# Jet Energy Loss and Photon Production in QGP – Putting it all together –

Guangyou Qin,

*McGill-AMY Group:* S. Turbide, C. Gale, G. D. Moore Sangyong Jeon

Department of Physics McGill University

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# Energy loss (jet quenching)

# Photons

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## E-loss - The Issue

- QGP makes jets lose energy
  - Radiational (Inelastic)



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# E-loss - The Big Picture

•  $\sum \left( f_{a/A} \otimes f_{b/A} \otimes \frac{d\sigma_{ab \to cd}}{dx} \right) \otimes (\text{E-loss module}) \otimes D_{\text{frag}}$ 

- Parton-parton scattering:  $\left(f_{a/A} \otimes f_{b/A} \otimes \frac{d\sigma_{ab \to cd}}{dx}\right)$
- D<sub>frag</sub>: As in vacuum but with reduced energy.
- Energy loss module Three separate pieces
  - Energy change rate:  $\frac{d\Gamma}{dtdk}(\epsilon, k; T)$ : Thermal QCD
  - Evolution (q, g coupled + keeps track of the radiated q, g):

$$\frac{dP(\epsilon,t)}{dt} = \int dk \frac{d\Gamma(\epsilon+k,k)}{dtdk} P(\epsilon+k,t) - \int dk \frac{d\Gamma(\epsilon,k)}{dtdk} P(\epsilon,t)$$

•  $T(\mathbf{x}, t), u^{\mu}(\mathbf{x}, t)$ : Must be obtained independently.

• Still schematic. There are theoretical and conceptual problems to further consider.

- Uses *full leading order* thermal QCD/QED rates LPM and BH limits are both correctly included.
- Dynamic medium: Thermal quarks and gluons in the medium. *T* and *α<sub>s</sub>* characterizes the medium.
- Keeps track of radiated gluons and  $q\bar{q}$  pairs.
- Thermal absorption included.
- The "jet" propagates in a hydrodynamically evolving medium.
- Flow is taken into account: Perform calc in the local rest frame, and then boost back to the lab frame.

# Rough Idea - Radiational (following BDMPS)



- Point here: Radiated gluon also undergoes multiple scatterings.
- Bethe-Heitler Spectrum (low  $\omega$ )

$$\omega \frac{dI}{d\omega} \approx \frac{\alpha_s N_c}{\pi}$$

Medium dependence comes through a scattering length scale /

$$\omega \frac{dI}{d\omega dz} \approx \frac{1}{I} \frac{\alpha_s N_c}{\pi}$$

# Rough Idea - Radiational (following BDMPS)

• If all scatterings are incoherent

$$I = I_{\rm mfp} = 1/\rho\sigma$$
 and  $\omega \frac{dI}{d\omega dz} \approx \frac{\alpha_s N_c}{\pi I_{\rm mfp}}$ 

Coherence matters when multiple scatterings are needed to get O(1) phase change: 1 ~ l<sub>coh</sub>ω(1 − k̂·v̂) ~ l<sub>coh</sub>ω ⟨θ<sup>2</sup>⟩
 Both the radiated gluon and the original parton undergo random walk:

$$\left\langle \theta^2 \right\rangle \approx N_{\rm coh} \left( \bar{\theta}_g^2 + \bar{\theta}_q^2 \right) \approx \frac{I_{\rm coh}}{I_{\rm mfp}} \left( \frac{\mu^2}{\omega^2} + \frac{\mu^2}{E^2} \right)$$

or

$$I_{\rm coh} = I_{\rm mfp} \sqrt{\frac{\omega}{E_{\rm LPM}}} \sqrt{\frac{E^2}{E^2 + \omega^2}}$$
 and  $\omega \frac{dI}{d\omega dz} \approx \frac{\alpha_s N_c}{\pi I_{\rm mfp}} \sqrt{\frac{E_{\rm LPM}}{\omega}}$ 

for  $E \gg \omega$  and  $\omega > E_{\text{LPM}} \equiv \mu^2 I_{\text{mfp}} \sim T$ .

