

Initial conditions at RHIC

for hydrodynamics

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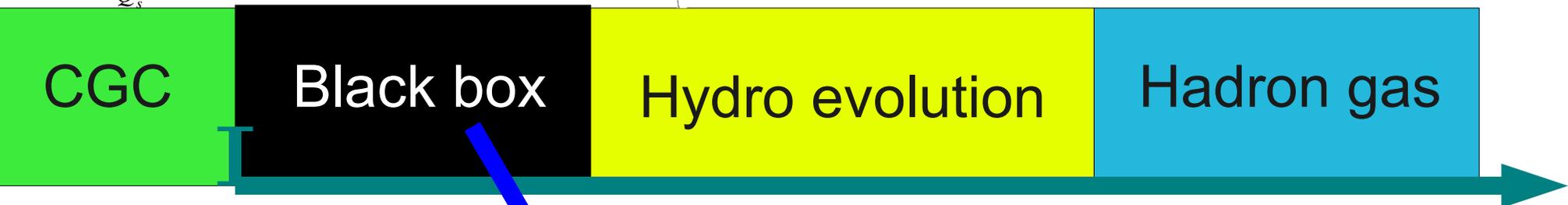
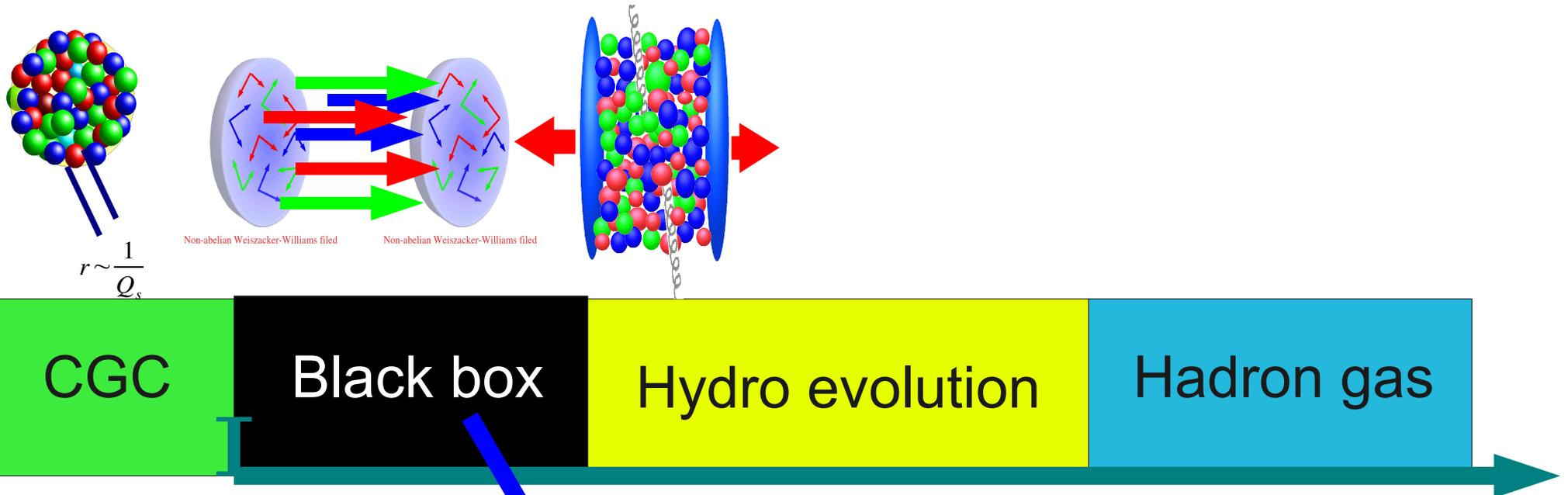
- CGC initial conditions, KLN, fKLN, MC-KLN.
- Eccentricity fluctuations within MC-KLN
- Initial fluctuations + hydrodynamics + hadronic cascade results for elliptic flow in Cu+Cu and Au+Au collisions.

Hydrodynamics and inputs

- **Initial condition: how to start**
thermalization time
energy density
(flow profile)
- **Equation of state and dissipative effects:**
how to evolve
ideal gas EoS, lattice QCD
- **Freezeout: how to stop**
Hadron cascade after burner
(hadronic dissipative effects)

Purpose: test uncertainties of the initial conditions.

