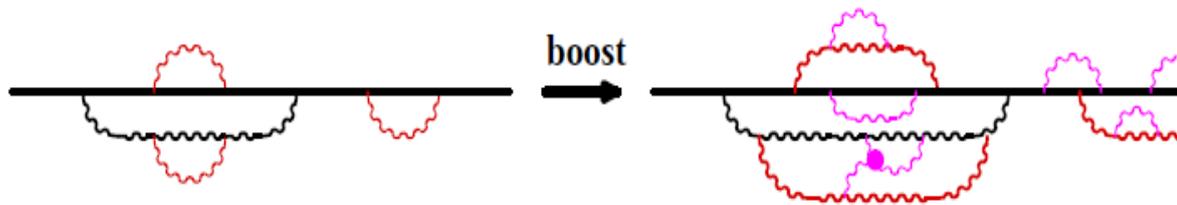
## Outline

- Introduction
  - CGC framework: MV model+BK evolution
  - Open Charm
  - Charmonium
  - Summary and discussion
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# Introduction: CGC in A

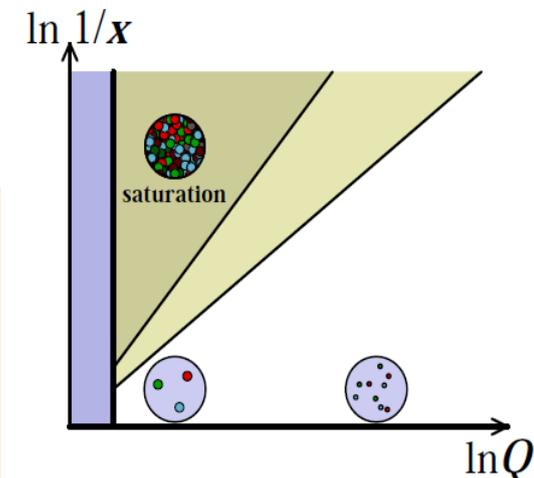
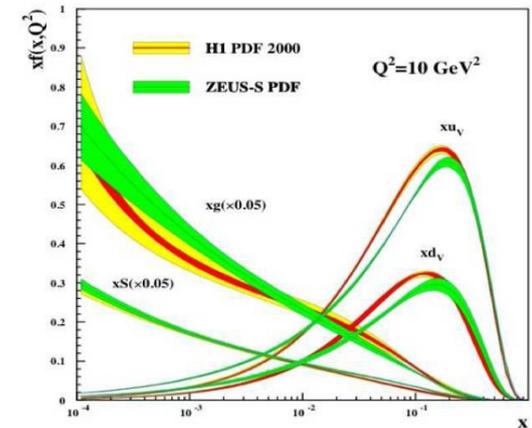
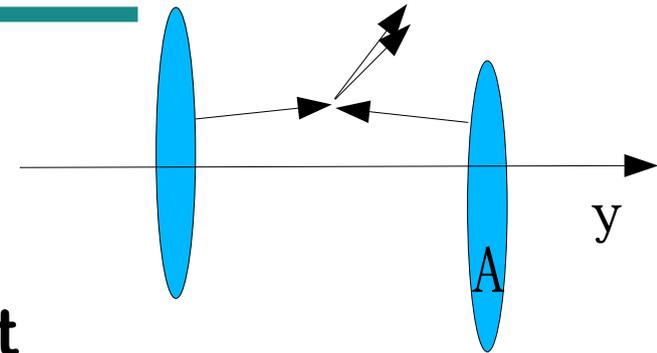
- Initial condition for AA collisions

- Small-x partons:  $\sqrt{s}x_A = k_1 e^{-y_1} + k_2 e^{-y_2}$
- Color Glass Condensate** in high E limit
  - Boost = seeing short time fluctuations
  - ⇒ dense partonic system



⇒ parton saturation

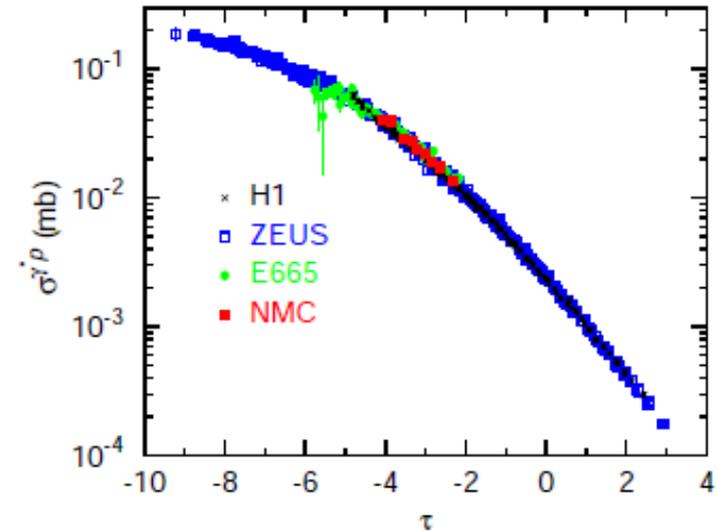
- In nuclei, larger *partons/trans area* by  $A^{1/3}$ 
  - Earlier saturation than proton
  - Multiple scatterings in A



# Introduction: CGC in A

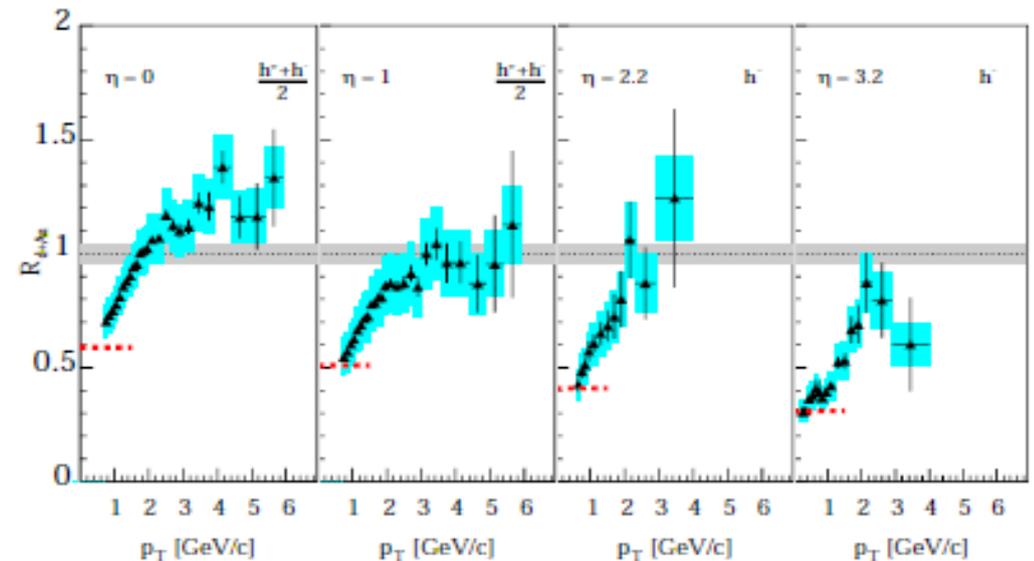
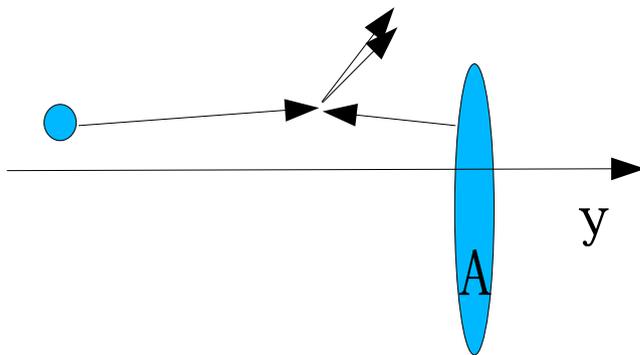
- Evidence of CGC