# Rough Idea - Collisional (Following Bjorken)



Energy loss per unit length

$$rac{dE}{dz}pprox\int d^3k\,
ho(k)\,\int dq^2\,(1-\cos heta_{
ho k})\Delta Erac{d\sigma^{
m el}}{dq^2}$$

#### where

- ho(k): density,  $(1 \cos \theta_{
  hok}) \Delta E \approx q^2/2k$ : flux factor
- Elastic cross-section (Coulombic)  $\frac{d\sigma}{dq^2} \approx C_R \frac{2\pi \alpha_s^2}{(q^2)^2}$

• with thermal  $\rho$ , this yields

$$\left(\frac{dE}{dz}\right)_{\rm coll} \propto \alpha_s^2 T^2 \ln(E/\alpha_s T)$$

• Compare:

$$\left(\frac{dE}{dz}\right)_{\rm rad} \propto \alpha_s^2 T \sqrt{TE}$$

• NOTE: We actually need  $\omega dl/d\omega dz$  in place of dE/dz.

Use BDMPS expression for the quenching factor for  $1/p^n$  with a large *n* but with the energy range extended to  $\omega < 0$ :

$$\mathcal{R}_{AA}(p) pprox \exp\left(-\int_{-\infty}^{\infty} d\omega \, \int_{0}^{t} dt' \, (d\Gamma_{\mathrm{inel+el}}/d\omega dt)(1-e^{-\omega n/p})
ight)$$

For the radiation rate, use simple estimates

$$\frac{d\Gamma}{d\omega dt} \approx \frac{\alpha}{\pi \omega} \frac{N_c}{I_{\rm mfp}} \text{ for } 0 < \omega < I_{\rm mfp} \mu^2$$

$$\frac{d\Gamma}{d\omega dt} \approx \frac{\alpha}{\pi \omega} N_c \sqrt{\frac{\mu^2}{I_{\rm mfp}\omega}} \text{ for } I_{\rm mfp} \mu^2 < \omega < I_{\rm mfp} \mu^2 (L/I_{\rm mfp})^2$$

$$\frac{d\Gamma}{d\omega dt} \approx \frac{\alpha}{\pi |\omega|} \frac{N_c}{I_{\rm mfp}} e^{-|\omega|/T} \text{ for } \omega < 0$$

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# Rough Idea - R<sub>AA</sub>

For elastic energy loss,

$$\begin{aligned} \mathcal{R}_{AA}^{\mathrm{el}} &\approx & \exp\left(-\int_{-\infty}^{\infty} d\omega \int_{0}^{t} dt' \, (d\Gamma_{\mathrm{el}}/d\omega dt)(1-e^{-\omega n/p})\right) \\ &\approx & \exp\left(-t\left(\frac{dE}{dt}\frac{K(\omega_{0})}{|\omega_{0}|}\right)\right) \\ &\approx & \exp\left(-t\left(\frac{dE}{dt}\right)\left(\frac{n}{p}\right)\left(1-\frac{nT}{p}\right)\right) \end{aligned}$$

valid for p > nT and we used

$$\begin{aligned} \mathcal{K}(\omega_0) &= (1+n_B(|\omega_0|))(1-e^{-|\omega_0|n/p}) + n_B(|\omega_0|)(1-e^{|\omega_0|n/p}) \\ &\approx |\omega_0|\left(\frac{n}{p}\right)\left(1-\frac{nT}{p}\right) \quad \text{for small } \omega_0 \end{aligned}$$

A (10) > A (10) > A (10)

# Rough Idea - R<sub>AA</sub>



- Upper line: Without elastic
- Lower line: With elastic
- Flat *R* is produced in both cases up to O(10 T).
- R just not that sensitive to p in the RHIC-relevant range.





HTL resummed

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# Why is this so hard?