High energy heavy ion collisions

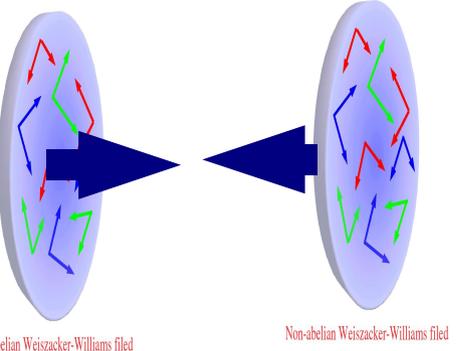


$\tau = 0$ $\tau \approx 1/Q_s$ $\tau \approx 1 \text{ fm}/c$ Reaction time

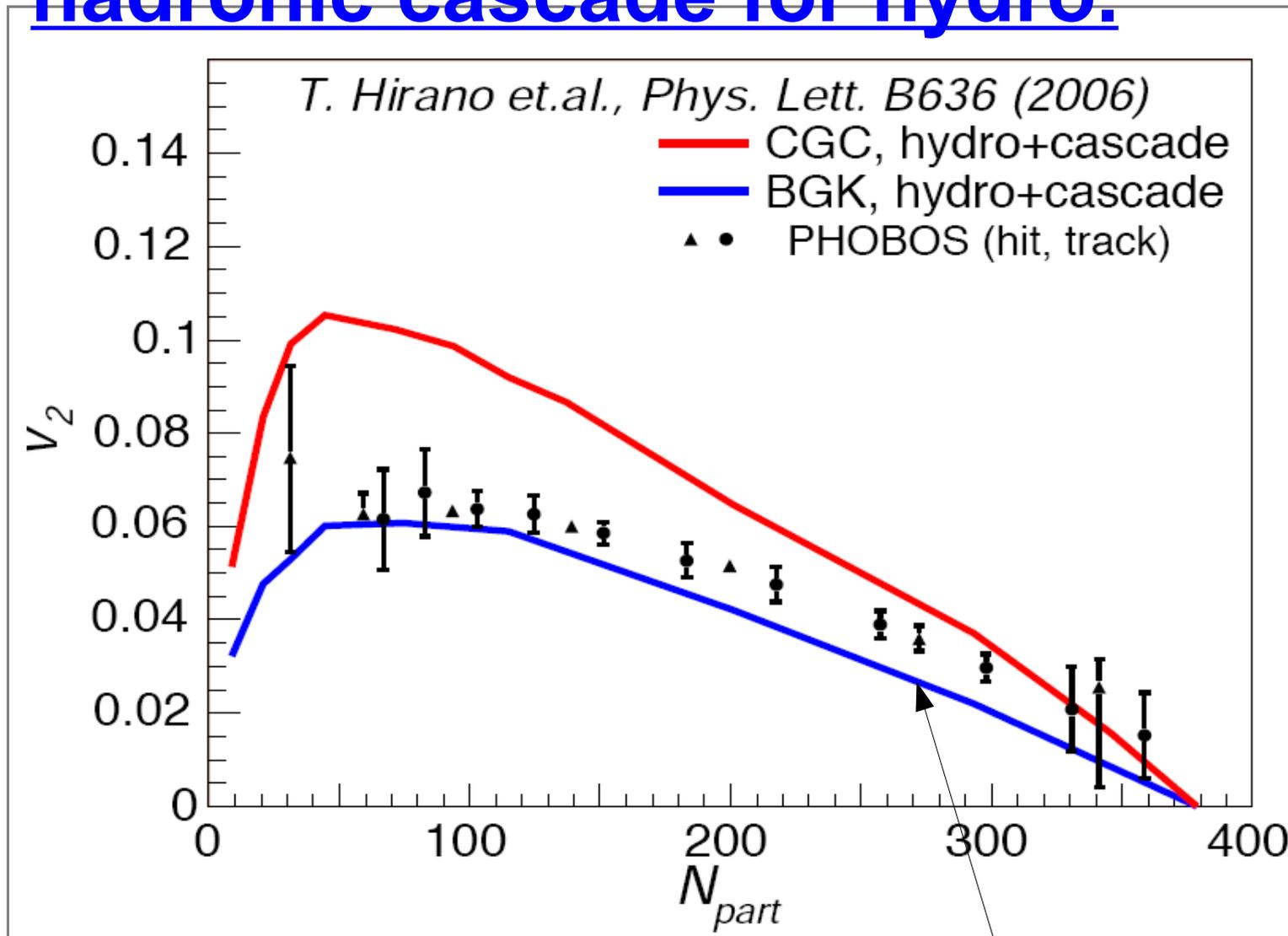
Strong longitudinal color field \rightarrow particle

Gluon production

Pre-equilibrium dynamics unknown



Effects of Initial condition and hadronic cascade for hydro.



Glauber + Ideal hydro + hadronic cascade underestimates

Initial transverse geometry

Glauber model

$$\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim N_{part,1}(\mathbf{x}_\perp) + N_{part,2}(\mathbf{x}_\perp)$$

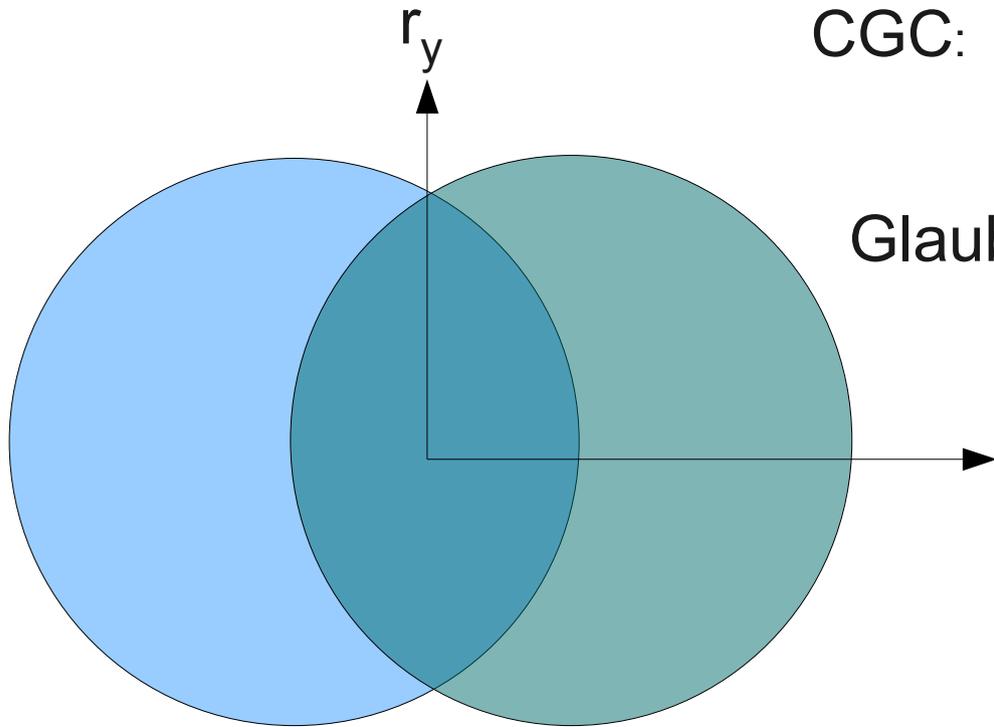
Initial energy density or entropy is taken from
Wounded nucleon model:
number of participants or collision scaling.

Color Glass Condensate (KLN)

$$\frac{dN_g}{d^2 x_t dy} = \frac{4\pi N_c}{N_c^2 - 1} \int \frac{d^2 p_t}{p_t^2} \int d^2 k_t \alpha_s \phi(x_1, k_t^2) \phi(x_2, (p_t - k_t)^2)$$

$$\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim \min \{ Q_{s,1}^2(\mathbf{x}_\perp), Q_{s,2}^2(\mathbf{x}_\perp) \} \sim \min \{ N_{part,1}(\mathbf{x}_\perp), N_{part,2}(\mathbf{x}_\perp) \}$$

Why large eccentricity in KLN?