- HERA (DIS) :  $\tau \sim Q^2/Q_s^2(x)$



- BRAHMS :  $R_{dA}(y)$

- Large  $x_p$  and small  $x_A$



# Introduction: Charm

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- **Heavy flavors:**  $m_Q \gg \Lambda_{\text{QCD}}$ 
  - initial hard productions only  $\Rightarrow$  pQCD predictions
  - Calibrated impurity probing medium property
  - **Caveats:** nuclear pdf, intrinsic kT, multiple scattering
  
- **Quarkonia:**
  - Rare formation
  - **Caveats:** longer formation time  $O(1/\alpha_s m^2)$ 

formation mechanism not fully understood

**estimate for cold nuclear effects**

# Introduction: Why charm in CGC?

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- Heavy flavors:  $m_Q \gg \Lambda_{\text{QCD}}$  but
  - Produced from gluon fusion
  - Multiple interactions possible at RHIC
    - $1/(2m) \sim 0.07 \text{ fm}/c$  vs  $R_A/\gamma \sim 0.13 \text{ fm}$
    - $1/(1/\alpha_s m^2) \sim 0.3 \text{ fm}/c$



# CGC framework

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# CGC framework: MV Gauss model

- “Valence” partons : random charge on  $x^+$  axis
- Small- $x$  partons: classical field

$$[D_\nu, F^{\nu\mu}]_a = \delta^{\mu+} \delta(x^-) \rho_a(\vec{x}_\perp)$$

- Compute observables  $\mathcal{O}(\rho)$
- Average over  $W$  the distribution of  $\rho$

$$\langle \mathcal{O} \rangle = \int [D\rho_a] W_{x_0}[\rho_a] \mathcal{O}[\rho_a]$$

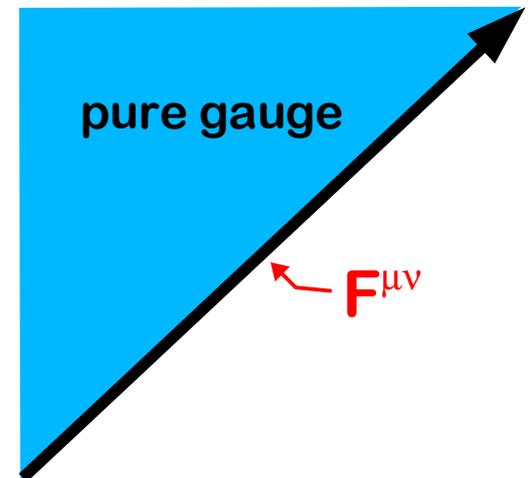
- McLerran-Venugopalan (MV) model

- **Gaussian** :  $W[\rho] = \exp\left[-\int d^2x \rho(x)_a^2 / 2\mu^2\right]$

- $\mu^2 \sim Q_s^2$ : mean charge density

- **valid for small  $x$ , but  $\alpha_s \ln(1/x) < 1$**  e.g.,  $x \sim 0.01$

McLerran, Venugopalan (1994), Iancu, Leonidov, McLerran (2001)



# CGC framework: pA collision

- pA coll = two sources

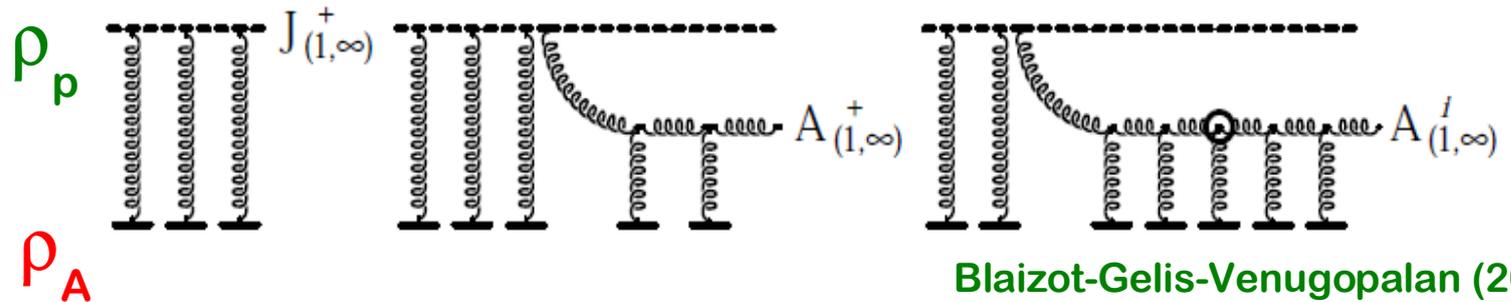
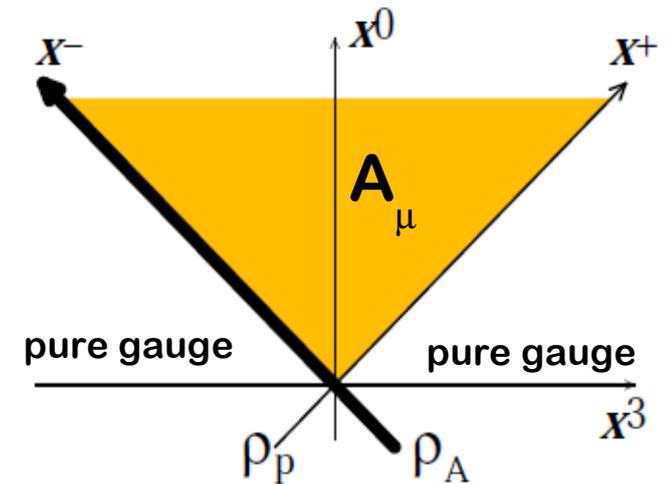
$$[D_\nu, F^{\nu\mu}]_a = J_a^{\mu(0)}$$

$$J_a^{\nu(0)} = g\delta^{\nu+}\delta(x^-)\rho_{p,a}(\mathbf{x}_\perp) + g\delta^{\nu-}\delta(x^+)\rho_{A,a}(\mathbf{x}_\perp)$$