 Collinear enhancement in photon & gluon radiations Aurenche, Gelis, Kobes and Zaraket, PRD58:085003,1998, Arnold, Moore and Yaffe (AMY), JHEP 0206:030,2002; JHEP 0112:009,2001; JHEP 0111:057,2001



## Photon SD (Simpler) – Sketch



$$F(P, P + K) = G_R(P)G_A(P + K)V(P, K)$$
  
+  $G_R(P)G_A(P + K)\mathcal{G}(Q)F(P - Q, P - Q + K)$ 

Bare vertex: V(P, K), Resummed vertex: F(P, K)
p<sup>0</sup> integrated legs (with K<sup>2</sup> = 0):

$$\int dp^0 G_R(P+K) G_A(P) \approx$$

$$\int dp^0 \frac{1}{E_{pk} E_p} \frac{1}{p^0 + k^0 - E_{pk} - i\Gamma_{pk}/2} \frac{1}{p^0 - E_p + i\Gamma_p/2}$$

$$\approx \frac{i}{E_{pk} E_p} \frac{1}{\delta E(p,k) - i(\Gamma_{pk} + \Gamma_p)/2}$$
(GIII)

## Photons – Cont.

• Integral eq (schematic):

 $(i\delta E(P,K) + \Gamma)F(P,P+K) = V(P,K) + \mathcal{G}(Q)F(P-Q,P-Q+K)$ or

$$i\delta E(P,K)F(P,P+K) = V(P,K) + \mathcal{G}(Q)[F(P-Q,P-Q+K) - F(P,P+K)]$$

•  $\Gamma$  turned out to be independent of P, K:

$$\Gamma \approx \int_Q \mathcal{G}(Q)$$

with

$$\mathcal{G} = \frac{m_D^2}{\mathbf{q}_\perp^2(\mathbf{q}_\perp^2 + m_D^2)}$$

# Gluon radiation is similar but more complicated ...



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# SD equation for the vertex

Equation for the vertex F

$$\begin{aligned} \mathbf{2h} &= i\delta E(\mathbf{h}, p, k)\mathbf{F}(\mathbf{h}) + g^2 \int \frac{d^2\mathbf{q}_{\perp}}{(2\pi)^2} C(\mathbf{q}_{\perp}) \times \\ &\times \Big\{ (C_s - C_A/2) [\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} - k \, \mathbf{q}_{\perp})] \\ &+ (C_A/2) [\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} + p \, \mathbf{q}_{\perp})] \\ &+ (C_A/2) [\mathbf{F}(\mathbf{h}) - \mathbf{F}(\mathbf{h} - (p - k) \, \mathbf{q}_{\perp})] \Big\}, \end{aligned}$$
$$\delta E(\mathbf{h}, p, k) &= \frac{\mathbf{h}^2}{2pk(p-k)} + \frac{m_k^2}{2k} + \frac{m_{p-k}^2}{2(p-k)} - \frac{m_p^2}{2p}. \end{aligned}$$

• *m*<sup>2</sup>: Medium induced thermal masses.

•  $\mathbf{h} = (\mathbf{p} \times \mathbf{k}) \times \mathbf{e}_{||}$  — Must keep track of both  $\mathbf{p}_{\perp}$  and  $\mathbf{k}_{\perp}$  now. For photons, we could just set  $\mathbf{k}_{\perp} = 0$ .

# **Gluon Radiation Rate**

#### Rate using F



where  $x \equiv k/p$  is the momentum fraction in the gluon (or either quark, for the case  $g \rightarrow qq$ ). **h**  $\equiv$  **p**  $\times$  **k**: 2-D vector.  $O(gT^2)$ 

• Correctly incorporates both the BH limit and the LPM limit.

## Elastic scattering rate

Coulombic t-channel dominates



#### We need

$$\frac{dE}{dt} = \frac{1}{2E} \int_{k,k',p'} \delta^4(p+k-p'-k') (E-E') |M|^2 f(E_k) [1 \pm f(E'_k)] \\ = C_r \pi \alpha_s^2 T^2 \left[ \ln(ET/m_g^2) + D_r \right]$$

where  $C_r$  and  $D_r$  are channel dependent O(1) constants.