CGC: $\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim \min \{ N_{part,1}(\mathbf{x}_\perp), N_{part,2}(\mathbf{x}_\perp) \}$

Glauber: $\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim N_{part,1}(\mathbf{x}_\perp) + N_{part,2}(\mathbf{x}_\perp)$

$\rho_{\text{Glauber}}(0, r_y) \sim \rho_{\text{CGC}}(0, r_y)$

$\rho_{\text{Glauber}}(r_x, 0) > \rho_{\text{CGC}}(r_x, 0)$

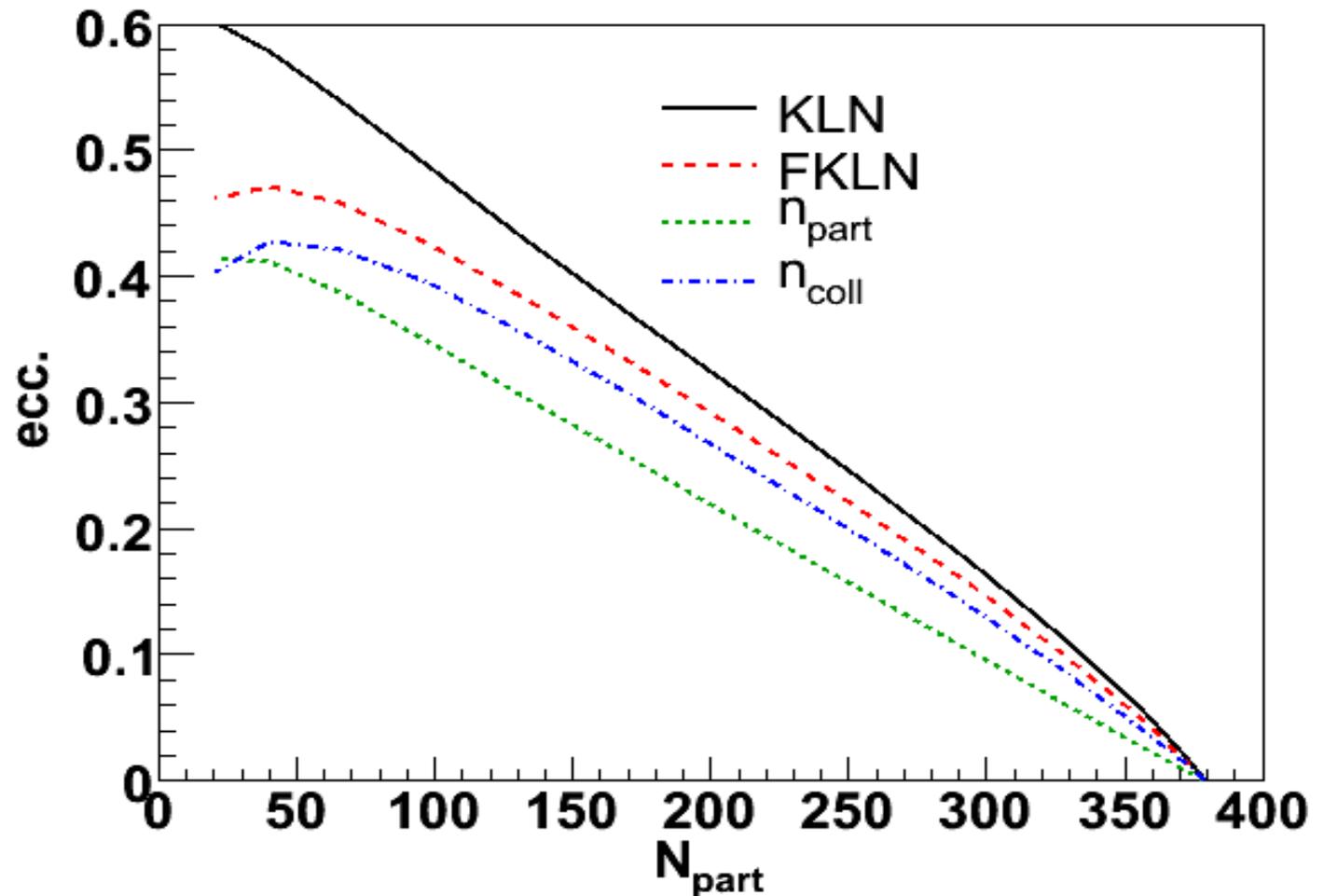
$\rho_{\text{glauber}} \sim (N_{part,1}(r_x, 0) + N_{part,2}(r_x, 0))$

$\rho_{\text{CGC}} \sim \min \{ N_{part,1}(r_x, 0), N_{part,2}(r_x, 0) \}$

$\epsilon_{\text{CGC}} > \epsilon_{\text{Glauber}}$

Eccentricity from KLN and fKLN

$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle x^2 + y^2 \rangle}$$

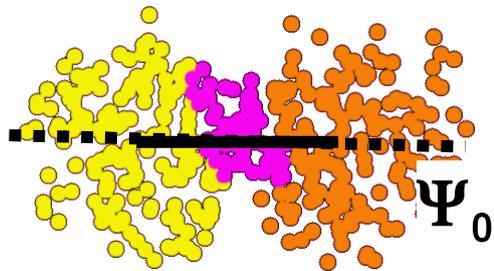


fKLN: Correct treatment of surface of nucleus:
minimum saturation scale is set to the saturation scale
of nucleon.

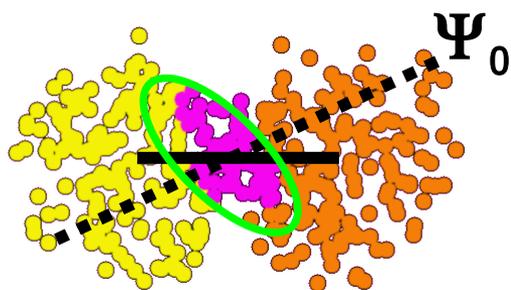
Eccentricity fluctuations

Event-by-event fluctuations in the shape of the initial collision zone for small systems or small transverse overlap regions may be important.