- dilute+dense system:  $g^2\rho_A = \mathcal{O}(1)$

- Classical EoM sums tree graphs  $\mathcal{O}(\rho_A^\infty)$

- Multiple scatterings



Blaizot-Gelis-Venugopalan (2004)

# CGC framework: gluon production

- **x-section:**

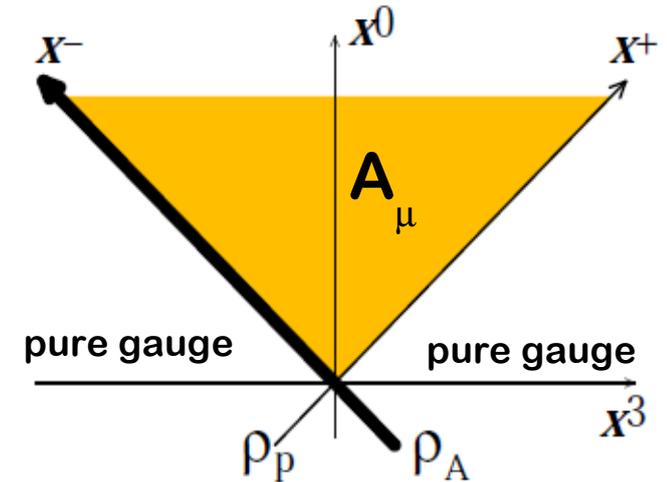
$$\frac{d\bar{N}_g}{d^2q_\perp dy} \sim \frac{\alpha_s}{q_\perp^2} \int_{k_\perp} \varphi_p(\mathbf{q}_\perp - \mathbf{k}_\perp) \phi_A^{gg}(\mathbf{k}_\perp)$$

- “Unintegrated gluon dist.fn.” (uGDF) includes multiple interactions

$$\phi_A^{g,g} \sim \mathbf{k}_\perp^2 \text{FT} \langle U(\mathbf{x}) U^\dagger(\mathbf{y}) \rangle$$

$$U(\mathbf{x}) \equiv \mathcal{P} \exp \left[ ig^2 \int dz^+ (1/\nabla^2) \rho(z^+, \mathbf{x}) \cdot T \right]$$

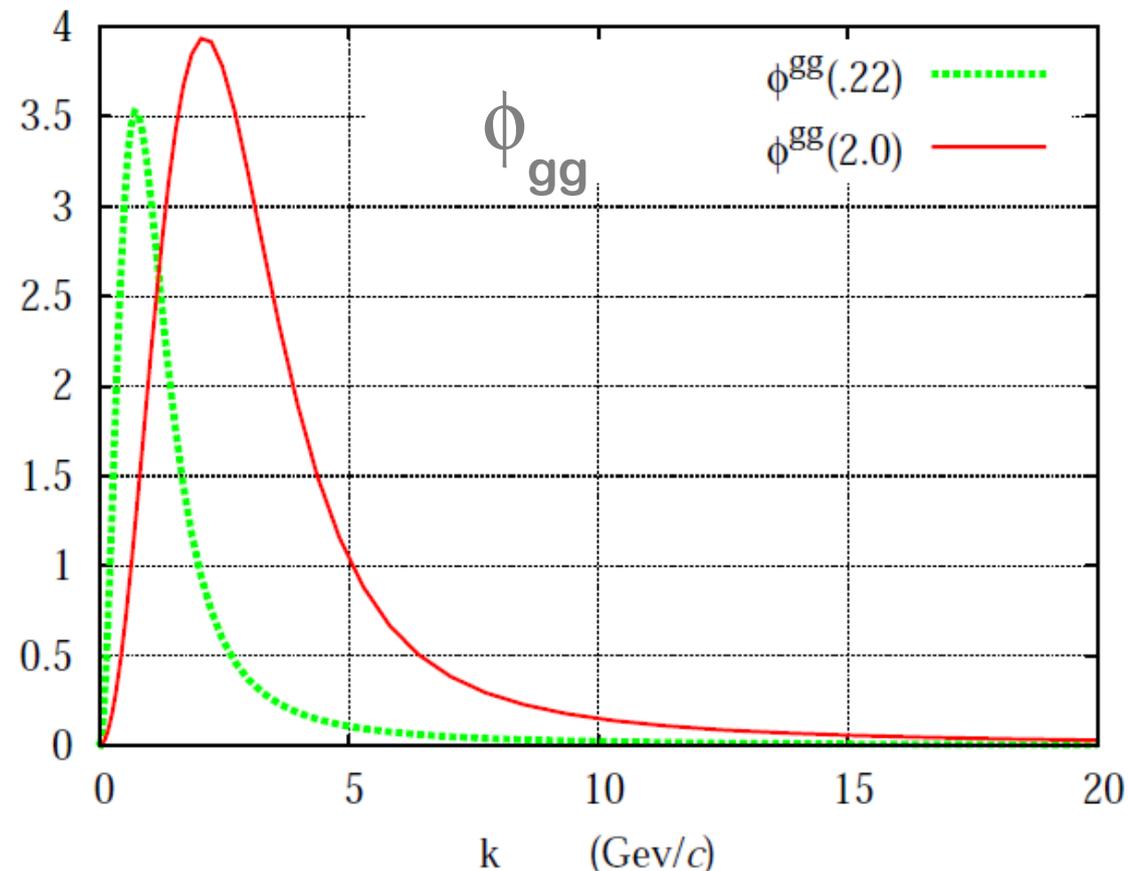
$$xg(x, Q^2) = \frac{1}{4\pi^3} \int dk_\perp^2 \phi_A^{g,g}(x, k_\perp^2)$$



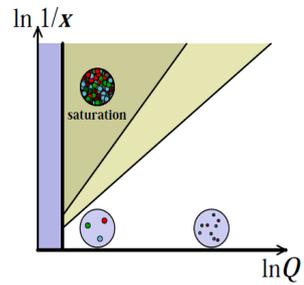
Blaizot-Gelis-Venugopalan (2004)

# CGC Framework: uGDF

- MV model assumed at  $x \sim 0.01$
- scale  $\mu^2 \sim Q_s^2 \sim A^{1/3}$  in the model characterizes targets
  - $0.22 \text{ GeV}^2$  ... “proton”
  - $2.0 \text{ GeV}^2$  ... “nucleus”  
(a.u.)
- intrinsic kT distribution
- $1/k^2$  – perturbative tail