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# Putting them together

Fokker-Planck Eqn.

$$\begin{aligned} \frac{dP_{q\bar{q}}(p)}{dt} &= \int_{k} P_{q\bar{q}}(p+k) \frac{d\Gamma_{qg}^{q}(p+k,k)}{dkdt} - P_{q\bar{q}}(p) \frac{d\Gamma_{qg}^{q}(p,k)}{dkdt} \\ &+ 2P_{g}(p+k) \frac{d\Gamma_{q\bar{q}}^{g}(p+k,k)}{dkdt} , \\ \frac{dP_{g}(p)}{dt} &= \int_{k} P_{q\bar{q}}(p+k) \frac{d\Gamma_{qg}^{q}(p+k,p)}{dkdt} + P_{g}(p+k) \frac{d\Gamma_{gg}^{g}(p+k,k)}{dkdt} \\ &- P_{g}(p) \left( \frac{d\Gamma_{q\bar{q}}^{g}(p,k)}{dkdt} + \frac{d\Gamma_{gg}^{g}(p,k)}{dkdt} \Theta(k-p/2) \right) \end{aligned}$$

•  $\Gamma = \Gamma_{el} + \Gamma_{inel}$ 

- Inelastic part is solved as it is.
- Elastic part Soft exchange dominated. Implement it as drag + diffusion
- Get T(x, t) and  $u^{\mu}(x, t)$  from 3+1 D Hydro

# (3+1)-D relativistic hydrodynamics (Nonaka & Bass)

- Based on conservation laws:  $\partial_{\mu}T^{\mu\nu} = 0, \partial_{\mu}j^{\mu} = 0.$
- For ideal fluid,  $T^{\mu\nu} = (\epsilon + p)U^{\mu}U^{\nu} pg^{\mu\nu}, j^{\mu} = n_BU^{\mu}$ .
- EOS: Bag model + Hadron with extended volume
- Initial conditions:  $\epsilon(x, y, \eta) = \epsilon_{\max} W(x, y; b) H(\eta)$ ,  $n_B(x, y, \eta) = n_{B\max} W(x, y; b) H(\eta)$



Particle spectra: Cooper-Frye Formula

$$Erac{dN_i}{d^3
ho} = \int_{\Sigma} 
ho \cdot d\sigma rac{g_i}{(2\pi)^3} rac{1}{\exp\left[(
ho \cdot U - \mu_i)/T_{
m f}
ight] \pm 1}$$

Nonaka and Bass, Phys.Rev.C75:014902,2007

## Following calculations mostly by

# Guangyou Qin (Rad + Coll, 3+1 Hydro) and Simon Turbide (Rad only, Bjorken Hydro)

#### with C. Gale, S. Jeon, G. Moore and J. Ruppert (McGill-AMY)

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# Example evolution of a single jet (Qin)

 The final momentum distribution P(E, t<sub>f</sub>) of a single quark jet after passing through RHIC medium (b = 2.4 fm)



- Medium described by (3+1)D ideal hydrodynamics.
- The jet starts at the center and propagates in plane.
- Jet energy loss turned off in hadronic phase.

# Averaged energy loss of a single jet (Qin)

 The averaged energy loss of a quark jet after passing through RHIC medium (b = 2.4 fm)



• Averaged energy:  $\langle E \rangle = \int dEEP(E) / \int dEP(E)$ 

Qin et al., arXiv:0710.0605 [hep-ph], PRC, in press, arXiv:0705.2575 [hep-ph]