Specifically **fluctuations in the nucleon positions.**



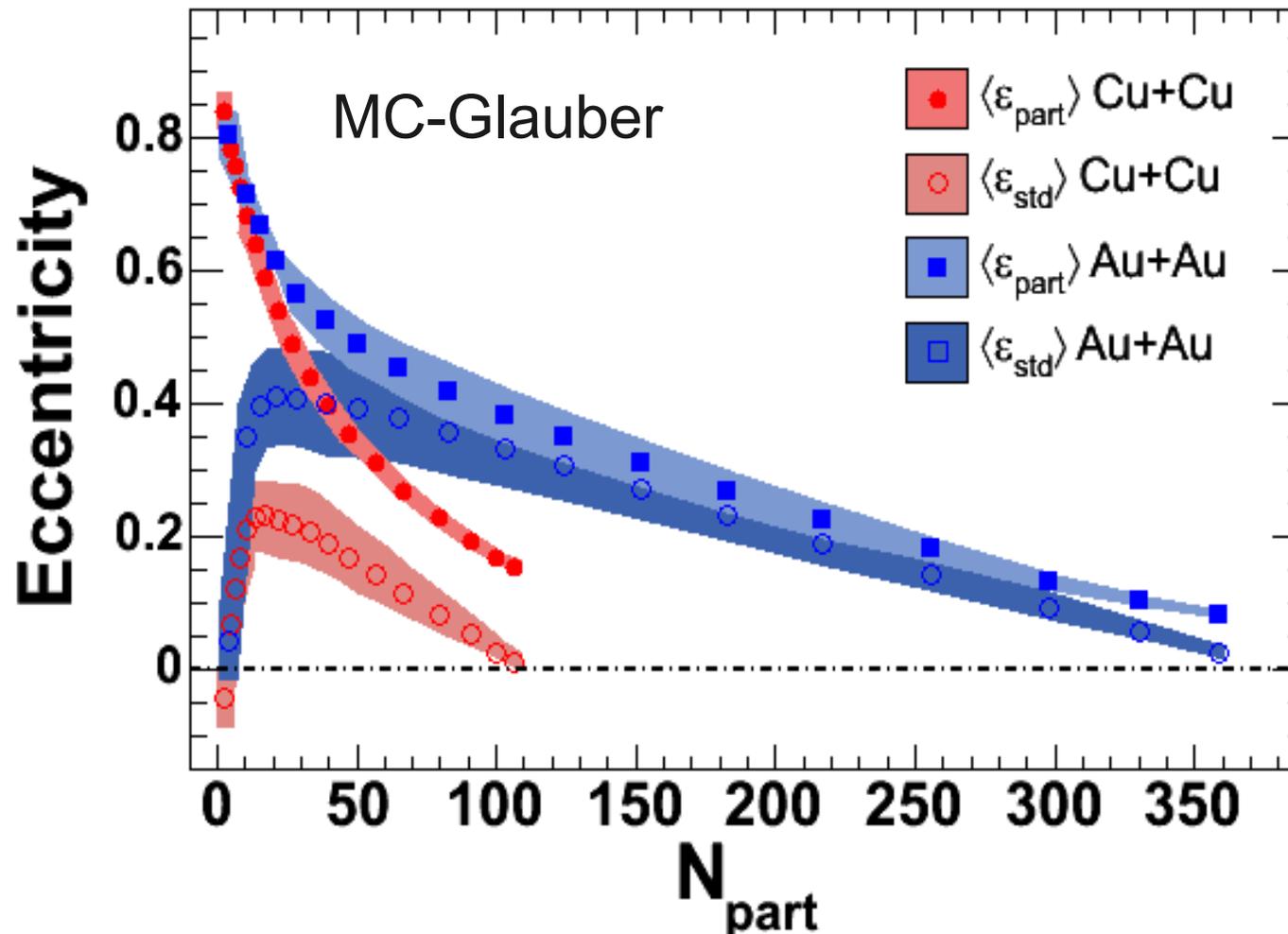
$$\epsilon_{\text{std}} = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$



$$\langle \epsilon_{\text{part}} \rangle = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

$$\sigma_x^2 = \langle x^2 \rangle - \langle x \rangle^2, \quad \sigma_y^2 = \langle y^2 \rangle - \langle y \rangle^2, \quad \sigma_{xy}^2 = \langle xy \rangle - \langle y \rangle \langle x \rangle$$

Eccentricity is large



ϵ was underestimated in early hydro calculations:
it is increased by fluctuations in the positions of nucleons
within the nucleus.

Monte-Carlo version of KLN (MC-KLN)

- Sample A and B nucleons according to the Woods-Saxon distribution.
- Local density of nucleons is obtained by