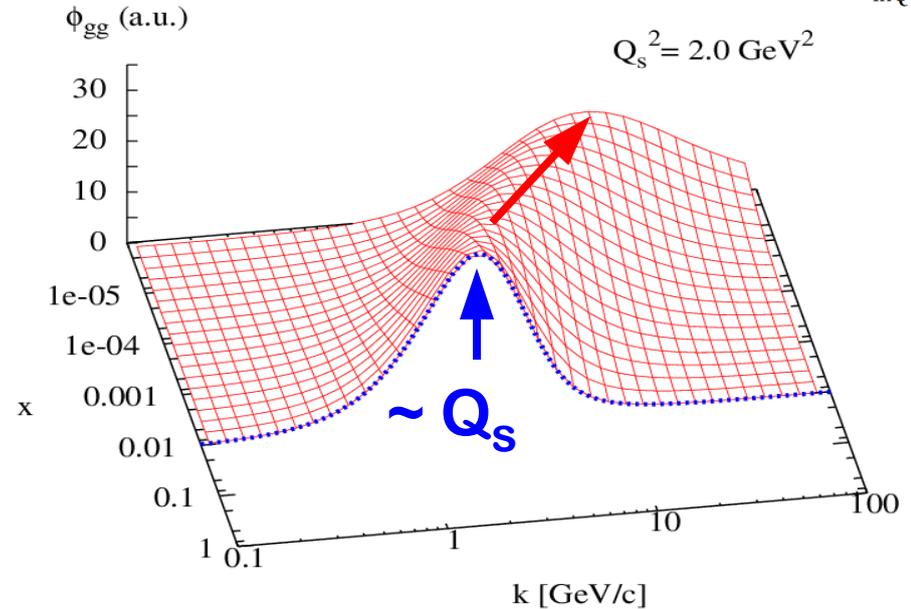


# CGC Framework: x-evolution



- **BK equation (large N & A)**

- Evolve from  $x_0=0.01$ 
  - MV model for  $x > x_0$
- Linear: BFKL sums up ( $\alpha_s y$ )
- Nonlinear: gluon fusion effect

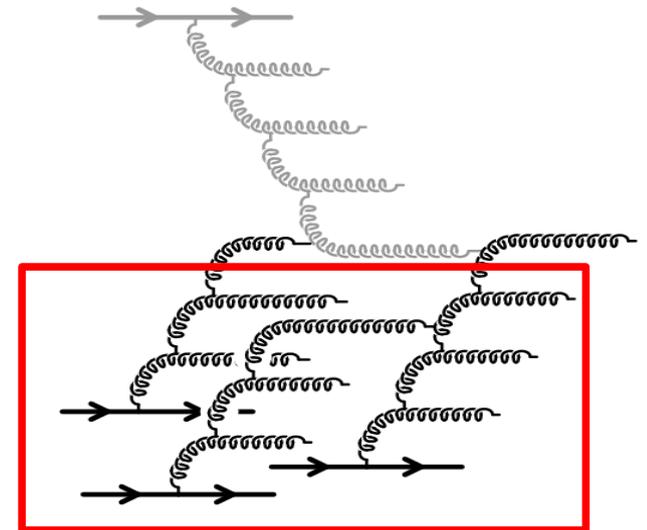


$$\frac{\partial}{\partial Y} T_Y(\mathbf{k}_\perp) = \bar{\alpha}_s [\chi(-\partial_L) T_Y(\mathbf{k}_\perp) - T_Y^2(\mathbf{k}_\perp)]$$

$$\bar{\alpha}_s = \alpha_s N / \pi, \quad L \equiv \ln(k_\perp^2 / \Lambda^2)$$

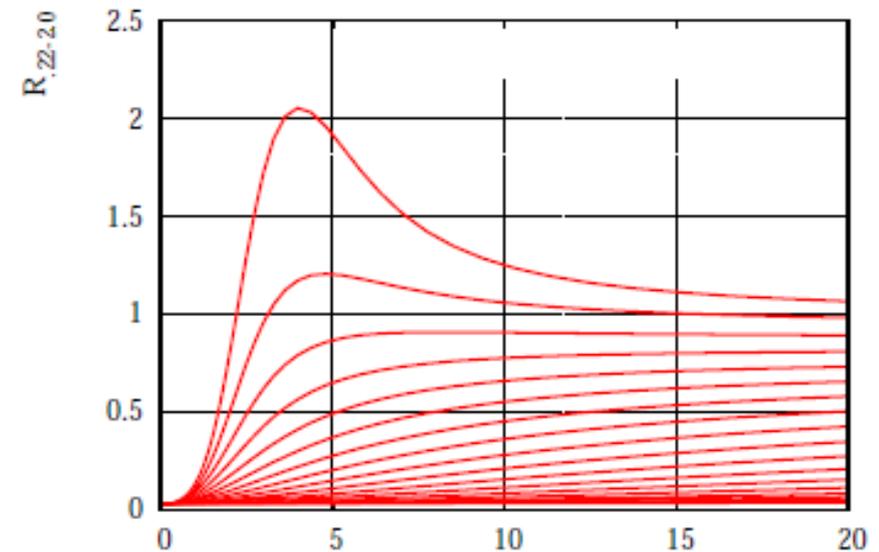
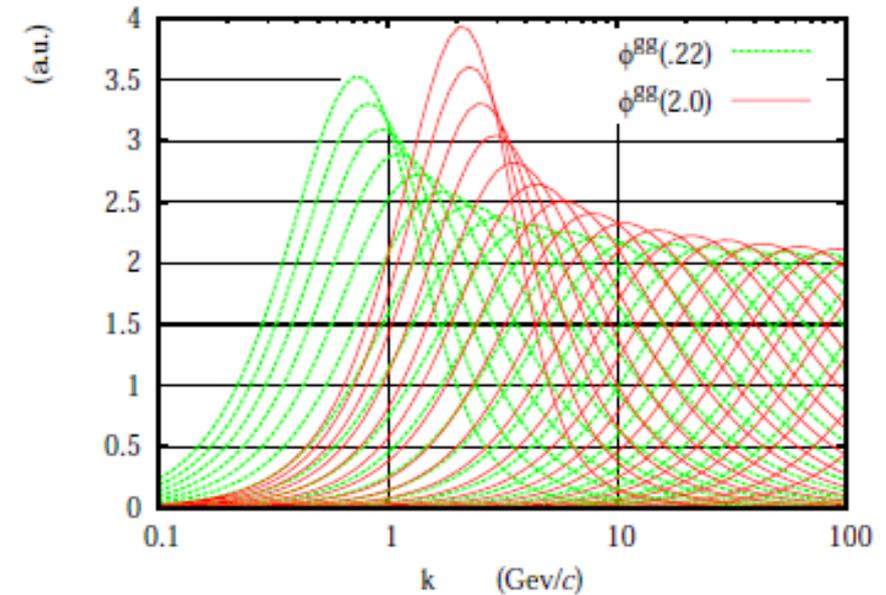
$$\chi(\gamma) = 2\psi(1) - \psi(\gamma) - \psi(1 - \gamma): \text{BFKL kernel}$$

$$T_Y(\mathbf{k}_\perp) = \int \frac{d^2 \mathbf{x}_\perp}{2\pi x_\perp^2} (1 - \langle \tilde{U} \tilde{U}^\dagger \rangle) e^{i\mathbf{k}_\perp \cdot \mathbf{x}_\perp} \phi_{gg}(k_T, x) =$$