# **Pion Production**

 Fold in the nuclear geometry, local production rate, jet angles, with the energy loss

$$\begin{aligned} \frac{dN_{AA}}{dyd^{2}\mathbf{p}_{T}} &= \frac{\langle N_{\text{coll}} \rangle}{\sigma_{in}} \sum_{a,b,c,d} \int dx_{a} dx_{b} g_{A}(x_{a},Q) g_{A}(x_{b},Q) \\ &\times \mathcal{K}_{\text{jet}} \frac{d\sigma_{a+b\to c+d}}{dt} \frac{\tilde{D}_{\pi^{0}/c}(z,Q)}{\pi z} \end{aligned}$$
with  $\tilde{D}_{\pi^{0}/c}(z,Q) = \int d^{2}r_{\perp} \mathcal{P}(\mathbf{r}_{\perp}) \tilde{D}_{\pi^{0}/c}(z,Q,\mathbf{r}_{\perp},\mathbf{n}), \text{ and } \\ \tilde{D}_{\pi^{0}/c}(z,Q,\mathbf{r}_{\perp},\mathbf{n}) = \int dp_{f} \frac{z'}{z} \left( P_{qq/c}(p_{f};p_{i};\Delta t) D_{\pi^{0}/c}(z',Q) + P_{g/c}(p_{f};p_{i};\Delta t) D_{\pi^{0}/c}(z',Q) \right) \end{aligned}$ 

with  $z = p_T/p_i$  and  $z' = p_T/p_f$ .

# $R_{AA}$ at RHIC - $\pi^0$ - Radiation only (Turbide)



 $T_i = 370 \text{ MeV}, dN/dy = 1260. \text{ 1-D Bjorken expansion.}$ Best  $\alpha_s = 0.33 \text{ s.Turbide, C.Gale, S.J. and G.Moore, PRC72:014906,2005}$ 

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# $R_{AA}$ at RHIC – $\pi^0$ - Full (Qin)



#### • total, rad, coll

#### Strong coupling α<sub>s</sub> tuned from 0.33 to 0.27

Qin et al., arXiv:0710.0605 [hep-ph], PRC, in press, arXiv:0705.2575 [hep-ph], 🗀 🕹 🖉 🖕 🦉 🚊 🖉 🖉

# $R_{AA}$ vs. reaction plane at RHIC (Qin)

•  $R_{AA}$  for  $\pi^0$  in plane and out of plane at RHIC (different *b*) 0.40.3 b = 7.5 fm ≅<sup>₹</sup>0.2  $- b = 2.4 \text{ fm}, \phi = 0$ -- b = 2.4 fm,  $\phi = \pi/2$ **—**  $b = 4.5 \text{ fm}, \phi = 0$ -- b = 4.5 fm,  $\phi = \pi/2$ 0.1  $b = 7.5 \text{ fm}, \phi = 0$  $b = 7.5 \text{ fm}, \phi = \pi/2$ 0 5 10 15 20 25 p<sub>T</sub> (GeV/c)

 Jets propagating out of plane (φ = π/2) are suppressed more than in plane (φ = 0)

# PHENIX data from QM06 (Pantuev's talk)



-RAA in plane and out of plane changes by factor ~2

- For peripheral bins no suppression in plane, while a factor ~2 out of plane 13

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# LHC R<sub>AA</sub> (Turbide)



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# Where are we now?

- Most models have jet quenching under control in the hadronic part.
- But  $R_{AA}$  too simple to be the full story.
- More information?  $\gamma$  production
  - Need:
    - Thermal photon radiation rate (AMY)
    - Jet bremsstrahlung rate (AMY)
    - Jet-photon conversion rate (Fries, Mueller, Srivastava)

# Various sources of photons



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Arnold, Moore and Yaffe (AMY), JHEP 0206:030,2002; JHEP 0112:009,2001; JHEP 0111:057,2001



Need to sum over the scattering centers and the radiation points.

## Remember this slide?

 Collinear enhancement in photon & gluon radiations Aurenche, Gelis, Kobes and Zaraket, PRD58:085003,1998, Arnold, Moore and Yaffe (AMY), JHEP 0206:030,2002; JHEP 0112:009,2001; JHEP 0111:057,2001



#### Schwinger-Dyson Equation



Arnold, Moore and Yaffe, JHEP 0112 (2001) 009

The same formalism can be used to calculate thermal radiation ( $P \sim T$ ) and bremsstrahlung from jets ( $P \gg T$ ).