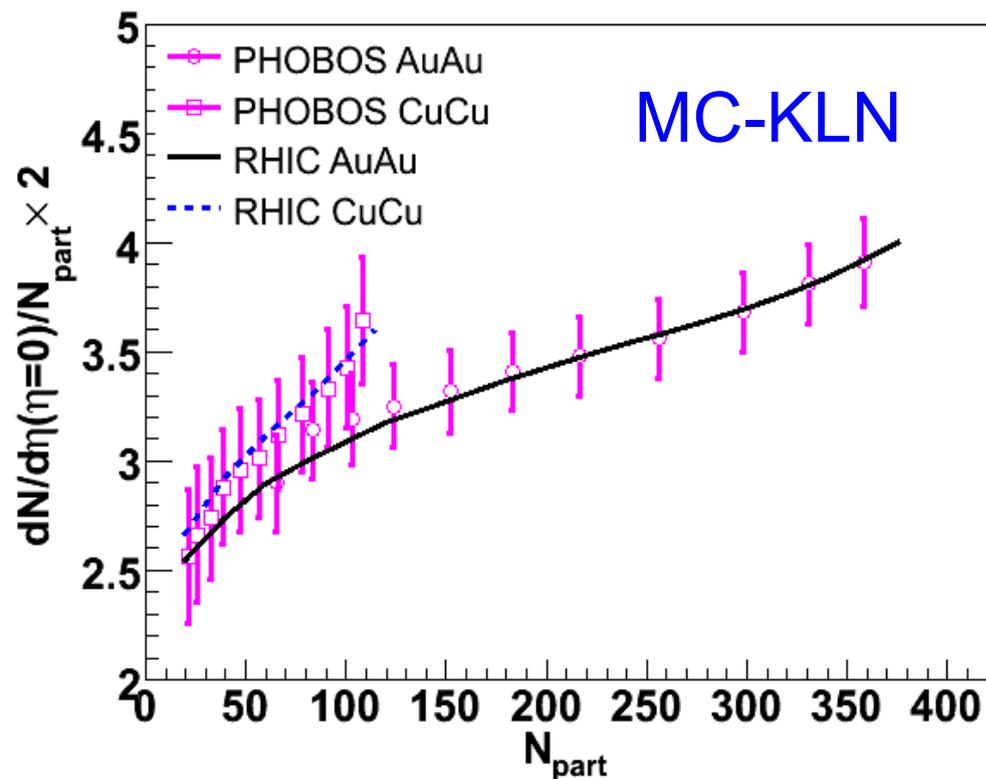
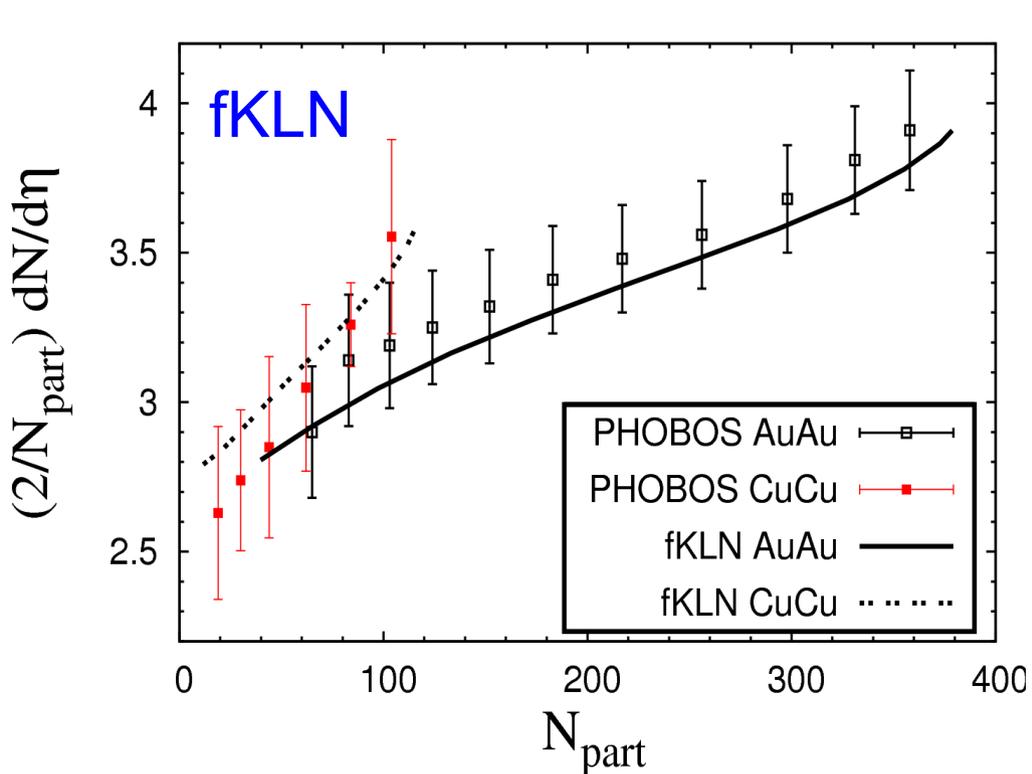
$$t_A(r_{\perp}) = \frac{\textit{number of nucleons}}{S}$$

- Saturation scale at a given transverse coordinate is given by

$$Q_{s,A}^2(r_{\perp}) = 2\text{GeV}^2 \left(\frac{t_A(r_{\perp})}{1.53} \right) \left(\frac{0.01}{x} \right)^{\lambda}$$

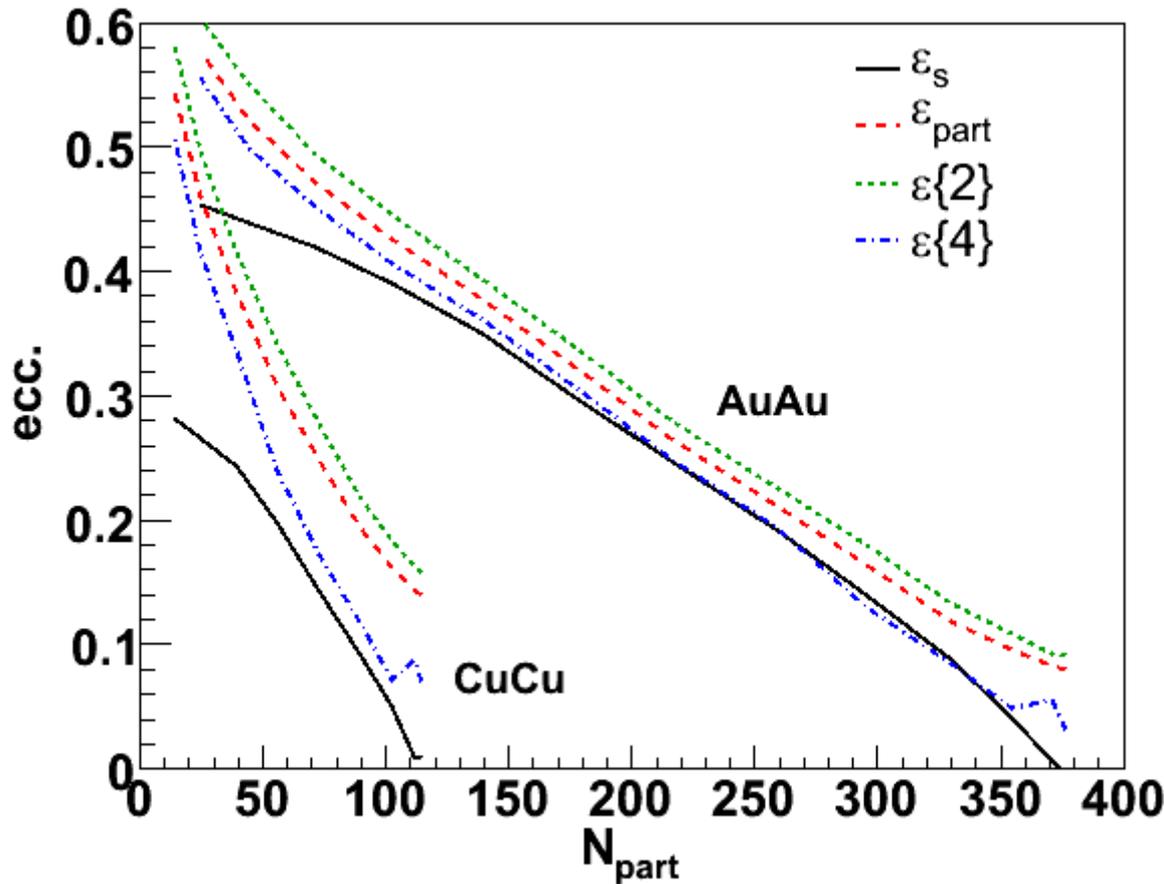
- For each generated configuration, we apply the k_t-factorization formula at each transverse coordinate.
- Average over many events.