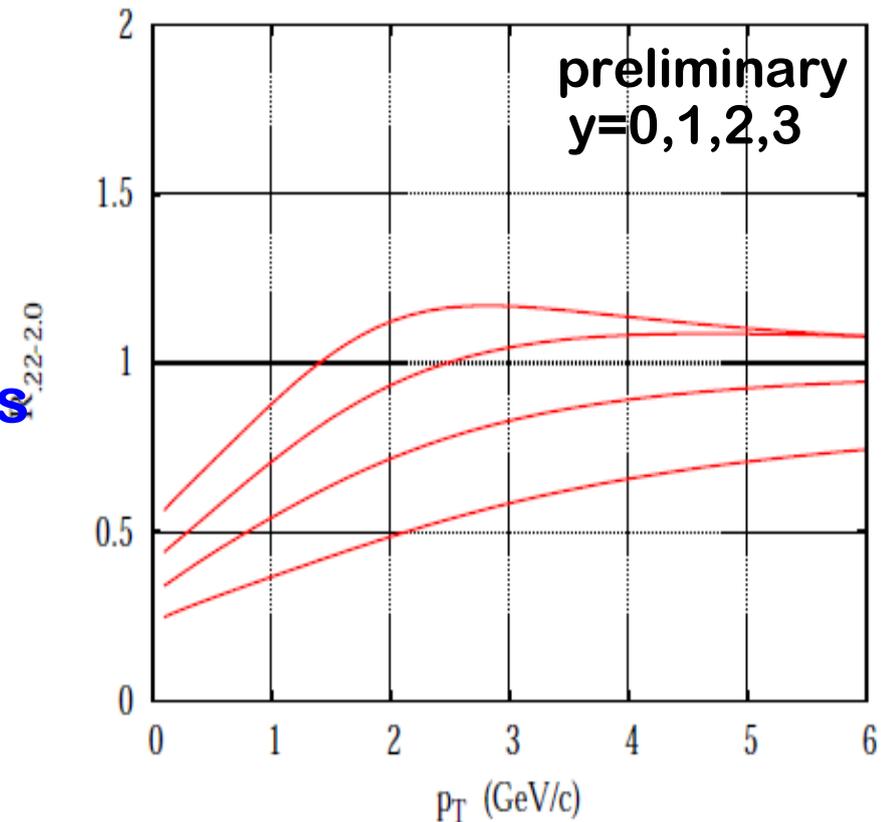
# CGC Framework: x-evolution

- BK equation (large N & A)
  - Evolve from  $x_0=0.01$
  - Nonlinear: gluon fusion effect
  - **Peak moves to higher pT**
  - **RpA suppressed due to faster saturation for A**



# CGC Framework: x-evolution

- BK equation (large N & A)
  - Evolve from  $x_0=0.01$
  - Nonlinear: gluon fusion effect
  - **Peak moves to higher  $p_T$**
  - **RpA suppressed due to faster saturation for A**
  - **Forward suppression for gluons similar to BRAHMS**



# Open charm production

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# Open charm production

- Analytic formula to  $O(\rho_p^1 \rho_A^{\text{infty}})$

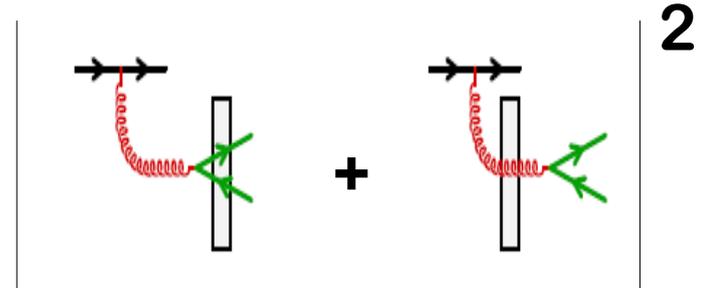
$$\frac{d\sigma_{q\bar{q}}}{d^2\vec{p}_\perp d^2\vec{q}_\perp dy_p dy_q} = \frac{\alpha_s^2 N}{8\pi^4 d_A} \int_{\vec{k}_{1\perp}, \vec{k}_{2\perp}} \frac{\delta(\vec{p}_\perp + \vec{q}_\perp - \vec{k}_{1\perp} - \vec{k}_{2\perp})}{k_{1\perp}^2 k_{2\perp}^2}$$

$$\times \left\{ \int_{\vec{k}_\perp, \vec{k}'_\perp} \text{tr} \left[ (\not{q} + m) T_{q\bar{q}}(\vec{k}_\perp) (\not{p}' - m) T_{q\bar{q}}^*(\vec{k}'_\perp) \right] \phi_A^{q\bar{q}, q\bar{q}}(\vec{k}_{2\perp} | \vec{k}_\perp, \vec{k}'_\perp) \right.$$

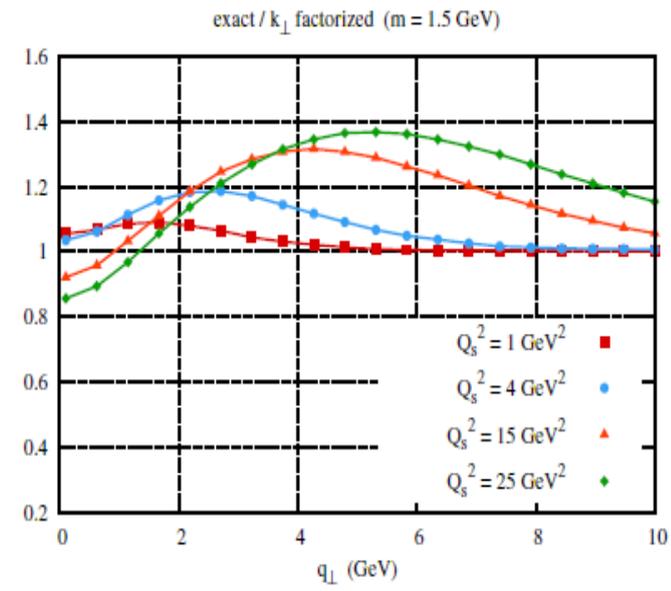
$$+ \int_{\vec{k}_\perp} \text{tr} \left[ (\not{q} + m) T_{q\bar{q}}(\vec{k}_\perp) (\not{p}' - m) L^* + \text{h.c.} \right] \phi_A^{q\bar{q}, g}(\vec{k}_{2\perp} | \vec{k}_\perp)$$

$$\left. + \text{tr} \left[ (\not{q} + m) L (\not{p}' - m) L^* \right] \phi_A^{g, g}(\vec{k}_{2\perp}) \right\} \varphi_p(\vec{k}_{1\perp})$$