# Jet-Thermal Conversion



Fries, Mueller, Srivastava (nucl-th/0208001)

$$\frac{dR}{dyd^2p_T} = \sum_f \left(\frac{e_f}{e}\right)^2 \frac{T^2 \alpha \alpha_s}{8\pi^2} [f_q(\vec{p}_{\gamma}) + f_{\bar{q}}(\vec{p}_{\gamma})] \left[2\ln\left(\frac{4E_{\gamma}T}{m^2}\right) - C\right]$$
with  $C \approx 2.33$ .

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# Putting everything together for $\gamma$ ...

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#### $\gamma$ – Baseline



Using P.Aurenche et al.'s pQCD program.

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E-Loss

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# $\gamma$ – Composition (Turbide)



# $\gamma$ – Our Calc vs. PHENIX Data (Turbide)



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# $\gamma$ – Our Prediction vs. Data (Turbide)



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# $\gamma$ – Composition – LHC (Turbide)



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# $\gamma - LHC$ prediction (Turbide)



# G. Qin - Photon production at RHIC

#### Photon production in Au+Au collisions at RHIC from various sources:



#### 3+1 D hydro. Rad + Coll E-loss.

Jet-plasma photons (bremsstrahlung and jet-conversion) are significant to understand the photon data in AA collisions Qin *et al*, in preparation

# G. Qin - Application: Photon-tagged jets

At LO, Compton scattering and annihilation process:



Wang, Huang, Sarcevic, PRL **77**, 231-234 (1996) Proposed advantage for photon-tagged jets (at LO):

$$E_{\rm jet} = E_{\gamma}$$

The photon is strongly correlated with the away-side jet  $\rightarrow$  a calibrated probe of the QGP.

#### How does it look like in a full calculation?

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# Results for photon-hadron correlations (Qin)

#### Centrality dependence of $I_{AA}$ and yield per trigger for away-side $\pi^0$ :



Both  $I_{AA}$  and yield per trigger are consistent with current data! Qin *et al*, in preparation Data from QM2008: Mohanty's plenary talk and Hamed's parallel talk

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# G. Qin - Contributions from different source of photons

Probability distributions of the initial jets tagged by different photons:

Different contributions to yield per trigger for away-side  $\pi^0$ :

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Direct photon-tagged jets dominate at lower  $p_T$ , jet-plasma and fragmentation photon-tagged jets dominated at higher  $p_T$ . Qin *et al*, in preparation

# G. Qin - What is the importance of additional processes?

 $I_{AA}$  for the away-side  $\pi^0$  for different photon triggers:



- Calculated Jet Quenching with radiational *and* collisional energy loss
- Radiational part plays bigger role, but collisional part not negligible.
- Best fit  $\alpha_s$  reduced by 10 %
- Important to use the full momentum distribution at any given time, not just dE/dx.
- Geometry and 3+1 D expansion included.
- Best we can do using perturbative results (We keep track of radiated partons as well)
- Good description of existing data pions and photons.
- For photons, jet-thermal interaction is crucial.
- LHC predictions Should be better since pQCD should work better there.
- Photon spectra + Photon tagged jets Preview version at HP08, full version soon

- Calculations consistent in the  $g \ll 1$  limit for momenta T < p. Yet for quantitative calculations, we needed  $\alpha_s \approx 1/3$  or  $g \approx 2!$  So in reality, one must sum all diagrams, not just pinching part of the ladder diagrams!
  - At this leading order, α<sub>s</sub> is an overall factor. So one might hope that the structure of the solution is OK.
  - Right now, this is best we can do with perturbative calculation.



Included in the PDF scale dependence



- What about jet correlations? Need to keep track of the evolution of the joint probability function of two jet energies. Much harder than single particle distributions!
- Most energy-loss calculations these days do get R<sub>AA</sub> right. Is there an experimental way to distinguish?

 Photon bremsstrahlung + jet-photon conversion should be able to distinguish different scenarios. How to fish that out of all others is another matter.

 It is important to keep in mind that photon tagging is not 100 % efficient!