Comparison of Multiplicities in Au+Au and Cu+Cu collisions



Better fit when fluctuations are included.

Eccentricity Fluctuations from MC-KLN



$$\epsilon_{part} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

$$\sigma_{xy} = \langle xy \rangle - \langle x \rangle \langle y \rangle$$

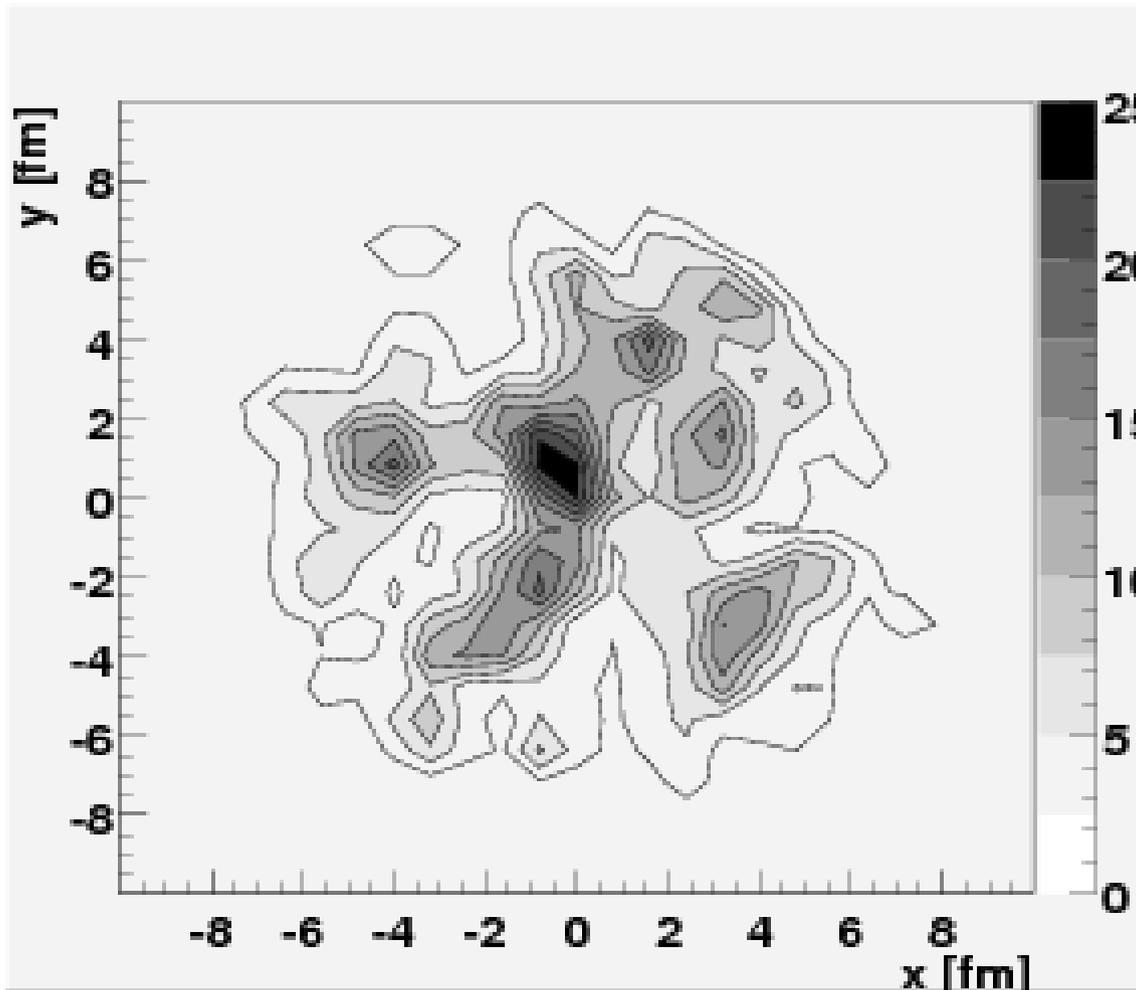
$$\sigma_x^2 = \langle x^2 \rangle - \langle x \rangle^2$$

$$\epsilon\{2\} = \sqrt{\langle \epsilon_{part}^2 \rangle}$$

$$\epsilon\{4\} = (2\langle \epsilon_{part}^2 \rangle^2 - \langle \epsilon_{part}^4 \rangle)^{1/4}$$

event-by-event fluctuations in hydro?