hard
nucleus
proton



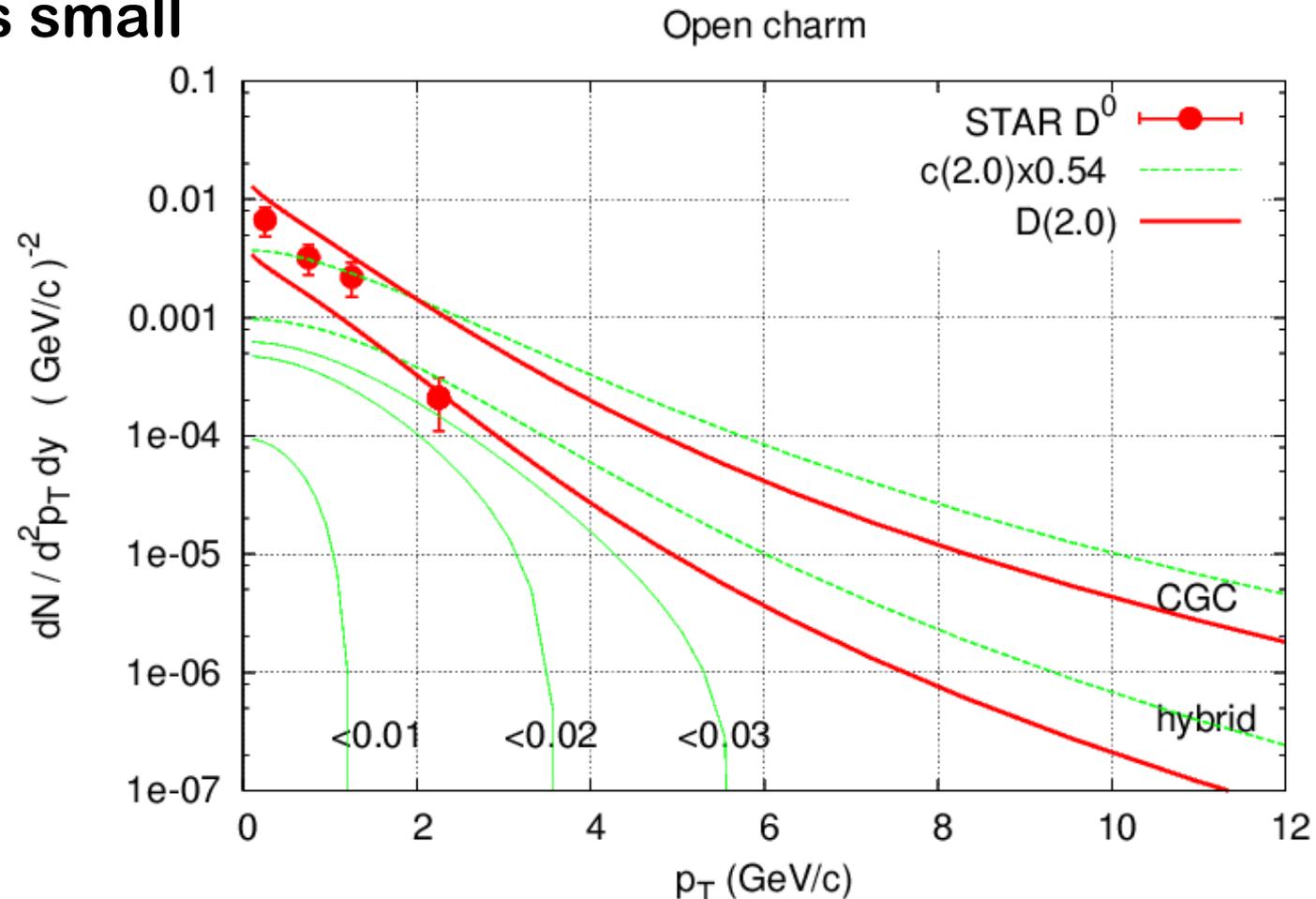
- kT factorization is broken, but small
- Collinear approx for proton may be OK
- = hybrid ; cheaper numerical task



HF, Gelis, Venugopalan

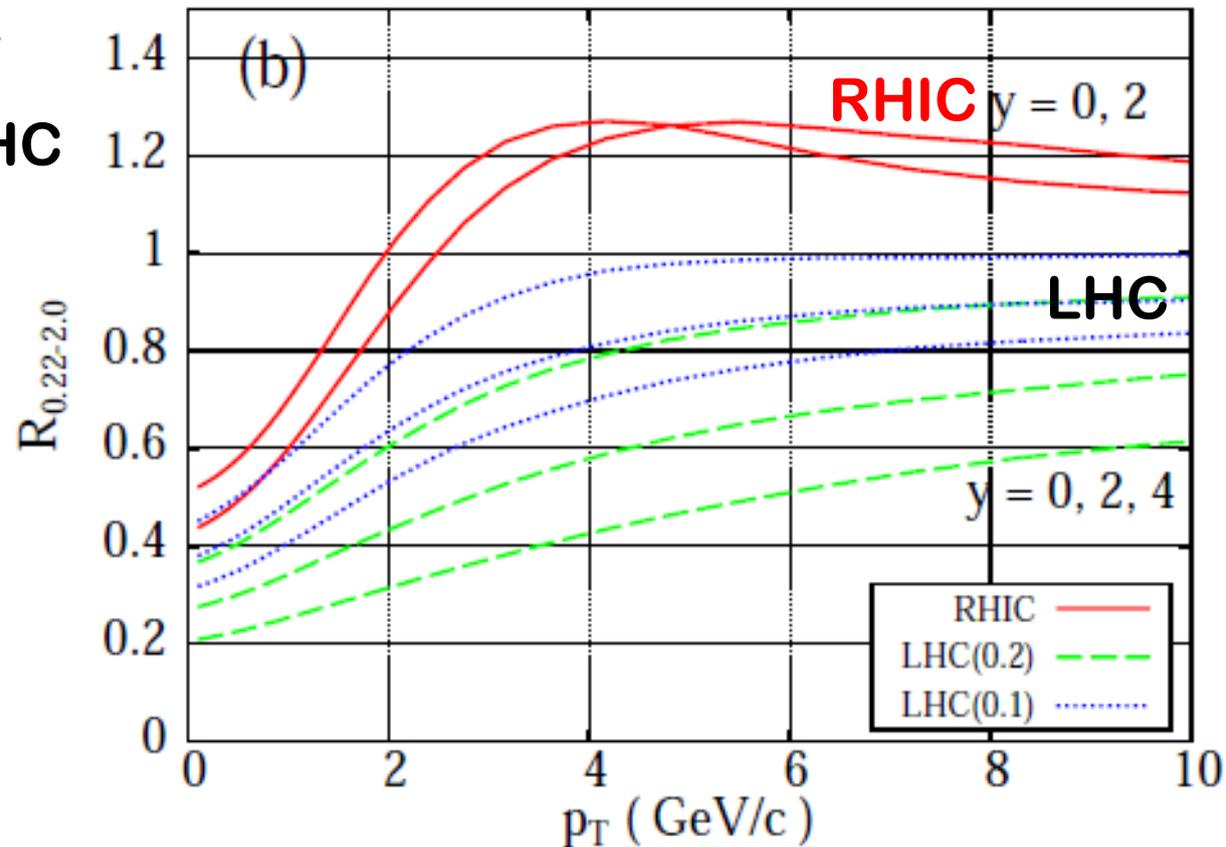
# Open charm production

- **CGC** = uGDF for p & A ; **Hybrid** = uGDF for A and xG for p
  - Hard spectrum in medium- x region
  - Small-x contrib is small
  - Look forward