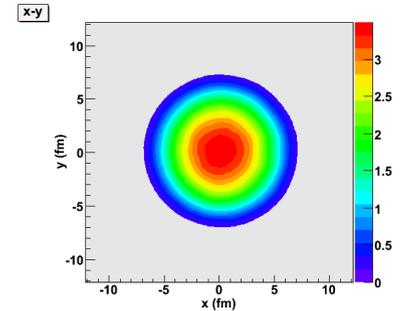
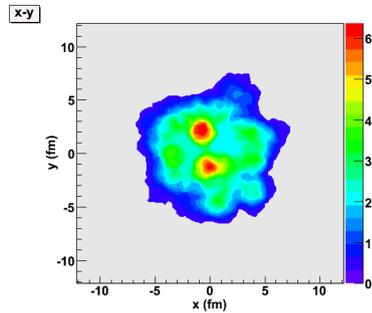
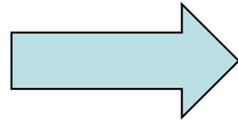
Y. Hama, R. Peterson, G. Andrade, F. Grassi, W. Qian, T. Osada, C. Aguiar, T. Kodama



Initial condition for Au+Au
from NeXus

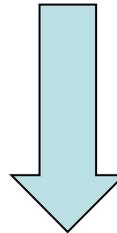
Initial Condition with an Effect of Eccentricity Fluctuation

Throw a dice to choose b :
 $b_{\min} < b < b_{\max}$

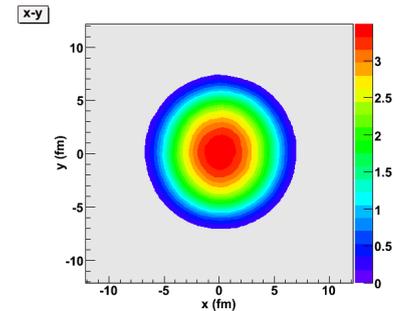
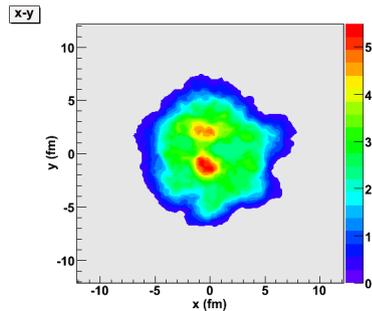


average
over events

Rotate to real
reaction plane



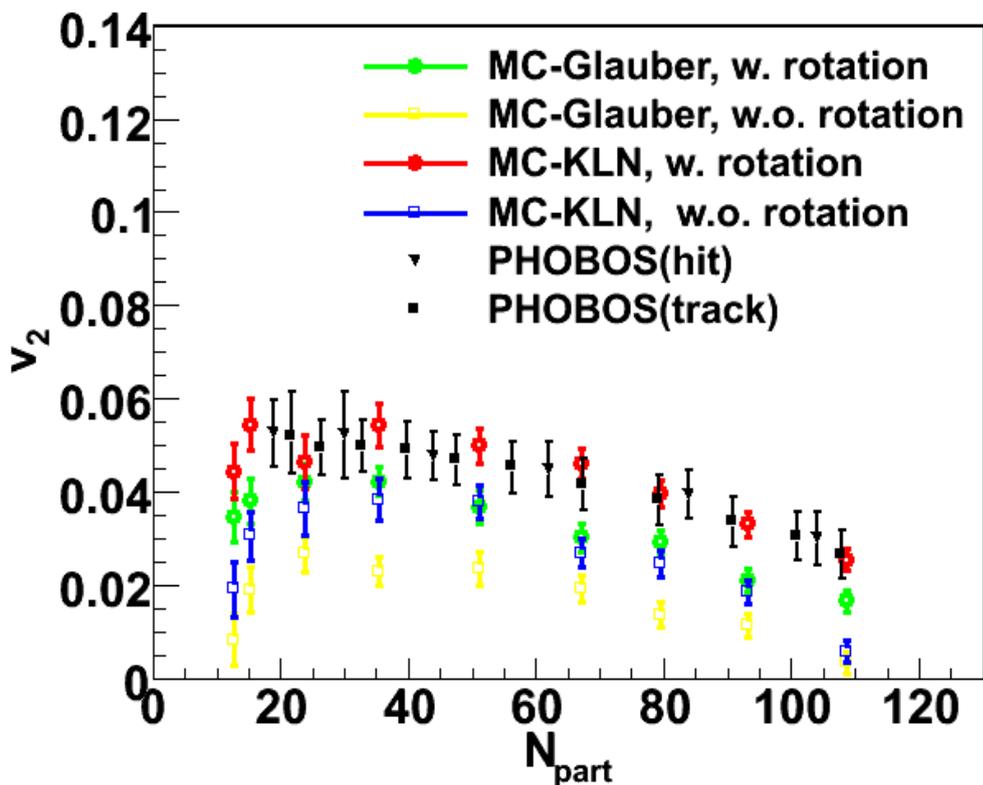
E.g.)
 $b_{\min} = 0.0\text{fm}$
 $b_{\max} = 3.3\text{fm}$
in Au+Au collisions
at 0-5% centrality