# Open charm production

- Ratio of pA/pp
- Hybrid:  $R = \text{“xG . uGDF(2.0)”} / \text{“xG . uGDF(0.22)”}$ 
  - Cronin enhancement @ RHIC
  - moves to higher pT w/ y
  - Large suppression @ LHC



# Charmonium

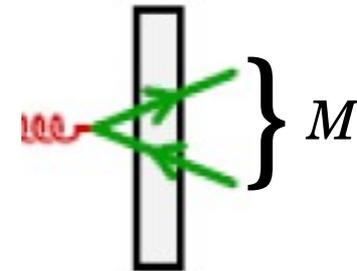
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# Charmonium in CEM

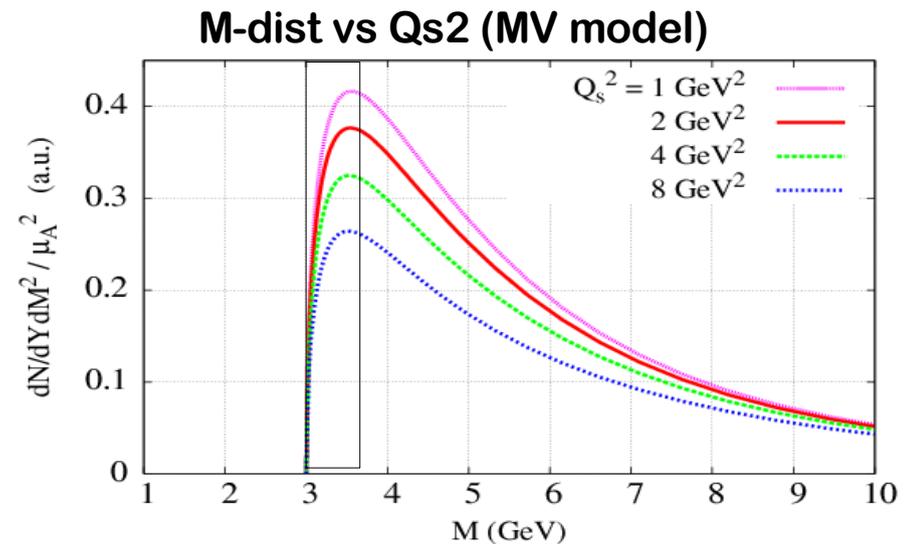
- Color evaporation model:

**Assume separation of pair production and b.s. formations**

$$\frac{dN_{J/\psi}}{dY d^2 P_{\perp}} \Big|_{CEM} = F_{J/\psi} \int_{4m^2}^{4m_D^2} dM^2 \frac{dN}{dY d^2 P_{\perp} dM^2}$$



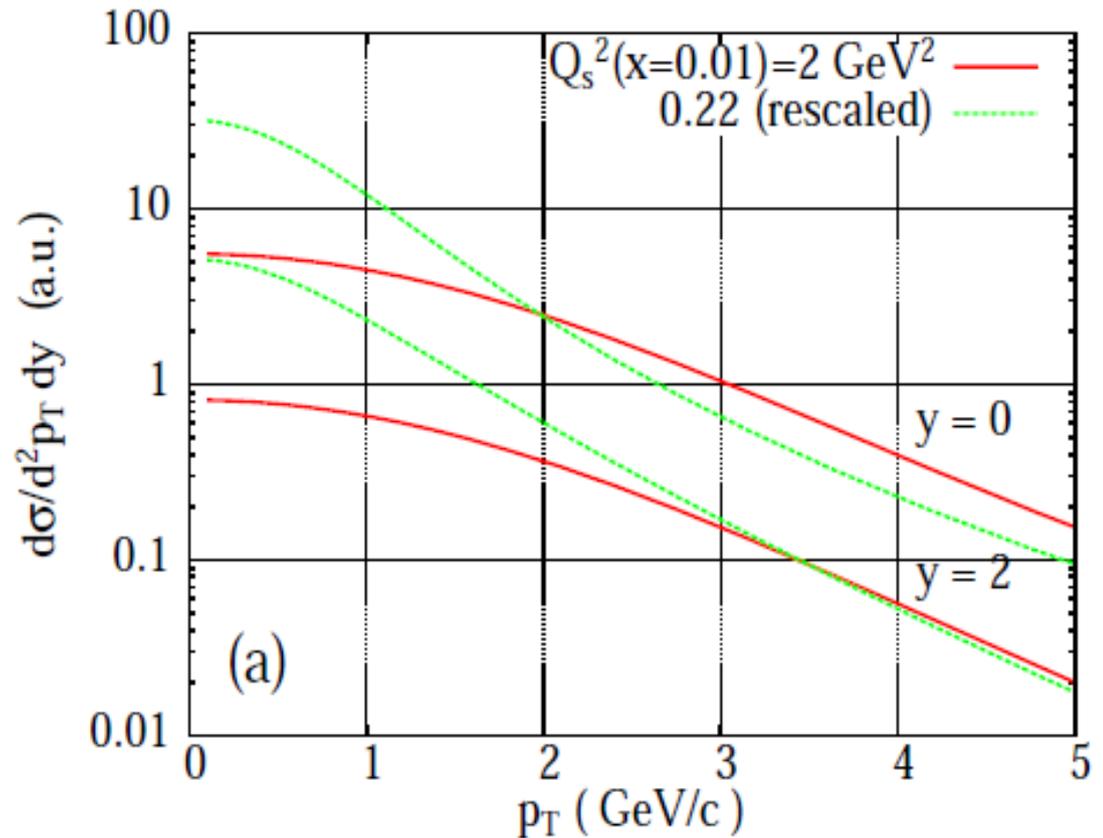
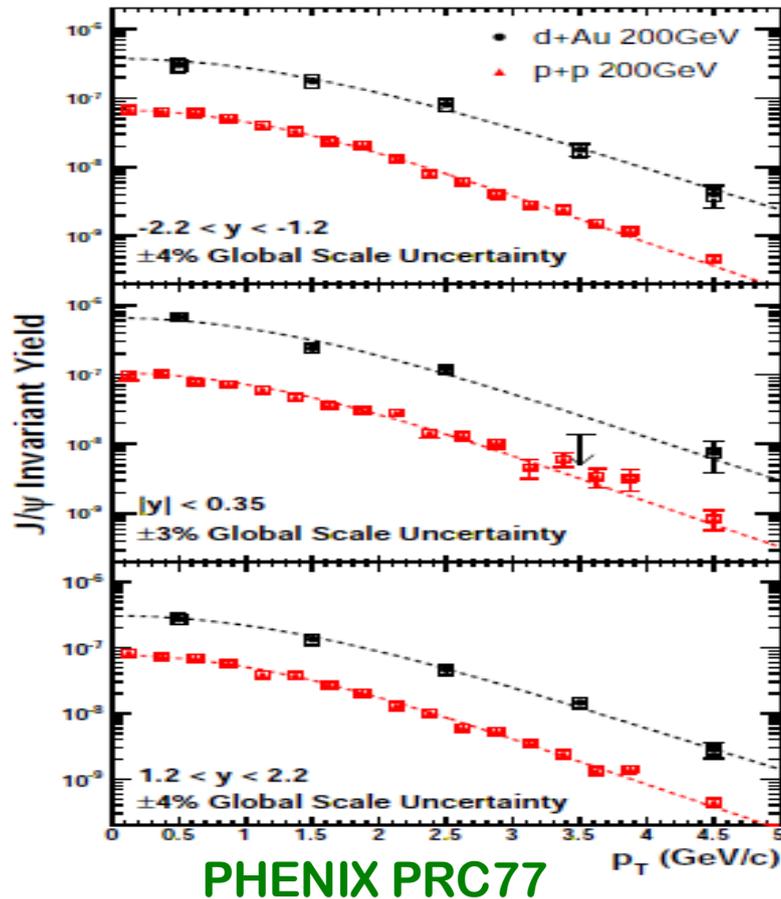
- Effects of dense gluons
  - Initial gluon saturation
  - Multiple scatterings of cc pair