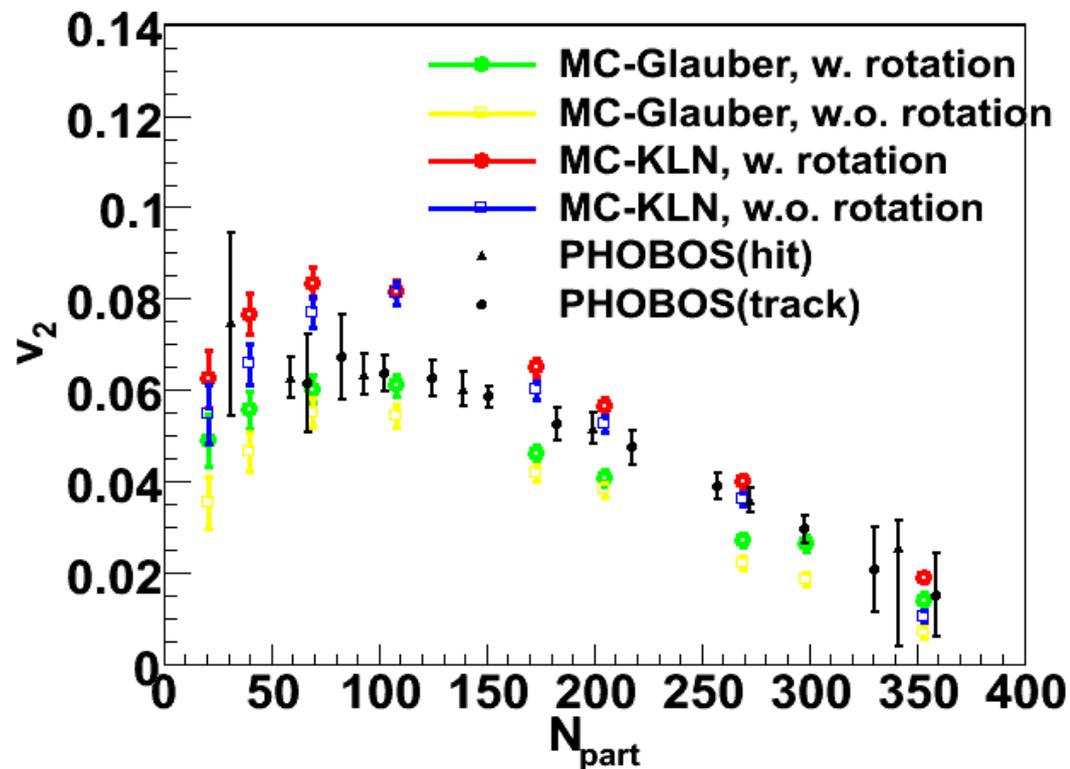
average
over events

Initial fluctuations+Hydro+Hadron cascade

Cu+Cu



Au+Au

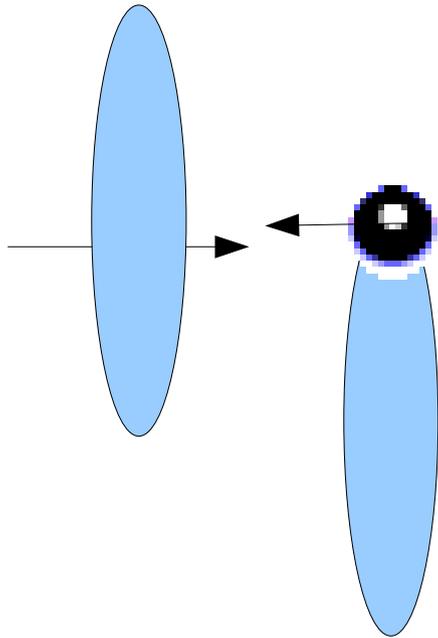


summary

- We presented the results of hydro+hadron cascade with initial eccentricity fluctuations within MC-Glauber and CGC (MC-KLN model).
 - Eccentricity larger and elliptic flow also larger.
 - Explain elliptic flow at central collisions.
 - Glauber initial condition **underestimates** the elliptic flow data.
 - CGC initial condition slightly **overestimates** the data.

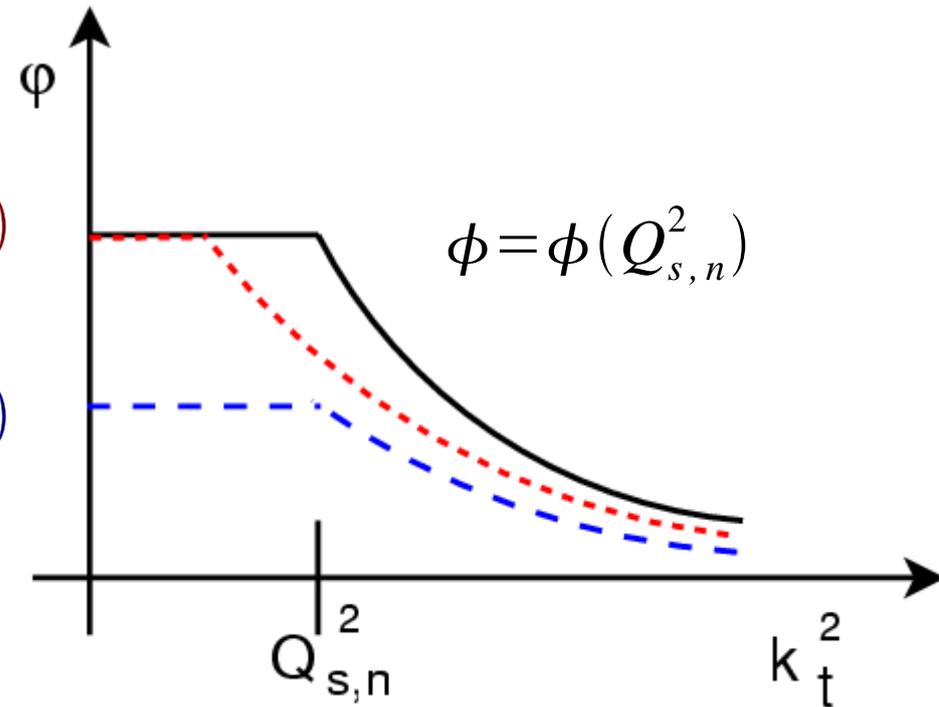
Main uncertainty in this work is the effect of EoS

How to implement universal saturation scale in KLN framework?



$$\phi_A = \phi(p_A Q_{s,n}^2)$$

$$\phi_A = p_A \phi(Q_{s,n}^2)$$



Saturation scale for nucleon

P_A Probability to find at least one nucleon at a given transverse coordinate.

$$\phi_A = p_A \phi\left(\frac{T_A}{p_A}\right)$$

$$T_{1,A} = \frac{\sum_{i \geq 0} p(i) t_A(i)}{\sum_{i \geq 1} p(i)} = \frac{T_A}{p_A}$$

fKLN Ansatz

$$\frac{dN_g}{d^2 x_\perp dy} = \frac{4\pi N_c}{N_c^2 - 1} \int \frac{d^2 p_t}{p_t^2} \int d^2 k_t \alpha_s p_A p_B \phi(T_A/p_A) \phi(T_B/p_B)$$

$$\frac{dN}{dy} \sim \min\{Q_{s,A}^2, Q_{s,B}^2\}$$

$$\approx \int \frac{d^2 p_t}{p_t^2} \int d^2 k_t \phi(p_A p_B T_A/p_A) \phi(p_A p_B T_B/p_B)$$

$$= \int \frac{d^2 p_t}{p_t^2} \int d^2 k_t \phi(n_{part,A}) \phi(n_{part,B}) \quad \text{Recover original KLN!}$$

If we take $p_A = 1 - (1 - \sigma_{NN} T_A/A)^A$