# Charmonium in CEM

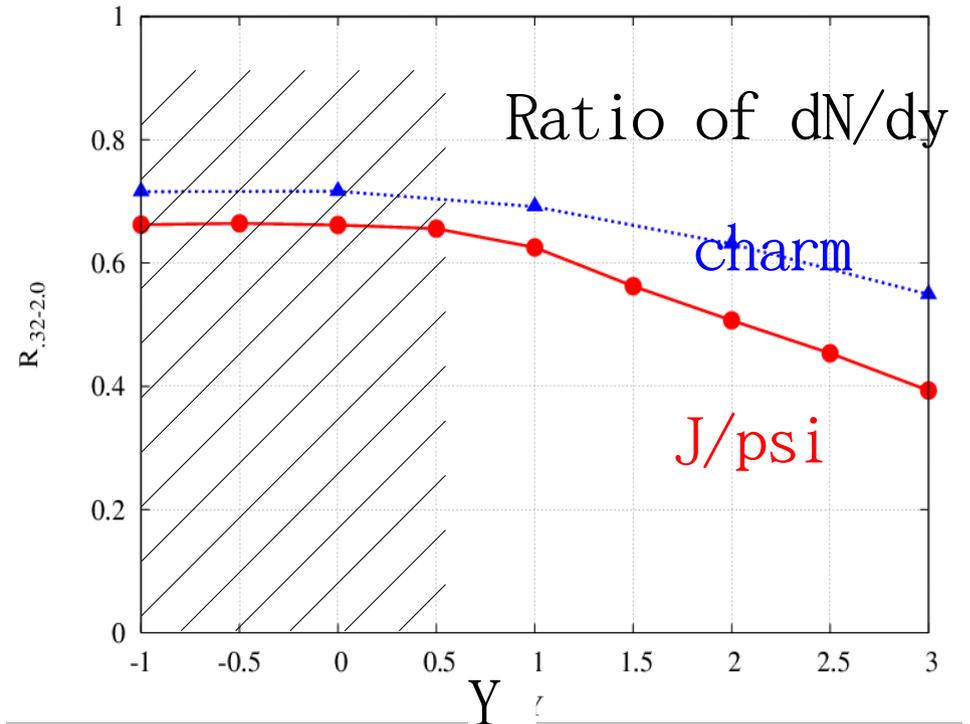
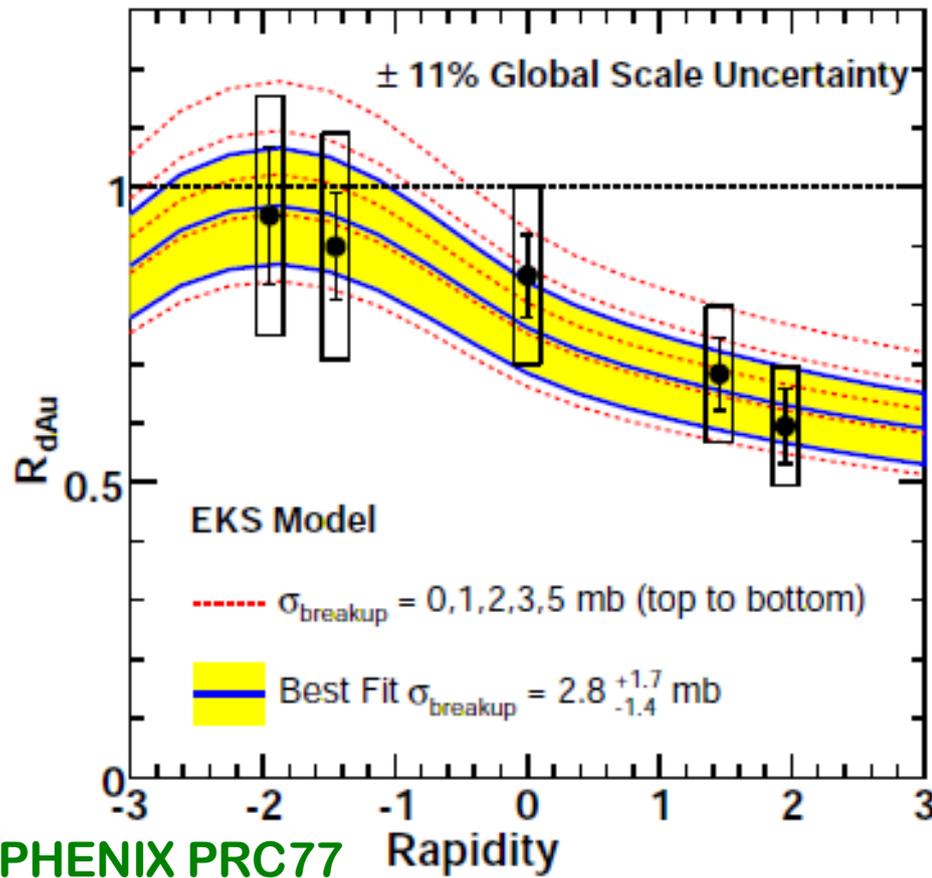
- Momentum distribution
  - Hardened too much
  - Difficulty of model?

hybrid=kT kick only from A or need improve medium-x?



# Charmonium in CEM

- Rapidity dependence of RdA



# Summary and Discussion

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- **CGC model for cc production in pA is presented**
  - **LO( $\alpha_s$ ), but O( $\rho_A^\infty$ )**
  - **Mid-rapidity at RHIC rather insensitive to small-x**
    - **Medium-x part is important**
  - **Saturation is reflected in forward rapidity**
  - **LHC will be best place to see the saturation**
  - **CGC model is still in primitive stage**

# Discussion

- More post-dictions and predictions
  - Improve the CGC model
    - medium-x pdf, onium formation, ..., etc
  - Centrality dep thru  $Q_s(x,b)$
  - AA at very forward  $y$
  - Test the model; azimuthal correlation of cc
    - intrinsic  $kT$  & multiple scattering

Just preliminary

